Cooperative Connectivity Models for Wireless Relay Networks

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Abstract: This paper considers the ways that cooperating terminals can be connected to each other in wireless relay networks and the constraints imposed by the availability of different system resources. A framework is developed that exposes the relationship between constraints on available system resources and the achievable combinations of communication links between cooperating terminals. Cooperative connectivity models defined by the achievable combinations of links are derived, associated with their minimum cost constraint sets, and mapped to diversity techniques presented in the literature. The constraints considered are the available number of orthogonal relaying channels, the ability of terminals to diversity combine signals on a single common channel, the ability of terminals to diversity combine signals on orthogonal channels, the ability of terminals to transmit signals on multiple orthogonal channels, and the ability of terminals to cancel the effects of interhop interference.

1 Introduction

Recent findings in the literature have shown that the performance of wireless relay networks can be improved through the application of distributed spatial diversity techniques that leverage cooperation between wireless terminals. Multi-user diversity [3] and virtual antenna arrays [15] achieve spatial diversity by relaying the signal along multiple routes in parallel. Multihop diversity [8], [9] achieves spatial diversity from the reception of signals that have been transmitted by multiple relays in serial along a single multihop route. Cooperative diversity [39], [40], [42], [61] achieves spatial diversity by sharing information between the source terminal and relay terminals such that each user of the group sends information to the destination using all of the terminals. Coded cooperative diversity [30], [31], [41], [45], [64], [76] uses various coding techniques, including space-time coding [1], to improve the performance over that of basic repetition coding. Various techniques based on the artificial generation of a rich multi-path fading environment [19], [23], [48], [55], [59], [62], [63], [68] can be leveraged to reclaim some of the spectral efficiency loss caused by repetition coding over orthogonal relaying channels. Information theoretic results for the classical relay channel [14] have been extended to include more general multi-hop relay channels [21], [38]. Results characterizing the diversity-multiplexing tradeoff of multiple-antenna [77] and multiple-access [65] channels have been extended to half-duplex cooperative channels [4]. Basic strategies for cooperation between wireless terminals have been extended to include cascaded [22], [28], [58], multihop multi-branch [57], and general [10] cooperation strategies. These distributed spatial diversity techniques contrast with non-distributed techniques such as classical MIMO transmission that require individual terminals to host multiple antennas.

Each of the distributed spatial diversity techniques proposed in the literature places different requirements on the wireless terminal hardware capabilities, channel availability, and multiple access schemes used to implement mesh connectivity between terminals, and thus places different requirements on the system resources that must be available. Therefore, system resource constraints that limit the ways that terminals can be connected to each other also constrain the distributed spatial diversity techniques that can be applied. Additionally, the cooperation between terminals needed to support each

technique can often be achieved with different combinations of system resources. Instead of generating results for one specific assumed set of available system resources, this paper explicitly specifies the system resources that must be available for terminals to be connected to each other in different ways, and therefore to utilize different distributed spatial diversity techniques.

This paper develops a framework for modeling the ways that terminals can be connected to each other in wireless relay networks and the relationship between constraints on the available system resources and achievable cooperative connectivity. The cooperative connectivity of a wireless relay network is defined as the set of communication links between pairs of terminals that are used in the transmission of an information signal from a source terminal to a destination terminal. Relay terminals are defined to cooperate with the source terminal when they transmit a signal that helps the destination terminal to successfully decode the original information signal. The system resource constraints considered in this paper are the available number of orthogonal relaying channels, the ability of relays and destinations to diversity combine incident signals on a single common channel, the ability of relays and destinations to diversity combine incident signals on different orthogonal channels, the ability of transmitters to transmit signals on multiple orthogonal channels, and the ability of receivers to cancel the effects of interhop interference [9]. Generally, it is of significant relevance to understand the different ways that cooperating terminals can be connected to each other in wireless relay networks, which of those options for cooperative connectivity show the most promise for further investigation and eventual adoption, and which system resources can enable those options for cooperative connectivity in the most efficient manner. The developed framework is a valuable first step in the analysis of these issues, and enables the formulation of interesting and relevant, but previous unexpressed, questions with respect to cooperative connectivity.

For example, the framework allows use to formulate and solve the following classes of problems: 1) given an available set of system resources, determine the achievable cooperative connectivity, 2) given a desired level of cooperative connectivity, determine the possible (and lowest cost) sets of system resources that can be used to achieve it, 3) given a baseline set of system resources and level of

cooperative connectivity, determine the impact on the achievable cooperative connectivity of incrementally adding or removing different system resources, and 4) given a baseline set of system resources and level of cooperative connectivity, determine the possible (and lowest cost) sets of system resources that can be incrementally added or removed to achieve different levels of cooperative connectivity. The first problem class and its inverse, the second problem class, consider the core relationship between system resources and achievable cooperative connectivity. The third problem class and its inverse, the fourth problem class, consider the value of reusing existing capabilities of the network infrastructure as incremental modifications are made. Each of the different system resources has an associated cost, so it is important that existing investment is leveraged when modifications are made to network infrastructure. These problem classes do not inherent express the philosophy that more connectivity is better, but are simply concerned with the relationship between achievable cooperative connectivity and available system resources. Even so, in the context of a given source-destination terminal pair when the system resources used are constant, it is clear that more cooperative diversity will result in better performance. However, this is not necessarily the case when considered in the context of a system with many source-destination terminal pairs, where many other factors such as spatial reuse and inter-user interference must be considered.

