




# Advanced Hybrid-ARQ Receivers for Broadband MIMO Communications

Soutenance  
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pour Obtenir le grade de  
**DOCTEUR DE TELECOM BRETAGNE**  
en habilitation conjointe avec l'Université  
de Bretagne Sud





# Advanced Hybrid-ARQ Receivers for Broadband MIMO Communications

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# Motivations and General Framework

## ■ Main objective:

How to efficiently combine multiple transmissions (diversity gain) while maintaining an affordable receiver complexity?

## ■ General Framework

- ✓ Chase-type ARQ
- ✓ Channel is short-term quasi-static block fading.
- ✓ Mutli-paths MIMO channels
- ✓ Cyclic-prefix (CP) transmissions to prevent inter-block interference (IBI).
- ✓ Frequency Domain Processing



# Presentation Outline

- **New Class of Turbo Packet Combiners**
- **Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)**
- **Turbo Packet Combining for Broadband MIMO CDMA Systems**
- **Generalized ARQ for Broadband Cooperative Communications**
- **Conclusions and Future Work**



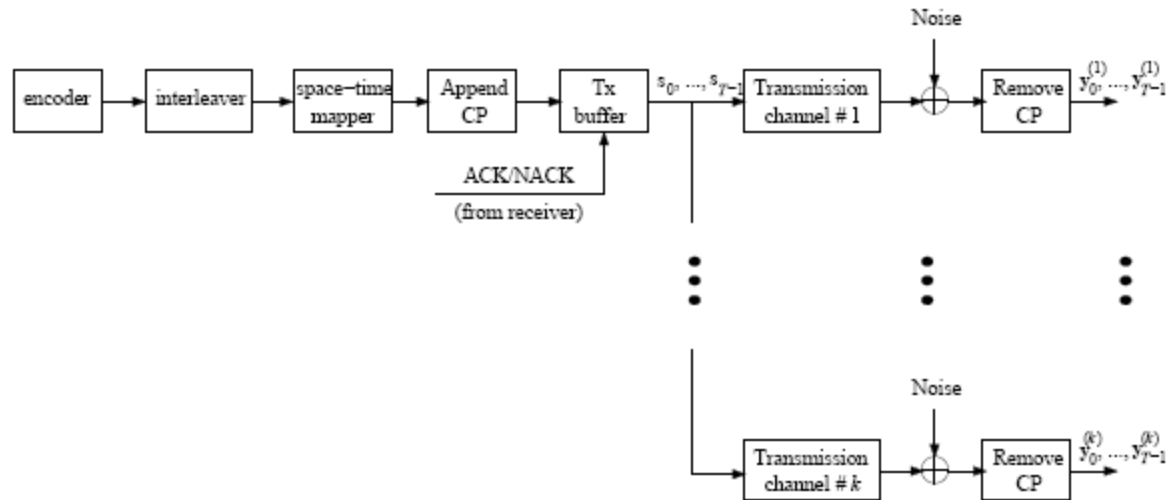
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- **New Class of Turbo Packet Combiners**
- Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)
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# New Class of Turbo Packet Combiners

## Transmission Scheme



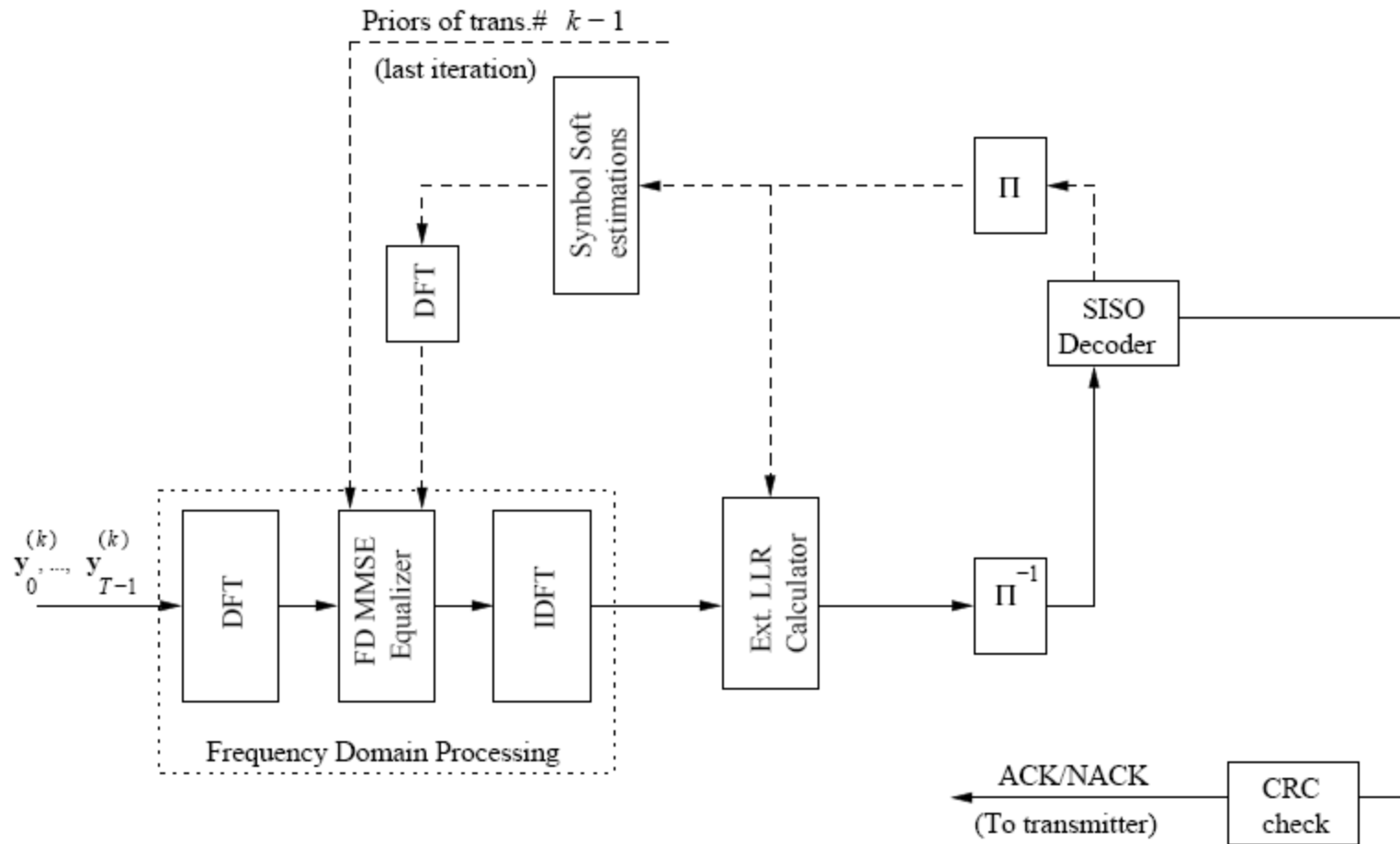
- ✓ At each transmission #  $k$ , a point to point MIMO link with  $N_T$  transmit and  $N_R$  receive antennas.
- ✓  $s_0, \dots, s_{T-1} \in S^{N_T}$  are the symbol vectors.
- ✓  $L$  paths MIMO channel:  $\mathbf{H}_0^{(k)}, \dots, \mathbf{H}_{L-1}^{(k)} \in \mathbb{C}^{N_R \times N_T}$ .

$$\mathbf{y}_i^{(k)} = \sum_{l=0}^{L-1} \mathbf{H}_l^{(k)} s_{(i-l) \bmod T} + \mathbf{n}_i^{(k)} \quad (1)$$



# New Class of Turbo Packet Combiners

## Receiver Scheme with no Packet Combining





# New Class of Turbo Packet Combiners

## Virtual Receive Antenna Concept

- Key idea:

ARQ rounds  $\Leftrightarrow$  Virtual receive antennas  
One (re)transmission  $\sim$  One set of  $N_R$  virtual Rx antennas.

