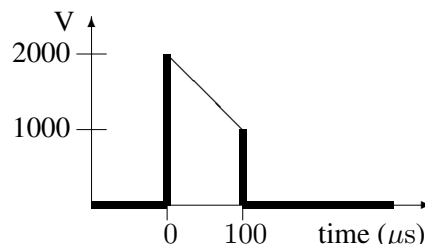


Background: Conducted Energy Weapons (CEWs), such as those manufactured by TASER International, are seeing increasing deployment in police forces as a less lethal force option; but, at the same time, these weapons are also seeing an increased level of concern in terms of their safety of use. These weapons send a sequence of electrical pulses into the subject, and are designed to stimulate nerves and cause muscular incapacitation. We consider a CEW which sends pulses of the shape below at a rate of 20 pulses/s.

In order to validate the reliability of these devices, they are tested by firing into a dummy load (normally a 600Ω resistor) and the voltage signal measured and digitized. A recent standard recommends a sampling frequency of 10 MSample/s. Instead, in this exam, consider an inadequately sampled signal using $f_s = 50$ kSample/s, used with a 6 bit A/D converter. The A/D converter's input range is $\pm 1500V$.

The electrical output from the weapon is a series of pulses, $x(t)$, described by the equation below and the graph at right.

$$x(t) = 2000 u(t)u(100\mu s - t)(1 - \frac{t}{200\mu s}) V$$



1. (1 point) Your exam is exam number **1**. Write down this number.
2. (5 points) The pulse, $x(t)$, is sampled at the indicated rate. **Sketch a stem plot of the sampled signal and write the sequence $x[n]$** , for $0\mu s \leq t \leq 100\mu s$.
3. (5 points) In order to calculate the net charge in a pulse, we use an integrating filter $y[n] = x[n] + y[n - 1]$. **Calculate and sketch $y[n]$ for $n = 0 \dots 5$.**
4. (5 points) Briefly indicate whether the filter in Q3 is: a) linear, b) memoryless, c) shift-invariant, d) LSI, e) stable, f) causal, g) FIR.
5. (5 points) In Q2, we considered the case in which the sampling was aligned with the pulse timing. If the sampling and pulse are offset in time, the peak output will appear to be lower. **What pulse offset, in t , results in the minimum peak in $x[n]$? Sketch a stem plot of the sampled signal in this case?**
6. (5 points) **Is there aliasing in signal $x[n]$?** Briefly (≤ 30 words) indicate the relationship between the lower peak measurement and an aliased signal. *Note: you do not need to prove it mathematically for this question, an explanation is sufficient.*
7. (5 points) **What is the resolution of the digitized signal, $x_s[n]$?**
8. (5 points) Calculate the sampled sequence $x_s[n]$, for $0\mu s \leq t \leq 100\mu s$?
9. (5 points) To detect the pulse arrival time, the FIR filter $h[n] = \{-1, 1\}$ is useful to amplify edges in the signal. **Calculate the DTFT, $H(\omega)$, of this filter.**
10. (5 points) To detect the pulse arrival time, the FIR filter $h[n] = \{-1, 1\}$ is useful to amplify edges in the signal. **Using with $N = 4$, calculate $H[0]$ and $H[1]$. What does $H[0]$ represent?**
11. (5 points) Consider the first four samples of $x[n] = \{2000, 1900, 1800, 1700\}$. **What is $y[n] = x[n] * h[n]$?**
12. (10 points) Consider the first four samples of $x[n] = \{2000, 1900, 1800, 1700\}$. **Calculate the circular convolution $y[n] = x[n] \circledast h[n]$ by calculating $H[k]$ and $X[k]$.**
13. (5 points) We wish to filter $x[n]$ by $h[n]$ using $N = 4$ using the overlap add. **Calculate the maximum block size of $x[n]$. Sketch a diagram of the filter using overlap-add.** Indicate each operation and the sizes of the sequences involved.
14. (5 points) (bonus?) Such a sequence of pulses can be generated by a recursive linear filter in response to a trigger. **Sketch a filter which outputs an infinite train of pulses in response to an input $x[n] = \delta[n]$.**