Although the focus of this paper is on uncoded systems, the developed framework is equally applicable to systems that employ traditional source and channel coding techniques. These coding techniques can be employed regardless of the ways that cooperating terminals can be connected to each other. However, the choice of coding technique should depend on the composite characteristics of the multihop relay channel formed by a given set of cooperating terminals and communication links between them. For cooperative coding techniques, such as those presented in [30], [31], [41], [45], [64], [76], where different relays generate different re-encoded versions of the original transmitted information signal, there are strong requirements on the ways that cooperating terminals can be connected to each other. For example, the distributed space-time code protocol of [41] requires that all relays be directly connected to both the source and destination in parallel. General analysis of the

cooperative connectivity requirements for different cooperative coding techniques is outside the scope of this paper. However, the framework can be used to determine the possible sets of system resources that can be used to achieve the required cooperative connectivity of a given technique.

The developed framework does not address the relationship between cooperative connectivity and spatial reuse of channels, a mechanism that can be applied in wireless relay networks to improve the overall spectral efficiency. Spatial reuse of channels occurs when different signals can be transmitted concurrently on the same channels in spatially separated portions of multihop paths (or networks). However, spatial reuse is less feasible in systems where terminals are connected by long direct communication links that do not allow spatial partitioning of the network, especially when using a multiple access scheme that does not allow spatial overlap of concurrent transmissions on the same channel. Systems with higher levels of cooperative connectivity, which generally have more long direct communication links and enjoy higher levels of spatial diversity, are generally less able to leverage spatial reuse due to a corresponding larger region of interference. This tradeoff between improved spatial diversity and improved spatial reuse is an important topic for further analysis.

The organization of the remainder of the paper is as follows. Section 2 describes the considered system resource constraints in detail. Section 3 analyzes the possible combinations of system resource constraints and derives cooperative connectivity models defined by the achievable combinations of communication links between cooperating wireless terminals. Section 4 derives the sets of constraints that result in the different cooperative connectivity models while minimizing the system cost (minimum cost constraint sets) and presents cooperative connectivity model transition diagrams following these minimum cost constraint sets. Section 5 describes the mapping of the cooperative connectivity models to various distributed spatial diversity techniques presented in the literature in order to highlight the general richness of the problem domain. Section 6 provides some concluding remarks.

2   System Resource Constraints

The considered system resource constraints are described in detail in this section. Options for each constraint are introduced, along with their corresponding relative system cost and connectivity impact.

In all cases, constraint options with lower cost have higher connectivity impact. Connectivity impact is defined as the reduction in achievable cooperative connectivity caused by absence of a system resource, and is measured in comparison to a fully connected (complete) relay network with links between all terminals. The term 'preceding terminal' denotes any terminal that is earlier along the multihop transmission path than the candidate terminal. The term 'following terminal' denotes any terminal that is later along the multihop transmission path than the candidate terminal.

2.1   Number of Channels Available

This constraint defines the number of orthogonal relaying channels available for each source-destination pair. The half-duplex nature of wireless terminal hardware requires that each relay transmit and receive with different channels, implying a minimum of two orthogonal channels. When the modulation scheme, total power, and rate are kept constant, use of more than two orthogonal channels for relaying increases the system cost since more bandwidth is necessary to achieve a given rate of transmission for each source-destination pair. However, when the symbol rate loss due to subdivision of the original bandwidth can be compensated for by an improved end-to-end SNR, the requirement for additional orthogonal channels may not necessarily result in an increase in overall required bandwidth.

- *N Channels Available (NCA):* The source and relays transmit using N orthogonal channels, where N+1 is the number of terminals. There is no connectivity impact.

- *K Channels Available (KCA):* The source and all relays transmit using K orthogonal channels, where $2 < K < N$. The connectivity impact is that each terminal may only be connected to preceding terminals that transmit on a different subset of channels (K-1 possible channels for relays and K possible channels for destinations).

- *2 Channels Available (2CA):* The source and all relays transmit using 2 orthogonal channels. The connectivity impact is that each terminal may only be connected to preceding terminals that transmit on a different subset of channels (1 possible channel for relays and 2 possible channels for destinations).