- Dimensionality of the communication model at round  $k$ :  $kN_R$  receive and  $N_T$  transmit antennas.
- Transmissions translate into additional diversity branches.

$$\begin{bmatrix} y_i^{(1)} \\ \vdots \\ y_i^{(k)} \end{bmatrix} = \sum_{l=0}^{L-1} \begin{bmatrix} \mathbf{H}_l^{(1)} \\ \vdots \\ \mathbf{H}_l^{(k)} \end{bmatrix} s_{(i-l) \bmod T} + \begin{bmatrix} n_i^{(1)} \\ \vdots \\ n_i^{(k)} \end{bmatrix} \quad (2)$$

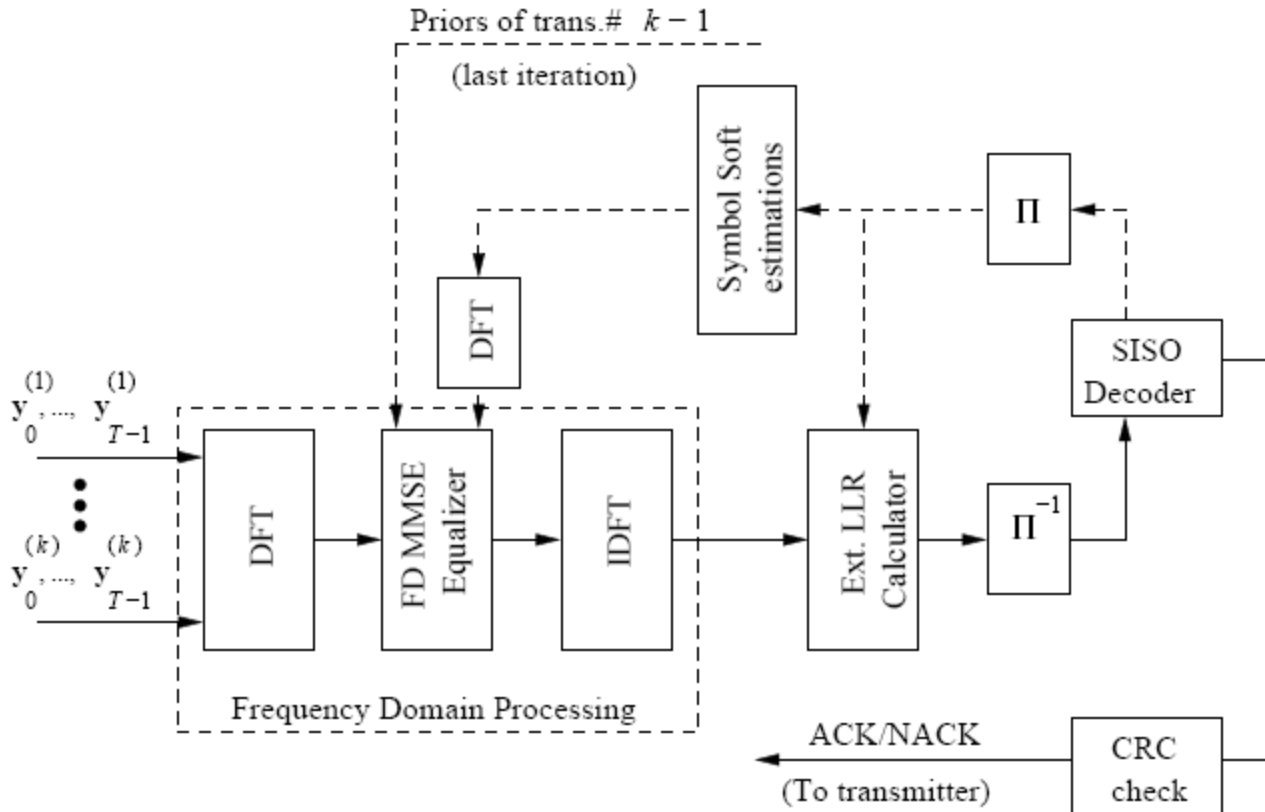




# New Class of Turbo Packet Combiners

## Signal-Level Turbo Packet Combining Scheme

### Receiver Architecture



T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Joint Hybrid ARQ and Iterative Space-Time Equalization for Coded Transmission over MIMO-ISI Channel," *IEEE WCNC 2008*, Las Vegas, NV, Mar-Apr. 2008.



# New Class of Turbo Packet Combiners

## Implementation Issues

- The proposed combining strategy **BOTTLENECK**:

Matrix inversion  $\Leftrightarrow$  complexity in order of  $O(k^3 N_R^3)$ .

Store received signals and their channels  $\Rightarrow$   
Memory size increases linearly with the number of retransmissions

- **Solution:**

### **Recursive Combining Strategy**

Translates the problem dimensionality from  $kN_R$  into  $N_T$

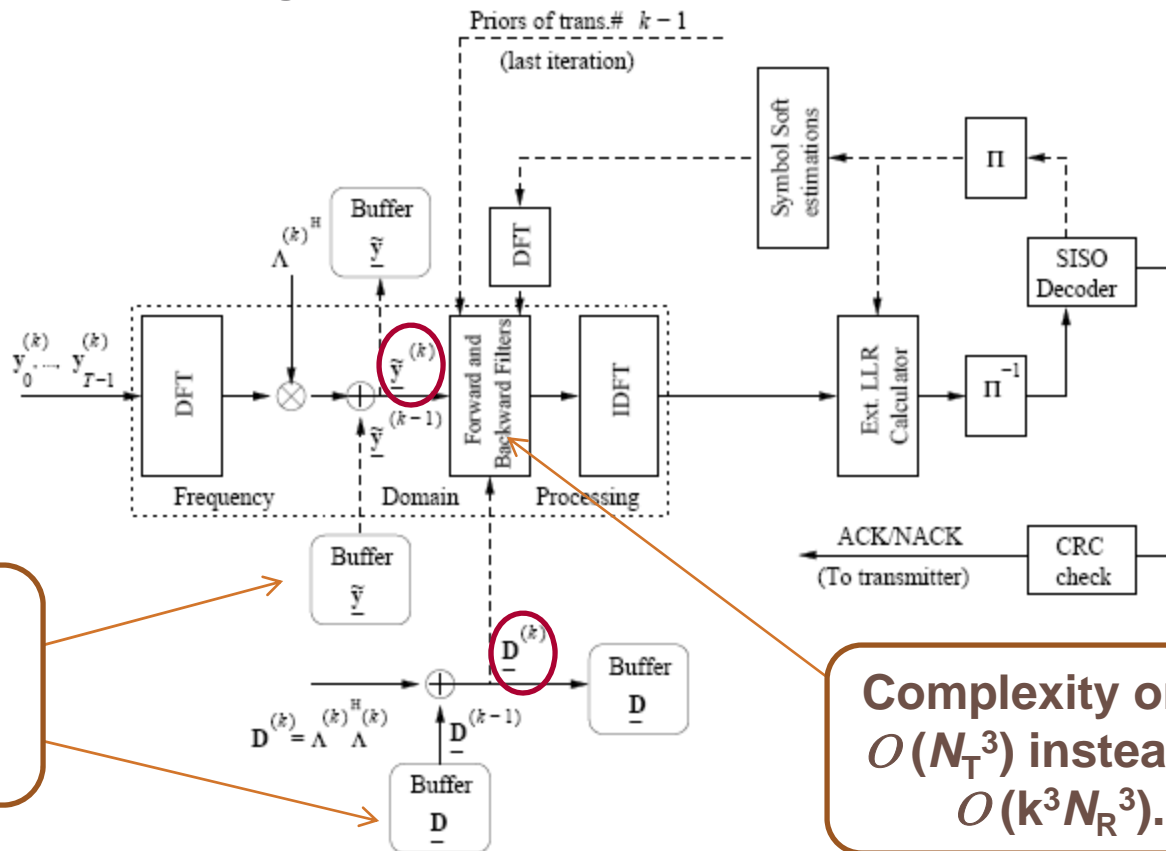
**H. Chafnaji**, T. Ait-Idir, H. Yanikomeroğlu, and S. Saoudi, "On the Design of Turbo Packet Combining Schemes for Relay-Assisted Systems over Multi-Antenna Broadband Channels," *IEEE 71st Semi-Annual VTC10Spring*, Taipei, Taiwan, May 2010.



# New Class of Turbo Packet Combiners

## Recursive Combining Scheme

New variables recursively computed ~ The packet combining algorithm remains identical from one



Memory size insensitive to  $kN_R$

Complexity order  $O(N_T^3)$  instead of  $O(k^3 N_R^3)$ .



# New Class of Turbo Packet Combiners

## Performance Evaluation (1/3)

### Simulation Settings

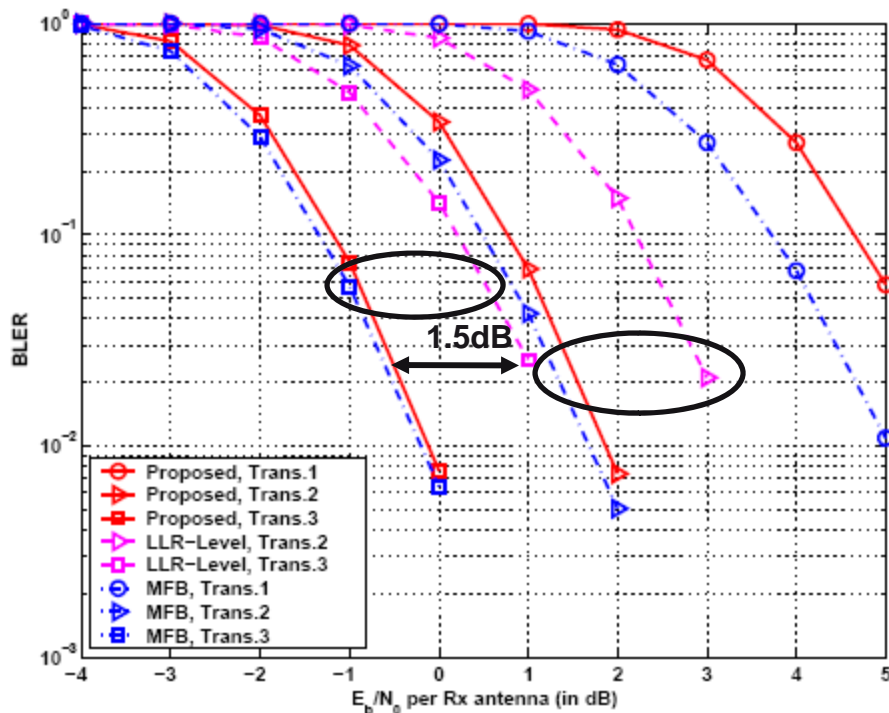
- **CC(35; 23)<sub>8</sub>, semi-random interleaving, and QPSK signaling.**
- **Coded block length: 1032 (including tails). EQual power taps channel profile.**
- **SISO decoding: Max-Log-MAP.**
- **Number of transmissions:  $K = 3$ .**
- **Number of channel paths:  $L = 10$ .**
- **Number of iterations:  $N_{iter} = 3$ .**
- **Performance evaluation: BLER and Throughput vs  $E_b/N_0$  (/Rx antenna/info bit).**
- **Benchmark: Coded matched filter bound (MFB)**
- **Reference: Conventional LLR-level combining.**