2.2 Common Channel Combination

This constraint defines the ability of terminals to diversity combine incident signals from multiple preceding terminals on a single common channel. Common channel combination can be achieved using various techniques including space-time coding, random relay phase rotation, and artificial multi-path generation with adaptive equalization, spatial processing, or RAKE reception [19], [23], [48], [55], [59], [62], [63], [68]. One interesting result of many of these references is that diversity combination can be achieved even without the use of orthogonal channels, although in many cases, depending on the specific channel conditions, there may be some degradation of performance in comparison to that of maximal ratio combining. Use of common channel combination increases the system cost since more advanced common channel processing and combination hardware is required at cooperating terminals.

- *Relay Common Channel Combination (RCC):* Relays are able to perform common channel combination. There is no connectivity impact.

- *No Relay Common Channel Combination (NRCC):* Relays are not able to perform common channel combination. The connectivity impact is that each relay may only be connected to one preceding terminal on each channel.

- *Destination Common Channel Combination (DCC):* Destinations are able to perform common channel combination. There is no connectivity impact.

- *No Destination Common Channel Combination (NDCC):* Destinations are not able to perform common channel combination. The connectivity impact is that each destination may only be connected to one preceding terminal on each channel.

2.3 Orthogonal Channel Combination

This constraint defines the ability of terminals to diversity combine incident signals from multiple preceding terminals on different orthogonal channels. Orthogonal channel combination can be achieved using classical combination techniques and possibly buffering of multiple orthogonal channels. Use of orthogonal channel combination increases the system cost since classical combination hardware is required at cooperating terminals.

- *Relay Orthogonal Channel Combination (ROC): Relays* are able to perform orthogonal channel combination. There is no connectivity impact.

- *No Relay Orthogonal Channel Combination (NROC):* Relays are not able to perform orthogonal channel combination. The connectivity impact is that each relay may only be connected to the subset of preceding terminals that transmit on one common channel.

- *Destination Orthogonal Channel Combination (DOC):* Destinations are able to perform orthogonal channel combination. There is no connectivity impact.

- *No Destination Orthogonal Channel Combination (NDOC):* Destinations are not able to perform orthogonal channel combination. The connectivity impact is that each destination may only be connected to the subset of preceding terminals that transmit on one common channel.

2.4   Multiple Channel Transmission

This constraint defines the ability of terminals to transmit a given signal on multiple orthogonal channels. Use of multiple channel transmission increases the system cost since more complex channel transmission hardware may be required at cooperating terminals (for example, transmitting concurrently at multiple frequencies) and each terminal that transmits on multiple channels generates additional energy and interference (when the modulation scheme and rate are kept constant).

- *Multiple Channel Transmission (MCT):* Terminals are able to transmit on multiple orthogonal channels. There is no connectivity impact.

- *No Multiple Channel Transmission (NMCT):* Terminals are not able to transmit on multiple orthogonal channels. The connectivity impact is that each terminal may only be connected to the subset of following terminals that receive on one common channel.

2.5   Interhop Interference Cancellation

This constraint defines the ability of receivers to cancel the effects of interhop interference created by the retransmission of signals on the same channel at different hops along a multihop transmission path. Interhop interference is a special case of intersymbol interference (ISI) that affects wireless relay networks where channels are reused [9], and therefore in theory it is expected that practical mitigation

techniques will be based on those used for ISI, including traditional equalization techniques. Use of interhop interference cancellation increases the system cost since more complex equalization (mitigation) hardware is required at cooperating terminals. Note that the analysis of this constraint is somewhat simplistic. First, it does not consider that in practice channel reuse may be possible without interhop interference cancellation in some circumstances due to sufficient spatial separation or attenuation between terminals. Second, it is assumed that interference cancellation is perfect when channels are reused at different hops within a single multihop path. Although this is not feasible in practice, even partial interference cancellation allows the same level of cooperative connectivity to be achieved, therefore resulting in the same cooperative connectivity models.

- *Interhop Interference Cancellation (IIC):* Terminals are able to cancel interhop interference. There is no connectivity impact.

- *No Interhop Interference Cancellation (NIIC):* Terminals are not able to cancel interhop interference. The connectivity impact is that networks with K channels available have a maximum of K hops in the longest multihop path of the network, since it is not possible to reuse channels within a single multihop path.

3   Cooperative Connectivity Models

A set of resultant cooperative connectivity models can be derived from the possible system resource constraint combinations. The cooperative connectivity models are fully characterized according to three parameters: the achievable connectivity of the relays, the achievable connectivity of the destination, and the maximum achievable length of the longest multihop path of the network. The cooperative connectivity models can therefore be identified using the form 'xRyDzH', where 'xR' indicates the achievable connectivity of the relays, 'yD' indicates the achievable connectivity of the destination, and 'zH' indicates the maximum achievable length of the longest multihop path of the network. Fig. 1 describes the possible values of x, y, and z used when characterizing the achievable cooperative connectivity of the models and shows graphical examples of the cooperative connectivity terminology, with transmitting channel allocations indicated in brackets. Note that other channel allocations are

possible that achieve the same connectivity. The relationship between this parameterization and the maximum achievable diversity order of the network is not simple, although higher levels of achievable relay and especially achievable destination connectivity definitely do correspond to an increase in maximum achievable diversity order. It is shown in [12] that the maximum achievable diversity order of wireless relay networks is constrained by either the terminal or cut set with the minimum number of incident inter-terminal links, depending on the class of relaying method.

The cooperative connectivity equations presented in Table 1 specify the relationship between the system resource constraints and the characterizing parameters of the cooperative connectivity models. These equations address the first problem class listed in the introduction: given an available set of system resources, determine the achievable cooperative connectivity. The complete set of achievable models is shown in Figs. 2-4, and discussed in more detail in the next section. The number of available channels (NCA, KCA, and 2CA) has a structuring influence on the connectivity impact of the other constraints. The results are therefore presented classified by the number of available channels in order to avoid complex and monolithic cooperative connectivity and minimum cost constraint set equations.

The cooperative connectivity models derived when there are K channels available (Fig. 2) are the most general set. The cooperative connectivity models derived when there are 2 channels available (Fig. 3) are a subset of the models derived when there are K channels available, with the reduction resulting from additional system resource constraints and intersection between models. The majority of cooperative connectivity models result from constraint combinations with less than N channels available (Fig. 4). Only the models with full relay connectivity, FR1DFH and FRFDFH, are exclusive to constraint combinations with N channels available. This means that full cooperative connectivity is only achievable when N orthogonal channels are available, implying that the FRFDFH model will be very expensive to implement in practice for even a moderate number of relay terminals.

4   Minimum Cost Constraint Sets

The sets of constraints that result in the different cooperative connectivity models while minimizing the system cost (the minimum cost constraint sets) are derived in this section. These minimum cost

constraint sets are important in that they indicate the optimal ways to implement the different cooperative connectivity models. The minimum cost constraints sets assume the following ordering, with increasing system cost, of the system resource constraints: DOC, DCC, ROC, IIC, RCC, MCT, KCA, and NCA. It is assumed that constraints involving additional power, interference, or channels within the network itself have a greater system cost than constraints involving more complex terminals. This is based on the underlying assumption that the cost of hardware complexity generally decreases with time while the cost of bandwidth is fixed [47]. It is further assumed that constraints involving more complex relays terminals have a greater system cost than constraints involving more complex destination terminals because in general they affect more terminals in a multihop transmission path. It is important to note that a different ordering of system resource constraints with respect to increasing system cost would result in different minimum cost constraint sets for some of the cooperative connectivity models.

The minimum cost constraint set equations presented in Table 1 specify the relationship between the characterizing parameters of the cooperative connectivity models and the presence of each system resource in the minimum cost constraint set. Together with the previously presented cooperative connectivity equations, these equations address the second problem class listed in the introduction: given a desired level of cooperative connectivity, determine the possible (and lowest cost) sets of system resources that can be used to achieve it. Note that when a particular system resource is never present for a given number of channels available it does not imply that the corresponding system resource does not have any impact, only that the same cooperative connectivity can be achieved using an alternative set of system resources with lower system cost.

Figs. 2-4 respectively show the transitions between the different cooperative connectivity models for constraint changes following the minimum cost constraint sets when there are K, 2, and N channels available. These transition diagrams show the paths of increasing cooperative connectivity that can be followed without wasting any system resources, which would occur if a particular allocated system resource does not contribute to improving the cooperative connectivity. Increasing cooperative

connectivity refers to the fact that as more system resources are available it is possible to add more active links between pairs of terminals. Each transition in the transition diagrams corresponds to the inclusion of an additional system resource and the possibility of adding more active links that rely on that system resource, therefore increasing the achievable cooperative connectivity. The boxes with 'KH/FH' represent two cooperative connectivity models with a different maximum length of the longest multihop path of the network. Transitions between 'KH' and 'FH' cooperative connectivity models correspond to the IIC system resource constraint being lifted. The boxes with only 'FH' indicate that the corresponding 'KH' cooperative connectivity model does not exist for the given number of available channels. Transitions are in the direction of decreased system resource constraints.

Transitions that decrease system resource constraints without improving the cooperative connectivity are not shown. For example, adding MCT when the cooperative connectivity model is 1R1DFH brings no benefit since the terminals are not able to diversity combine the new channels. Transitions that do not follow the minimum cost constraint sets are also not shown. For example, adding DOC when the cooperative connectivity model is 1RNDFH is not optimal since the resultant 1RFDFH cooperative connectivity model does not require MCT. Together with the previously presented cooperative connectivity and minimum cost constraint set equations, these transition diagrams address the third and fourth problem classes listed in the introduction.