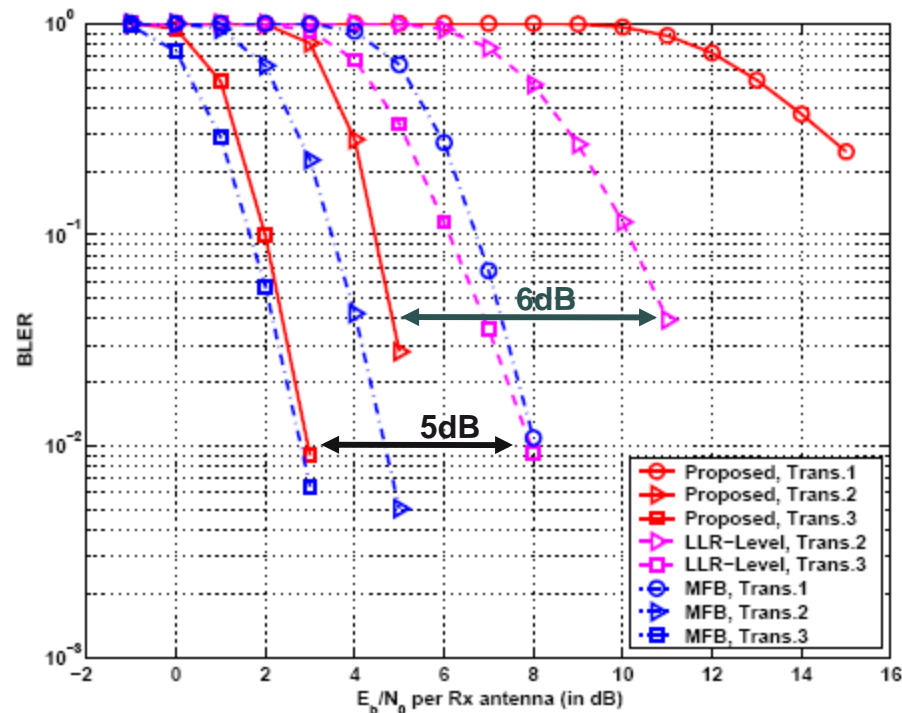
# New Class of Turbo Packet Combiners

## Performance Evaluation (2/3)

### BLER Performances



$$N_T = N_R = 2$$



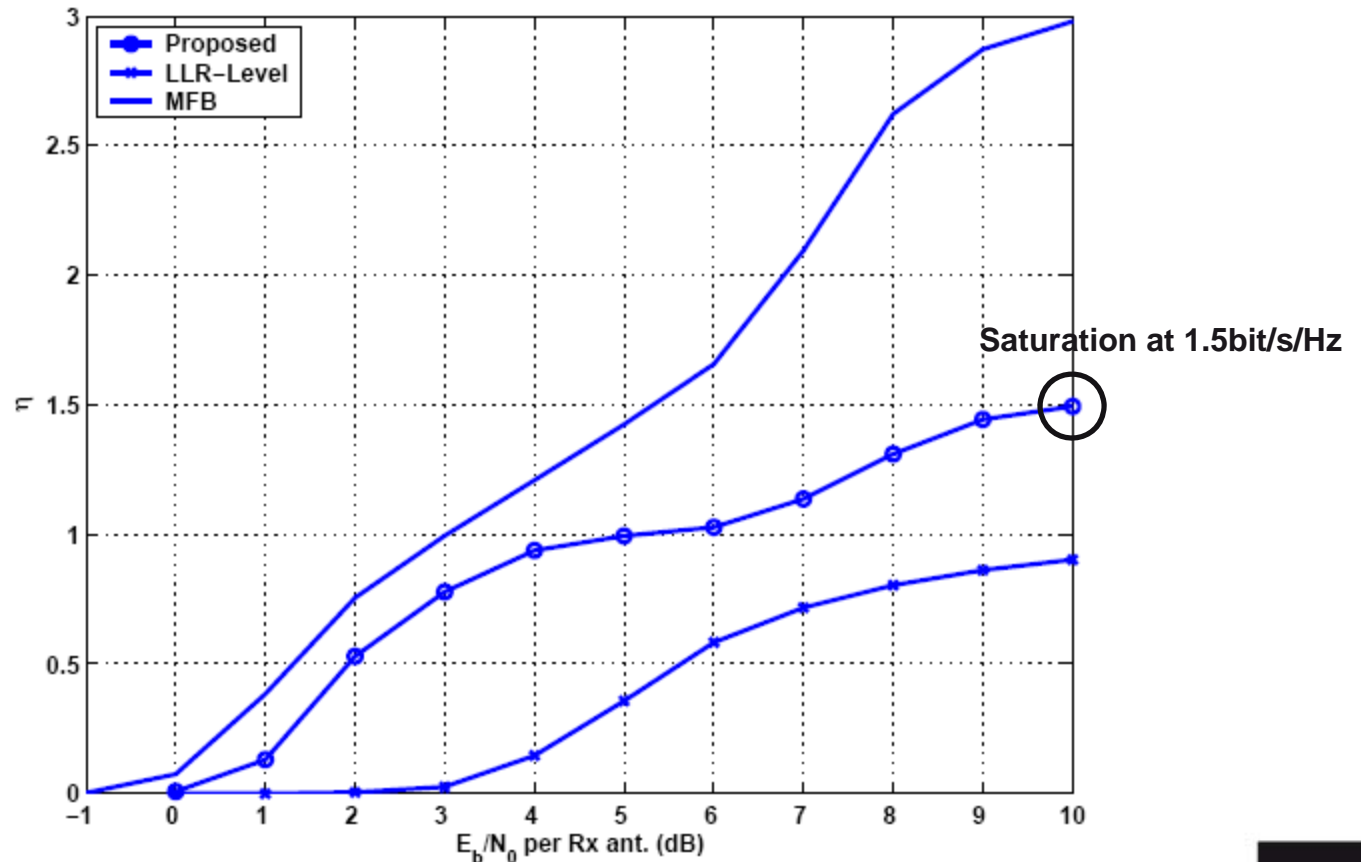
$$\text{Overloaded system } N_T = 4, N_R = 2$$



# New Class of Turbo Packet Combiners

## Performance Evaluation (2/3)

Throughput: Overloaded system  $N_T = 3, N_R = 1$





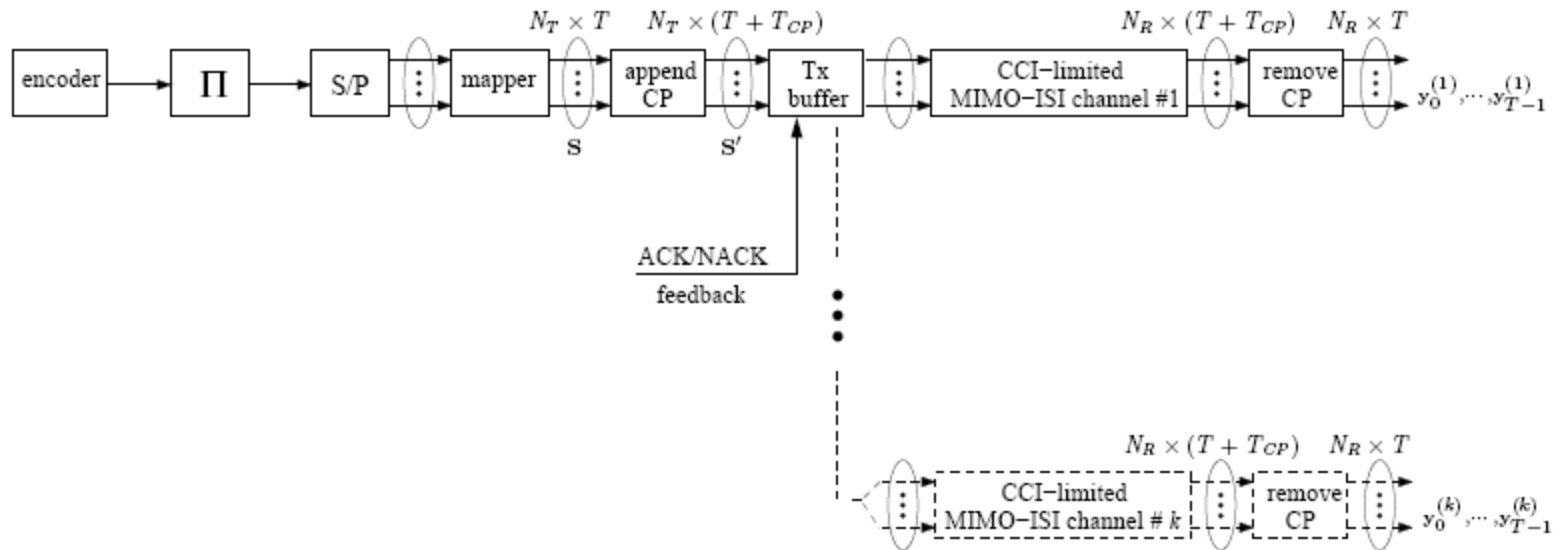
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# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

## General Framework:

Cyclic Prefix (CP)-aided single carrier transmission under the presence of CCI

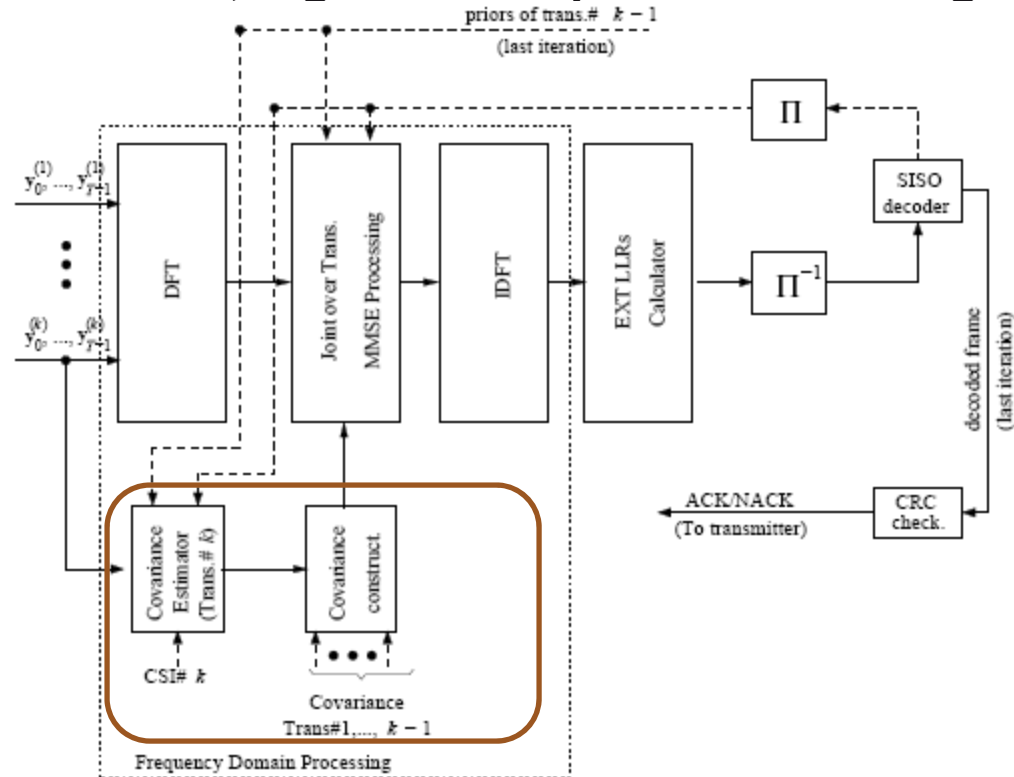


$$y_i^{(k)} = \sum_{l=0}^{L-1} \mathbf{H}_l^{(k)} s_{(i-l) \bmod T} + \underbrace{\sum_{l'=0}^{L'-1} \mathbf{H}_{l'}^{\text{CCI}(k)} s_{(i-l') \bmod T} + \mathbf{n}_i^{(k)}}_{\mathbf{w}_i^{(k)} = \text{CCI+noise}}, \quad (3)$$



# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

**Signal-Level Turbo Packet Combining Architecture:**  
 Iterative turbo estimation of CCI covariance matrix in the frequency domain, together with packet combining.



# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

## Asymptotic Performance (1/2)

- We assume perfect LLR feedback from the SISO decoder.
- The interferer CSI is perfectly known
- $\rho_k$  is the rank of CCI covariance matrix at round  $k$ .

**Theorem:** We consider a CCI-limited MIMO ARQ system with  $N_T$  transmit and  $N_R$  receive antennas, and ARQ delay  $k$ . The signal-level packet combiner provides perfect CCI suppression for asymptotically high SNR if

$$\sum_{u=1}^k \rho_u < kN_R - N_T. \quad (4)$$

# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

## Asymptotic Performance (2/2)

$$\sum_{u=1}^k \rho_u < kN_R - N_T. \quad (4)$$

### ■ System Interpretations:

- **Impact of CCI fading channel:** Interference is desired with users having low channel ranks.
- **Impact of the Nbr of Tx antennas and ARQ delay:** Increase  $K$  and/or reduce  $N_T$ .

T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Turbo Packet Combining for Broadband Space-Time BICM Hybrid-ARQ Systems with Co-Channel Interference," *IEEE Transactions on Wireless Communications*, vol. 9, no. 5, pp. 1686-1697, May 2010.

T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Frequency Domain Hybrid-ARQ Chase Combining for Broadband MIMO Communication with Co-Channel Interference," *IEEE GLOBECOM 2009*, Honolulu, Hawaii, Nov-Dec. 2009.

# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

## Performance Evaluation (1/2)

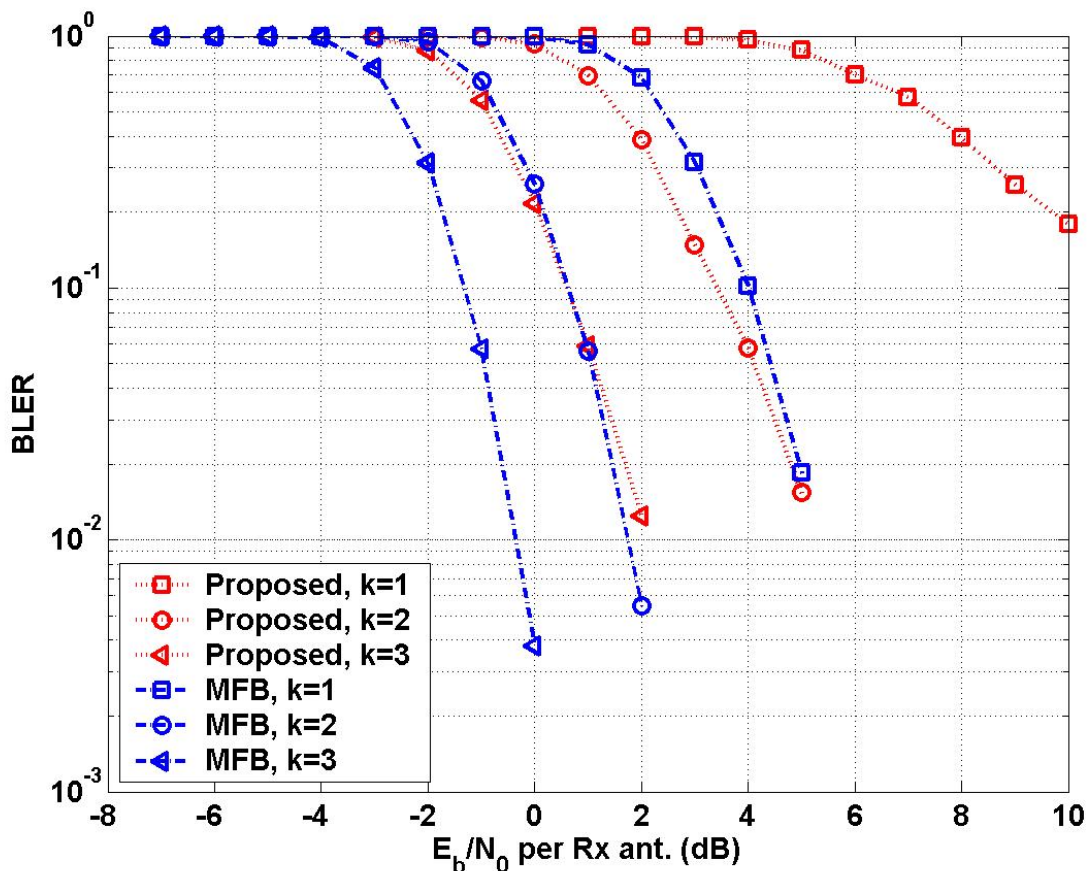
### Simulation Settings

- CC(35; 23)<sub>8</sub>, semi-random interleaving, and QPSK signaling.
- Coded block length: 1032 (including tails). EQual power taps channel profile.
- SISO decoding: Max-Log-MAP.
- Number of transmissions:  $K = 3$ .
- Number of channel paths:  $L = 2$ .
- Number of iterations:  $N_{\text{iter}} = 3$ .
- Performance evaluation: BLER vs  $E_b/N_0$  (/Rx antenna/info bit).
- Benchmark: Coded matched filter bound (MFB).