5 Mapping to the Literature

This section summarizes the mapping of the cooperative connectivity models to various distributed spatial diversity techniques presented in the literature. The list of presented references is not intended to be comprehensive, but is generally representative of the current state of the literature at the time of writing. Table 2 shows this mapping, indicating the name of the distributed spatial diversity technique, the corresponding references, the corresponding cooperative connectivity model of the current framework, and the channel allocation assumed in the references. Those references with an indicated channel allocation of "N/A" present information theoretic results independent of channel allocation. This mapping highlights that although the literature published so far has only started to explore the many

possible cooperative connectivity models there is already a broad range of connectivity and channel allocation assumptions. It also illustrates the wide variation in terminology used in the literature. The developed framework allows us to compare the cooperative connectivity and system resource requirements of the proposed distributed spatial diversity techniques and analyze the efficiency, in comparison to the minimum cost constraint sets, of the available system resources assumed in the literature. Due to space constraints, we do not summarize herein the sets of available system resources actually assumed in the included references.

6 Conclusion

This paper develops a framework for modeling the ways that cooperating terminals can be connected to each other in wireless relay networks and the relationship between constraints on the available system resources and the achievable cooperative connectivity. Cooperative connectivity equations are derived that specify the relationship between system resource constraints and achievable cooperative connectivity. The resulting cooperative connectivity models defined by the achievable combinations of communication links between cooperating wireless terminals are associated with their minimum cost constraint sets and mapped to relevant diversity techniques presented in the literature. It is indicated that the literature published so far has only started to explore the many possible cooperative connectivity models and the richness of the problem domain. Finally, it is straightforward to see how this framework can provide value as an analysis tool, for example by leveraging it in a series of probability of outage or error simulations that compare the different cooperative connectivity models in order to isolate the performance impact of specific system resource constraints.

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# Channels Available	Cooperative Connectivity Equations	Minimum Cost Constraint Set Equations

K Channels Available	`xR:  if (NRCC & NROC) then x = 1`
	`      else if (NRCC & ROC) then x = K`
	`      else if (RCC & NROC & NMCT) then x = C`
	`      else if (RCC & (ROC | MCT)) then x = N`
	`yD:  if (NDCC & NDOC) then y = 1`
	`      else if (NDCC & DOC) then y = K`
	`      else if (DCC & NDOC & NMCT) then y = C`
	`      else if (DCC & (DOC | MCT)) then y = F`
	`zH:  if (IIC) then z = F`
	`      else if (NIIC) then z = K`
		RCC: `if (CR | NR) then RCC = TRUE`
		`      else if (1R | KR) then RCC = FALSE`
		DCC: `if (CD | FD) then DCC = TRUE`
		`      else if (1D | KD) then DCC = FALSE`
		ROC: `if (KR | NR) then ROC = TRUE`
		`      else if (1R | CR) then ROC = FALSE`
		DOC: `if (KD | FD) then DOC = TRUE`
		`      else if (1D | CD) then DOC = FALSE`
		MCT: `MCT = FALSE`
		IIC: `if (FH) then IIC = TRUE`
		`      else if (KH) then IIC = FALSE`

2 Channel Available	`xR:  if (NRCC | NIIC) then x = 1`
	`      else if (RCC & NMCT & IIC) then x = C`
	`      else if (RCC & MCT & IIC) then x = N`
	`yD:  if (NDCC & NDOC) then y = 1`
	`      else if (NDCC & DOC) then y = 2`
	`      else if (DCC & NDOC & NMCT) then y = C`
	`      else if (DCC & NDOC & MCT) then y = N`
	`      else if (DCC & DOC) then y = F`
	`zH:  if (IIC) then z = F`
	`      else if (NIIC) then z = 2`
		RCC: `if (CR | NR) then RCC = TRUE`
		`      else if (1R) then RCC = FALSE`
		DCC: `if (CD | ND | FD) then DCC = TRUE`
		`      else if (1D | 2D) then DCC = FALSE`
		ROC: `ROC = FALSE`
		DOC: `if (2D | FD) then DOC = TRUE`
		`      else if (1D | CD | ND) then DOC = FALSE`
		MCT: `if (NR | ND) then MCT = TRUE`
		`      else MCT = FALSE`
		IIC: `if (FH) then IIC = TRUE`
		`      else if (2H) then IIC = FALSE`

N Channels Available	`xR: if (ROC	(RCC & MCT)) then x = F` ` else x = 1` `yD: if (DOC	(DCC & MCT)) then y = F` ` else y = 1` `zH: z = F`	RCC: `RCC = FALSE` DCC: `DCC = FALSE` ROC: `if (FR) then ROC = TRUE` `      else if (1R) then ROC = FALSE` DOC: `if (FD) then DOC = TRUE` `      else if (1D) then DOC = FALSE` MCT: `MCT = FALSE` IIC: `IIC = FALSE`