# Turbo Packet Combining for MIMO ARQ with Co-Channel Interference (CCI)

## Performance Evaluation (2/2)

$N_R=N_T=4$ ,  $L=2$ , and  $SIR = 1\text{dB}$



$N_T = 2$ ,  $L' = 1 \Rightarrow \rho=2$

Asymptotic Analysis:

Perfect CCI  
cancellation  
for  $k = 3$

Simulations:

Better  
CCI cancellation  
for  $k = 3$



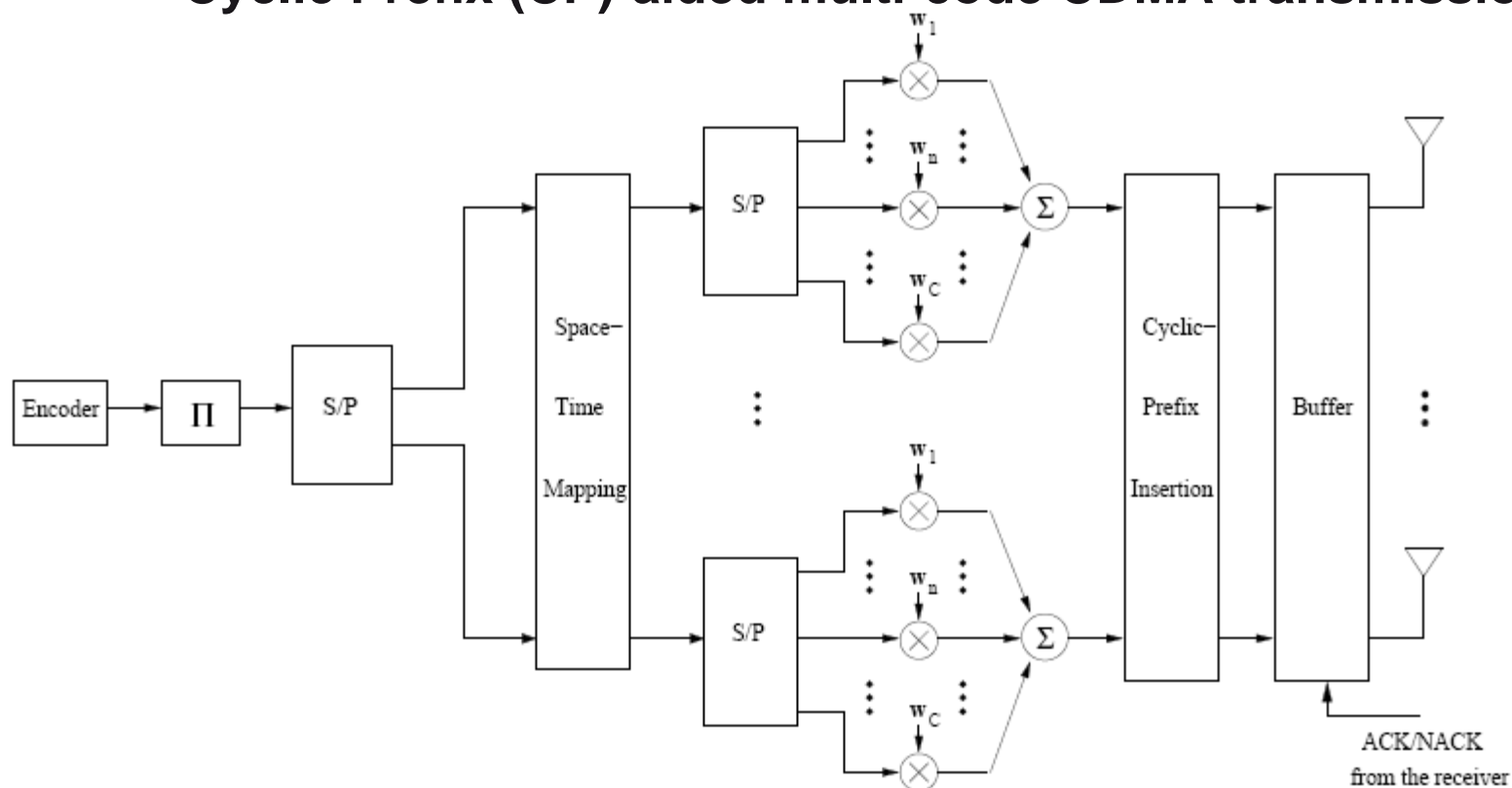
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# Turbo Packet Combining for Broadband MIMO CDMA Systems

## General Framework:

### Cyclic Prefix (CP)-aided multi-code CDMA transmission





# Turbo Packet Combining for Broadband MIMO CDMA Systems

## Iterative Receivers for Multi-Code CDMA ARQ

- **Chip-Level Turbo Packet Combiner: Straightforward extension of signal-level turbo packet combiner**
- **Symbol-Level Turbo Packet Combiner: Combining is performed jointly with the soft symbol demapper**

**H. Chafnaji**, T. Ait-Idir, and S. Saoudi, "Packet Combining and Chip Level Frequency Domain Turbo Equalization for Multi-Code Transmission over Multi-Antenna Broadband Channel," *19th Annual IEEE Symposium PIMRC 2008*, Cannes, France, Sep. 2008.

**H. Chafnaji**, T. Ait-Idir, and S. Saoudi, "A comparative study of frequency domain HARQ Chase combining schemes for broadband single carrier MIMO CDMA systems," Accepted to *IEEE GLOBECOM 2010*, Miami, Florida, USA, 6 December 2010.



# Turbo Packet Combining for Broadband MIMO CDMA Systems

## Performance Evaluation (1/4)

### Simulation Settings

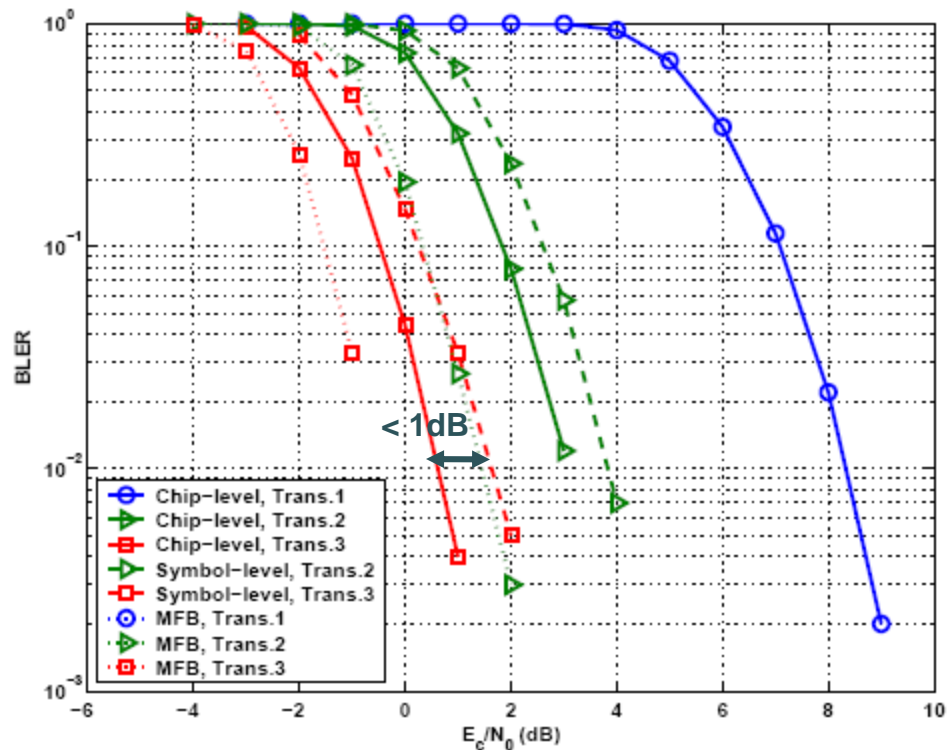
- $CC(35; 23)_8$ , semi-random interleaving, QPSK signaling, and spreading factor  $SF = 16$ .
- Coded block length: 1024 (including tails). EQual power taps channel profile.
- SISO decoding: Max-Log-MAP.
- Number of transmissions:  $K = 3$ .
- Number of channel paths:  $L = 10$ .
- Number of iterations:  $N_{iter} = 3$ .
- Performance evaluation: BLER and Throughput vs  $E_c/N_0$  (/Rx antenna/chip).
- Benchmark: Coded matched filter bound (MFB).

# Turbo Packet Combining for Broadband MIMO CDMA Systems

## Performance Evaluation (2/4)

BLER Performances:  $N_T = N_R = 4$  and  $C = 16$

$$C_{memory}(\text{Chip\_Comb}) = 5 \cdot C_{memory}(\text{Symbol\_Comb})$$

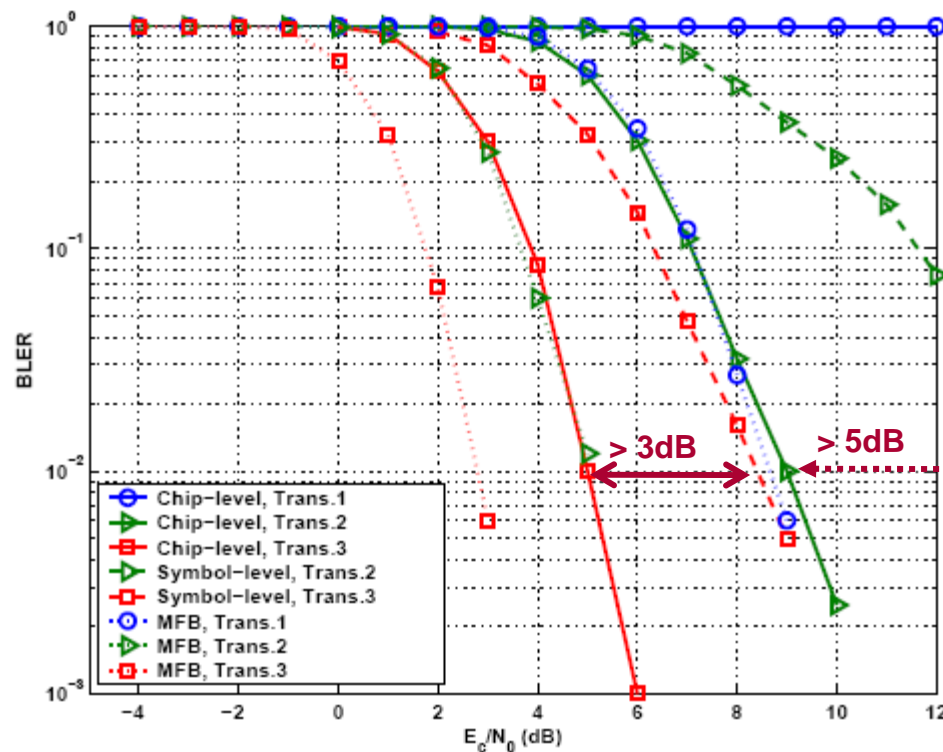


**Symbol-Level combining is the best candidate with a low implementation cost and a small performance loss**

# Turbo Packet Combining for Broadband MIMO CDMA Systems

## Performance Evaluation (3/4)

BLER Performances:  $N_T=2$ ,  $N_R=1$ , and  $C=16$



# Turbo Packet Combining for Broadband MIMO CDMA Systems

## Performance Evaluation (4/4)

### Throughput Performances: $N_T=2, N_R=1$

High ICI:  $C = 16$

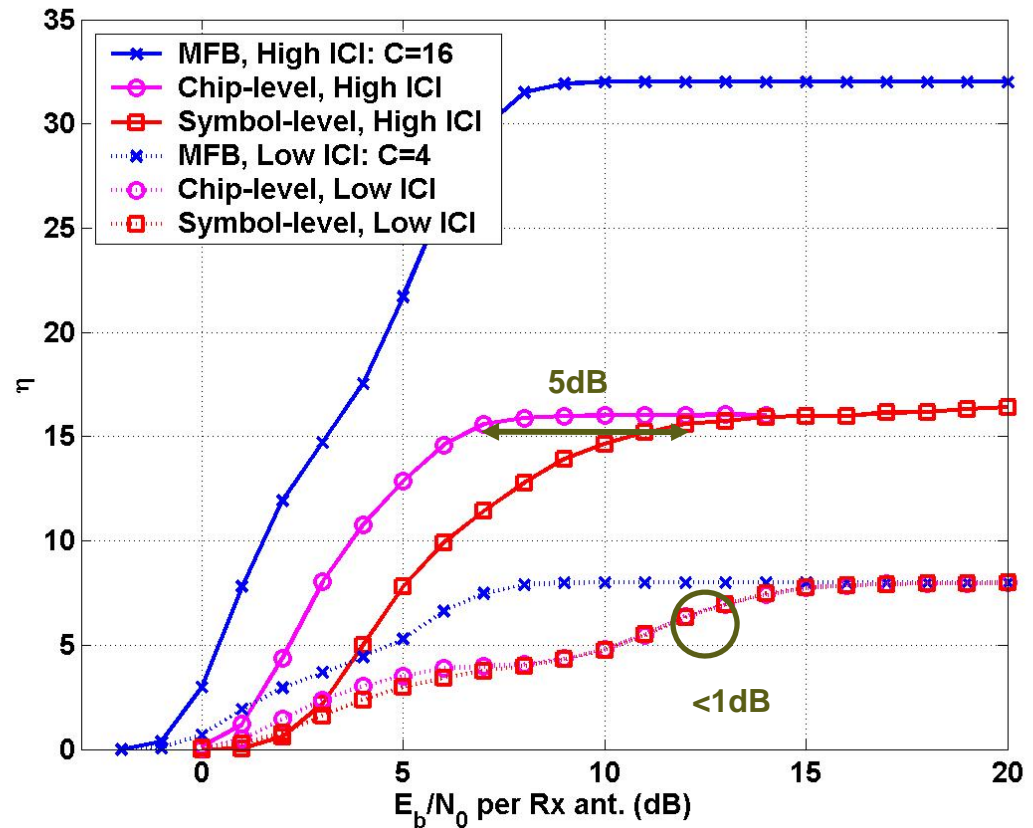
$$C_{memory}(\text{Chip\_Comb}, C=16) = 1.5C_{memory}(\text{Symbol\_Comb}, C=16)$$

⇒ **Chip-Level Combining is the BEST**

Low ICI:  $C = 4$

$$C_{memory}(\text{Chip\_Comb}, C=4) = 12C_{memory}(\text{Symbol\_Comb}, C=4)$$

⇒ **Symbol-Level Combining is the BEST**



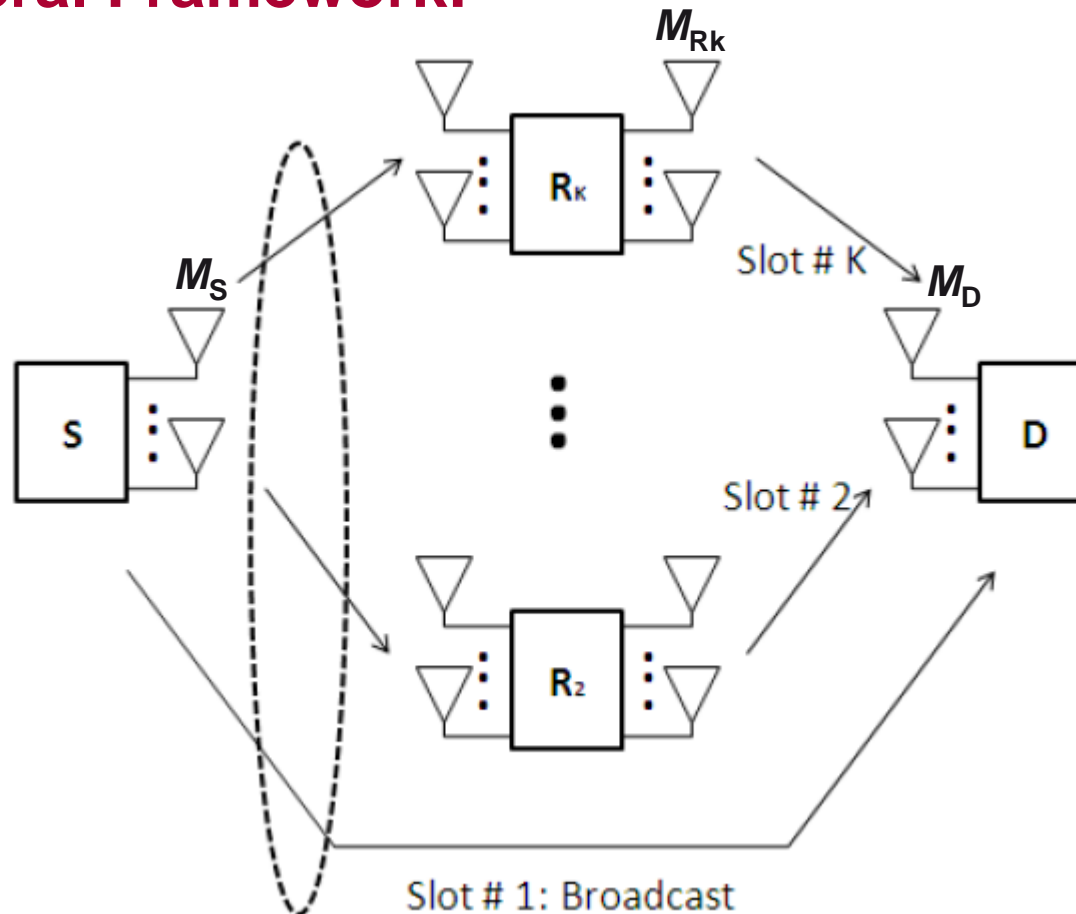


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# Generalized ARQ for Broadband Cooperative Communications

## General Framework:





# Generalized ARQ for Broadband Cooperative Communications

## ■ Problem

How to extend the proposed combining strategy to cooperative communications operating under the framework of multi-paths MIMO channels?

## ■ Main Concern

Build an appropriate system model to mask the cooperation and simplify the application of virtual antenna based combining

# Generalized ARQ for Broadband Cooperative Communications

## Relaying Schemes

### ■ Amplify-and-Forward scheme:

The relay simply amplifies the received signal and forwards it towards the destination during the allocated slot.

### ■ Decode-and-Forward schemes

#### ➤ Selective Decode-and-Forward scheme:

The relay only transmits when it can reliably decode the data packet.

#### ➤ Modified Selective Decode-and-Forward scheme:

To prevent the occurring "silence", when the relay fails to correctly decode the packet, it sends back a NACK message to the source that directly transmits the packet to the destination during the allocated relay slot.