Table 1. Mapping of Cooperative Connectivity Models to the Literature

Distributed Spatial Diversity Technique	References	Model	# Chnls
2-hop multihop without diversity	[9]	1R1D2H	2CA
Conventional 2-hop relaying	[28]	1R1D2H	2CA
Relayed transmission	[26],[72]	1R1D2H	2CA
Multihop without diversity	[9]	1R1DFH	2CA
Multi-hop cooperation	[57]	1R1DFH	NCA
Multihop relaying	[25],[34],[53]	1R1DFH	NCA
Wireless network O(√n)	[20]	1R1DFH	NCA
Multihop relaying	[35]	1R1DFH	N/A
2-hop multihop diversity	[8],[9]	1R2D2H	2CA
Coded cooperation	[30],[31],[32],[51]	1R2D2H	2CA
Cooperative coding	[45],[64]	1R2D2H	2CA
Cooperative diversity	[27],[39],[40],[42],[43]	1R2D2H	2CA
Cooperative protocols I, II, and III	[50]	1R2D2H	2CA
Cooperative space-time delay coding	[52]	1R2D2H	2CA
Cooperative superposition modulation	[44]	1R2D2H	2CA
Distributed turbo coded diversity	[76]	1R2D2H	2CA
Relayed block markov transmission	[13]	1R2D2H	2CA

MIMO relay channel	[67]	1R2D2H	N/A
Relay channel	[14]	1R2D2H	N/A
Multihop, multi-branch cooperation	[57]	1RKDKH	NCA
Non-interfering multi-path transmission	[55]	1RKDKH	NCA
2-hop MSE relaying	[36]	1RCD2H	2CA
Coherent cooperative transmission	[66]	1RCD2H	2CA
Interference relay network	[48]	1RCD2H	2CA
Linear relaying	[70]	1RCD2H	2CA
Parallel relays w space-time modulations	[29]	1RCD2H	2CA
User cooperation	[7],[37],[61]	1RCD2H	2CA
Virtual antenna array	[5]	1RCD2H	2CA
Parallel relay network	[60]	1RCD2H	N/A
Interfering multi-path transmission	[55]	1RCDKH	KCA
2-hop cooperative relaying	[23],[24]	1RFD2H	2CA
2-hop relay network	[69]	1RFD2H	2CA
Collaborative coding	[46]	1RFD2H	2CA
Distributed Alamouti system	[3]	1RFD2H	2CA
Distributed space-time coding	[33],[41],[49]	1RFD2H	2CA
Dynamic decoded and forward	[4]	1RFD2H	2CA
Network path selection diversity	[6]	1RFD2H	2CA
Non-orthogonal amplify and forward	[4]	1RFD2H	2CA
Relay assisted MIMO channel	[56]	1RFD2H	2CA
Single-stage cooperative relaying	[53]	1RFD2H	2CA
Cooperative network	[2]	1RFD2H	NCA
Multi-branch cooperation	[57]	1RFD2H	NCA
Multi-user spatial diversity	[17]	1RFD2H	NCA
Repetition-based cooperative diversity	[41]	1RFD2H	NCA
C(m) cooperative diversity where K=m+1	[58]	KRFDFH	NCA
Cascaded (K-1)-hop cooperative diversity	[28]	KRKDFH	KCA
Two-level leapfrog scheme with K=2	[22]	KRKDFH	KCA
Amplify-and-forward MIMO tunnel	[55]	CRKDKH	KCA
Distributed MIMO multihop system	[15]	CRCDKH	KCA
Multi-stage cooperative relaying	[53]	CRCDKH	KCA
Opportunistic large array	[59], [63]	CRCDKH	KCA
C(N-1) cooperative diversity where K=N	[58]	FRFDFH	NCA
Full cooperative relaying	[28]	FRFDFH	NCA
Multihop diversity	[8],[9]	FRFDFH	NCA
Relay network	[18]	FRFDFH	NCA
Cooperative wireless system	[73],[74]	FRFDFH	N/A
Decode / compress and forward	[38]	FRFDFH	N/A
Multiple level relay channel	[71]	FRFDFH	N/A
Wireless network O(n)	[21]	FRFDFH	N/A

Table 2. Mapping of Cooperative Connectivity Models to the Literature

Single Relay (1R): Each relay can be connected to one preceding terminal.

R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

Single Destination (1D): Each destination can be connected to one preceding terminal.

R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

K Channel Relay (KR): Each relay can be connected to one preceding terminal on each of the K-1 orthogonal channels that it does not transmit on.

R1(1) R4(1)
S(0) R3(0) D
R2(2) R5(2)
*Example for K=3

K Channel Destination (KD): Each destination can be connected to one preceding terminal on each of the K orthogonal channels that it does not transmit on.

R1(1) R4(1)
S(0) R3(0) D
R2(2) R5(2)
*Example for K=3

Common Channel Relay (CR): Each relay can be connected to the subset of preceding terminals that transmit on a single common channel.