# Generalized ARQ for Broadband Cooperative Communications

## Amplify-and-Forward scheme

### ■ Problem

Transmissions over relaying links in AF scheme suffer from colored noise as well as correlation between source-to-relay and relay-to-destination multi-path channels.

### ■ Solution to mask this cooperation problems

Perform whitening using Cholesky decomposition and derive an equivalent source-to-relay-to-destination channel

# Generalized ARQ for Broadband Cooperative Communications

## Decode-and-Forward scheme

### ■ Problem

Heterogeneous nature of cooperative networks where the different nodes are equipped with different number of antennas.

### ■ Solution to mask this cooperation problems

Derive a fixed rate equivalent multi-antenna system communication model where the multi-rate multi-node received signals can be viewed as direct retransmissions from a virtual node with a fixed transmission rate.

H. Chafnaji, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "Signal-level turbo packet combining for multi-rate relay-assisted systems over multi-antenna broadband channels," Accepted to *IEEE GLOBECOM 2010*, Miami, Florida, USA, 6-10 December 2010.

# Generalized ARQ for Broadband Cooperative Communications

## Performance Evaluation (1/5)

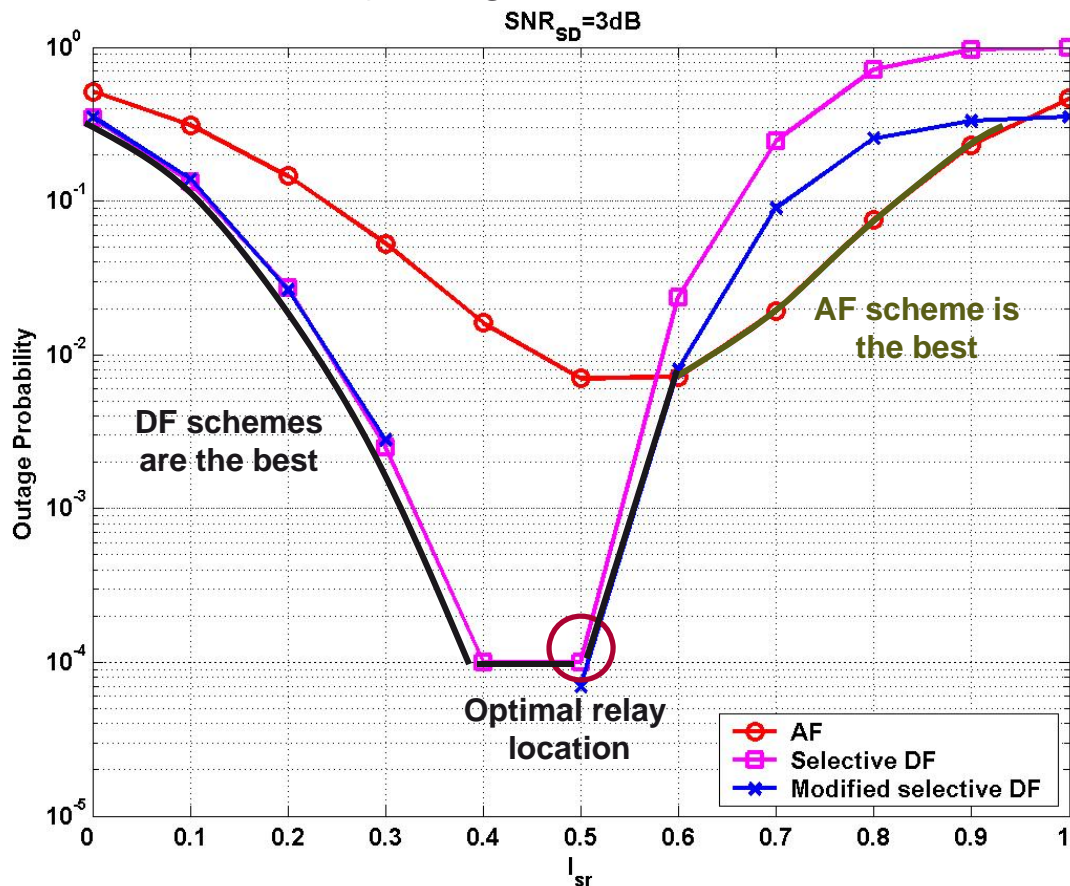
### Simulation Settings

- The distances are normalized:  $l_{SR} + l_{RD} = l_{SD} = 1$ .
- All digital nodes use the same BICM scheme.
- Coded block length: 2048 (including tails).
- SISO decoding: Max-Log-MAP.
- All links have the same channel profile with  $L=3$ .
- Number of iterations:  $N_{iter} = 3$ .
- Performance evaluation: Outage Probability vs  $l_{SR}$  and BLER vs  $SNR_{SD}$  (S  $\rightarrow$  D link signal-to-noise ratio per useful bit per receive antenna).
- References: Conventional hybrid-ARQ and conventional LLR-level packet combining.

# Generalized ARQ for Broadband Cooperative Communications

## Performance Evaluation (2/5)

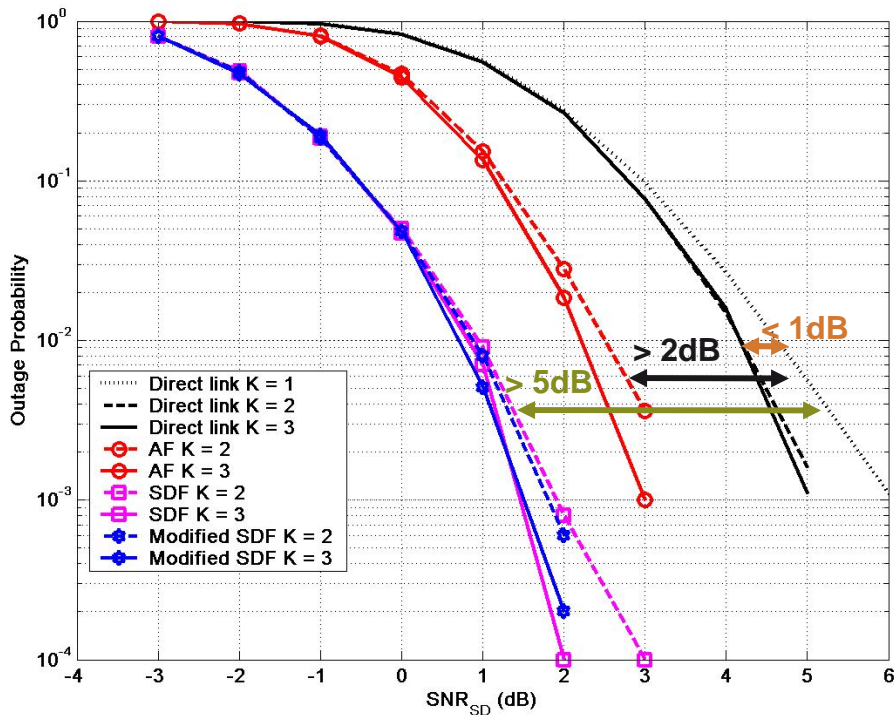
Outage Probability:  $M_S = M_R = M_D = 2$  and  $K = 2$



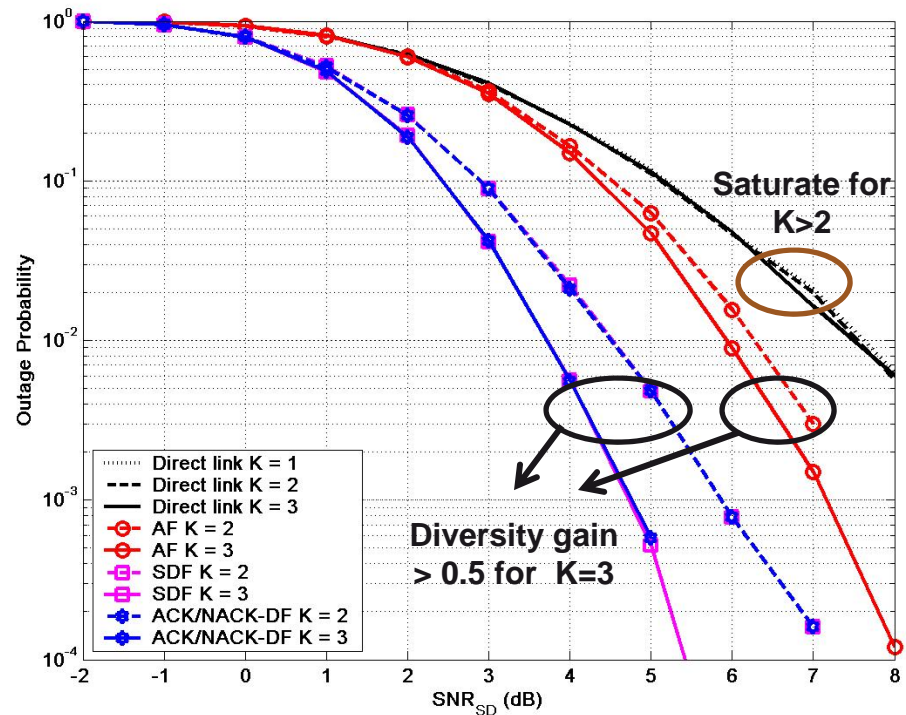
# Generalized ARQ for Broadband Cooperative Communications