R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

Common Channel Destination (CD): Each destination can be connected to the subset of preceding terminals that transmit on a single common channel.

R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

Non-Identical Relay (NR): Each relay can be connected to all preceding terminals that use a non-identical subset of channels from the relay itself.

R1(1) R4(0)
S(0,1) R3(1) D
R2(0) R5(1)

Non-Identical Destination (ND): Each destination can be connected to all preceding terminals that use a non-identical subset of channels from the destination itself.

R1(1) R4(0)
S(0,1) R3(1) D
R2(0) R5(1)

Full Relay (FR): Each relay can be connected to all preceding terminals.

R1(1) R4(4)
S(0) R3(3) D
R2(2) R5(5)

Full Destination (FD): Each destination can be connected to all preceding terminals.

R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

K Hop Network (KH): There are a maximum of K hops in the longest multihop path of the network, where K is the number of available channels.

R1 R4
S(0) R3 D
R2(1) R5(2)
*Example for K=3

Full Hop Network (FH): There are a maximum of N hops in the longest multihop path of the network, where N+1 is the number of cooperating terminals.
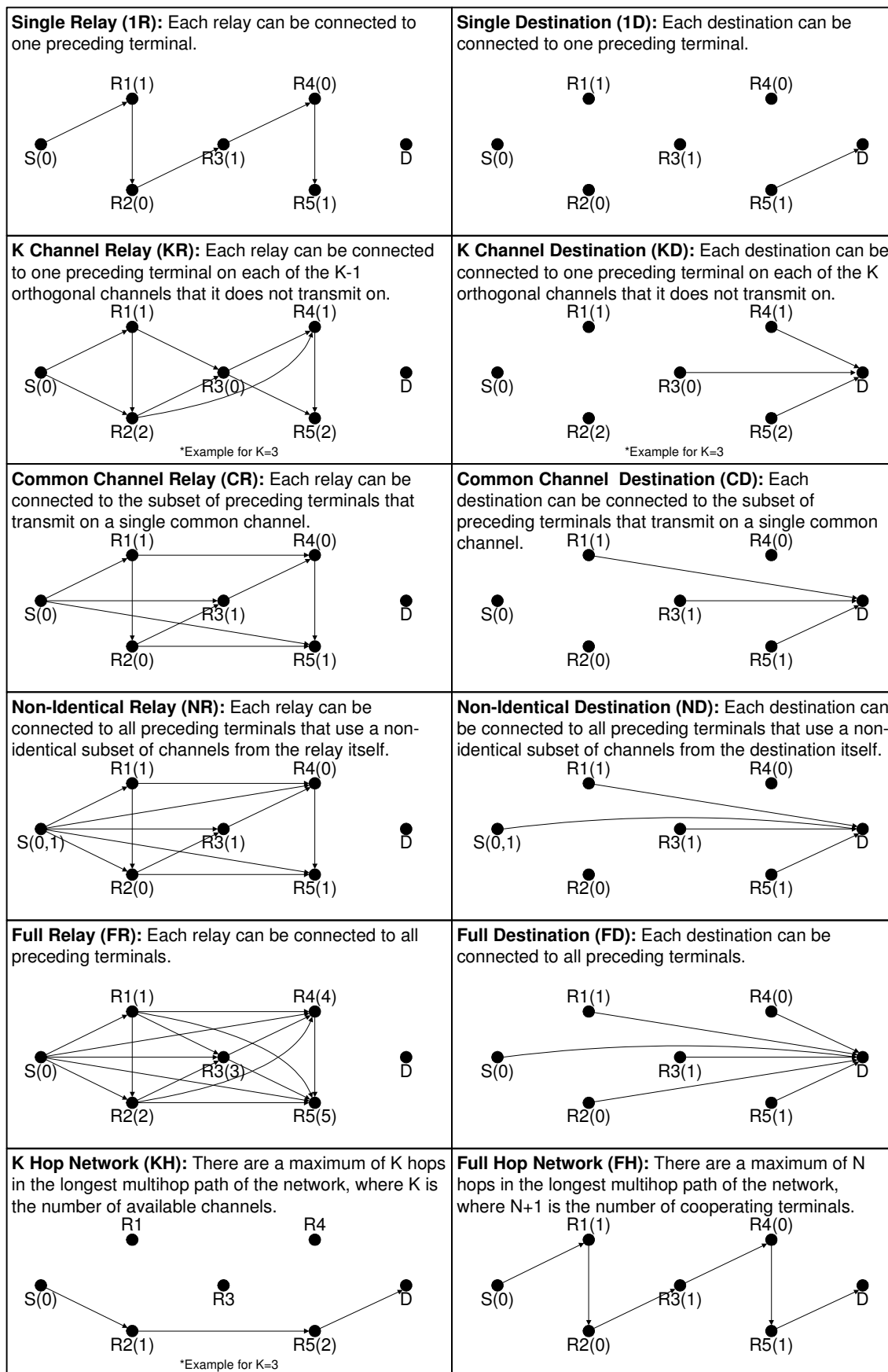
R1(1) R4(0)
S(0) R3(1) D
R2(0) R5(1)