## Performance Evaluation (3/5)

Outage Probability:  $I_{SR} = 0.5$



$$M_S = M_R = M_D = 2$$

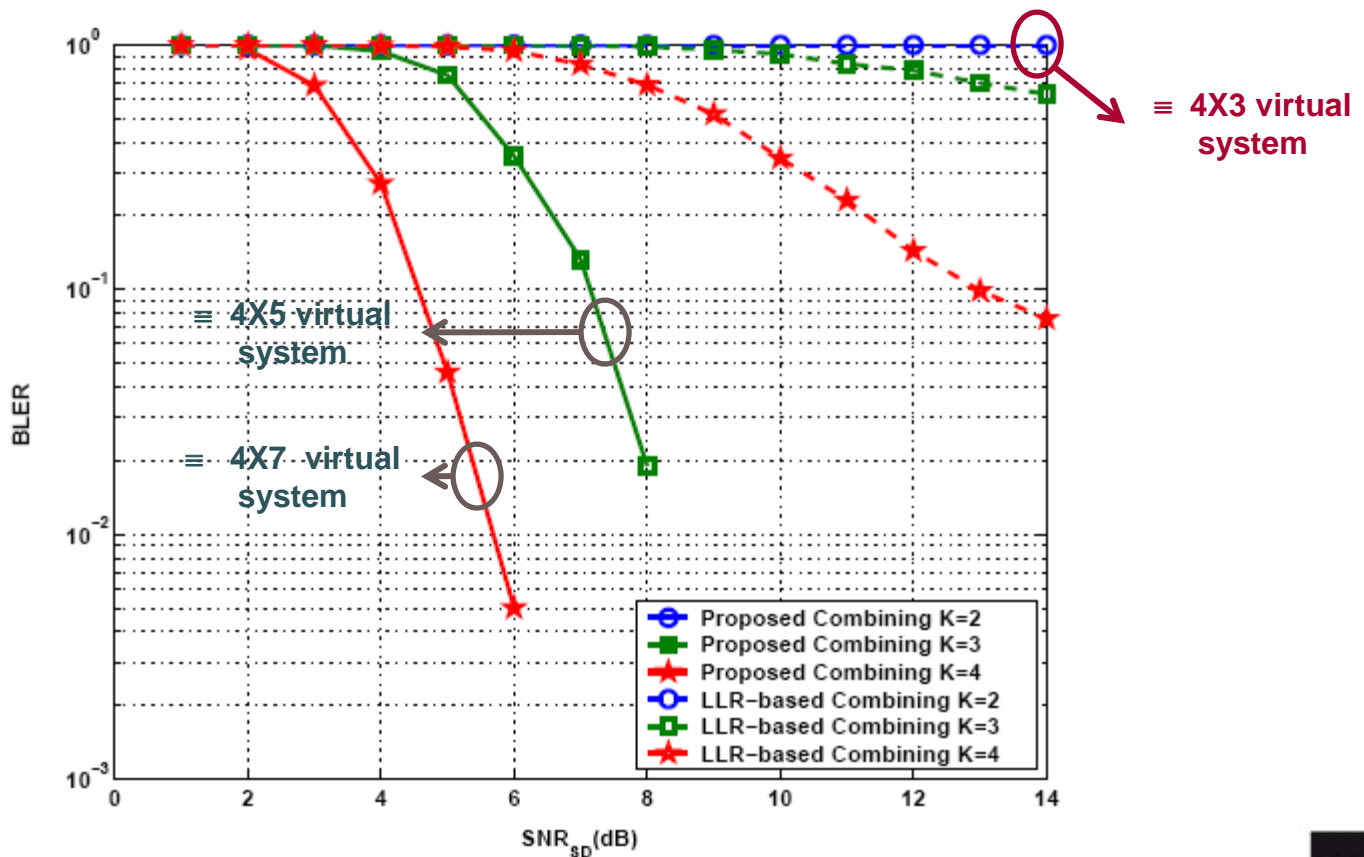


$$M_S = M_R = 2, M_D = 1$$

# Generalized ARQ for Broadband Cooperative Communications

## Performance Evaluation (5/5)

Modified Selective DF:  $M_S = 4$ ,  $M_R = 2$ ,  $M_D = 1$  and  $I_{SR} = 0.3$





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# Conclusions and Future Work

## Conclusions

- **New class of turbo packet combiners for broadband MIMO communications.**
- **Asymptotic Analysis of the CCI effect.**
- **Two efficient turbo receiver schemes for multi-antenna multi-code CDMA transmission with ARQ.**
- **An appropriate communication model to mask the cooperation in broadband multi-antenna cooperative systems.**





# Conclusions and Future Work

## Future research directions:

- Extension to uplink multi-user space division multiple access (SDMA) framework.
- Investigate the influence of imprecise CSI on the proposed turbo receiver.
- Hybrid AF/DF scheme under the framework of broadband multi-user.

# Related Publications (1/3)

## Book Chapter

- T. Ait-Idir, **H. Chafnaji**, S.Saoudi, and A. V. Vasilakos, “Advanced Hybrid-ARQ Receivers for Broadband MIMO Communications,” Chapter in “Radio Communications”, Alessandro Bazzi (Ed.), ISBN: 978-953-307-091-9, INTECH.

## Journal Articles

- T. Ait-Idir, **H. Chafnaji**, and S.Saoudi, “Turbo Packet Combining for Broadband Space-Time BICM Hybrid-ARQ Systems with Co-Channel Interference,” *IEEE Transactions on Wireless Communications*, vol. 9, no. 5, pp. 1686-1697, May 2010.
- **H. Chafnaji**, T. Ait-Idir, S.Saoudi, and A. V. Vasilakos, “Frequency Domain Hybrid-ARQ Chase Combining for Broadband MIMO CDMA Systems,” To be submitted to *EURASIP Journal on Wireless Communications and Networking*.
- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, “Relaying Schemes and Joint Turbo Processing for Spatial Multiplexing over Broadband MIMO Channels,” To be submitted to *IEEE Transactions on Wireless Communications*.

## Related Publications (2/3)

### Conference papers (12 accepted)

- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "Signal-level turbo packet combining for multi-rate relay-assisted systems over multi-antenna broadband channels," Accepted to *IEEE GLOBECOM 2010*, Miami, Florida, USA , 6-10 December 2010.
- **H. Chafnaji**, T.Ait-Idir, and S. Saoudi, "A comparative study of frequency domain HARQ Chase combining schemes for broadband single carrier MIMO CDMA systems," Accepted to *IEEE GLOBECOM 2010*, Miami, Florida, USA , 6 December 2010.
- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "Analysis of Packet Combining for Single Carrier Multi-Relay Broadband Systems," *IEEE SPAWC 2010*, Marrakech, Morocco, Jun. 2010.
- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "Turbo Packet Combining Techniques for Multi-Relay-Assisted Systems over Multi-Antenna Broadband Channels," *ACM IWCMC 2010*, Caen, France, Jun. 2010.
- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "On the Design of Turbo Packet Combining Schemes for Relay-Assisted Systems over Multi-Antenna Broadband Channels," *IEEE 71st Semi-Annual VTC10Spring, Taipei, Taiwan*, May 2010.
- T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Frequency Domain Hybrid-ARQ Chase Combining for Broadband MIMO Communication with Co-Channel Interference," *IEEE GLOBECOM 2009*, Honolulu, Hawaii, Nov-Dec. 2009.

# Related Publications (3/3)

## Conference papers

- T. Ait-Idir, **H. Chafnaji**, H. Yanikomeroglu, and S. Saoudi, "Turbo Packet Combining for Broadband MIMO Relay Communication," *9th IEEE Mediterranean Microwave Symposium, MMS 2009*, Tangiers, Morocco, Nov. 2009. (Invited Paper).
- **H. Chafnaji**, T.Ait-Idir, H. Yanikomeroglu, and S. Saoudi, "Joint Turbo Equalization for Relaying Schemes over Frequency-Selective Fading Channels," *ACM IWCMC 2009*, Leipzig, Germany, Jun. 2009.
- **H. Chafnaji**, T.Ait-Idir, and S. Saoudi, "Packet Combining and Chip Level Frequency Domain Turbo Equalization for Multi-Code Transmission over Multi-Antenna Broadband Channel," *19th Annual IEEE Symposium PIMRC 2008*, Cannes, France, Sep. 2008.
- **H. Chafnaji**, T.Ait-Idir, and S. Saoudi, "Implementation and Complexity evaluation of Packet Combining for Multi-Code Transmission over Multi-Antenna Broadband Channel," *IEEE IWCMC 2008*, Crete Island, Greece, Aug. 2008.
- T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Frequency Domain Packet Combining with Integrated MMSE Block Turbo Equalization for Broadband MIMO Communications," *IS/VC 2008*, Bilbao, Spain, Jul. 2008 (Invited Paper).
- T. Ait-Idir, **H. Chafnaji**, and S. Saoudi, "Joint Hybrid ARQ and Iterative Space-Time Equalization for Coded Transmission over MIMO-ISI Channel," *IEEE WCNC 2008*, Las Vegas, NV, Mar-Apr. 2008.



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pour Obtenir le grade de

**DOCTEUR DE TELECOM BRETAGNE**

en habilitation conjointe avec l'Université  
de Bretagne Sud