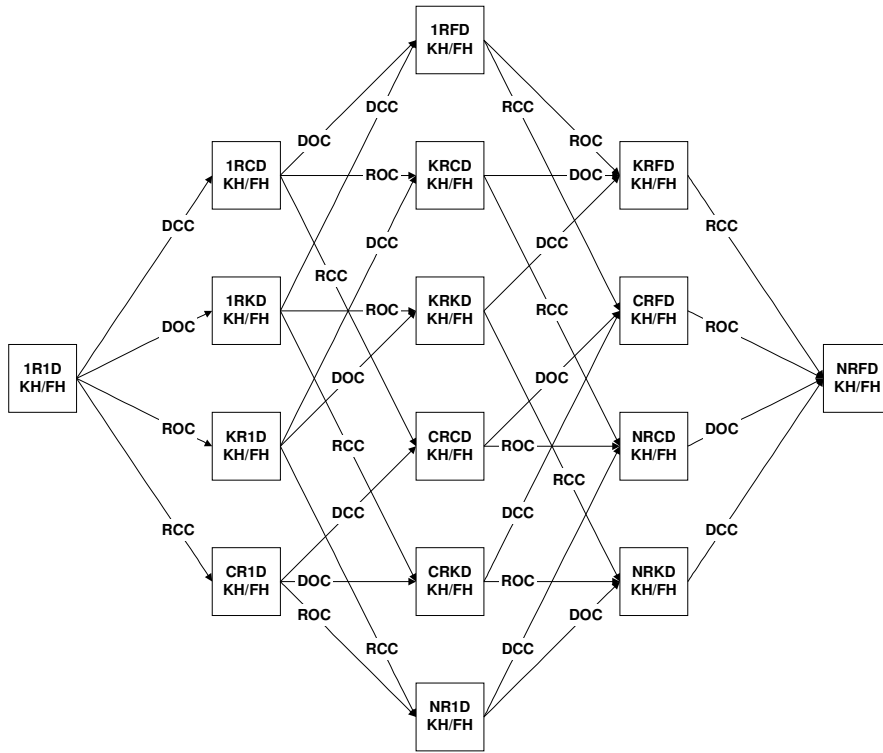Fig. 1. Cooperative Connectivity Model Terminology Examples

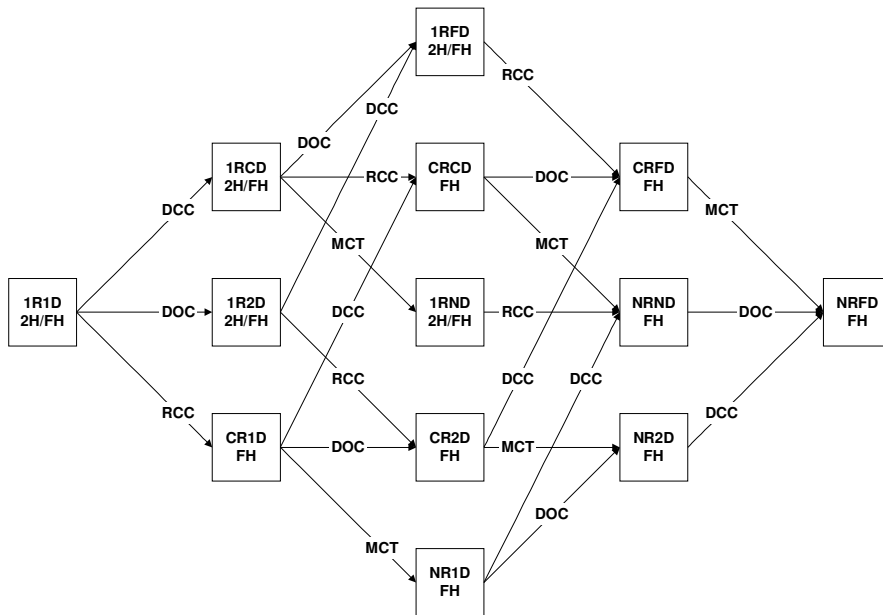Fig. 2. Cooperative Connectivity Model Transitions for KCA

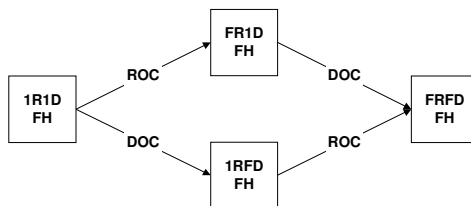Fig. 3. Cooperative Connectivity Model Transitions for 2CA

Fig. 4. Cooperative Connectivity Model Transitions for NCA