Spatial Heterogeneity of Users in Wireless Cellular Networks Based on Open Urban Maps

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Abstract—Wireless cellular network planning benefits from accurate and realistic, yet relatively simple and manageable, spatial traffic models. User locations in cellular networks are often modeled as homogeneous (uniform) Poisson point processes (PPPs). However, the real user distributions are seldom purely homogeneous. Network users are usually concentrated at social attractors such as residential and office buildings, shopping malls, and bus stations. Wireless spectral efficiency depends significantly on the users’ spatial heterogeneity, and thus relevant spatial traffic generators and models are important. In future (5G) networks, for which device-to-device (D2D), millimeter-wave (mmWave), and small-cell deployments in Heterogeneous Networks (HetNets), are promising technologies, it will become more important to have spatial traffic models which can represent the broad possibilities from completely homogeneous cases (e.g., a deterministic lattice) to extremely heterogeneous cases (e.g., highly clustered scenarios).

In this paper, we use maps of Paris, France, obtained from OpenStreetMaps, to study the spatial traffic heterogeneity of outdoor users in the denser areas of the city center. Specifically, we investigate a second-order statistic, the Coefficient of Variation (CoV), of two spatial metrics: the Voronoi cell area and the Delaunay cell edge length. The expected value of the CoV of these metrics allows us to study how the heterogeneity increases with the density of users. Moreover, we find that the statistical distribution of both metrics is close to Weibull. The results illustrate that the topology of the buildings in the city imposes a significant degree of heterogeneity on the spatial distribution of the wireless traffic.

Index Terms—Heterogeneous Spatial Traffic Distribution, Wireless Cellular Networks, Open Map Data.

I. INTRODUCTION

The enhancement and proliferation of wireless devices with advanced communication technology and excessive processing power drives exponential growth in the wireless traffic demand. To cope with this massive demand, network operators are forced to improve network performance and provide the required wireless capacity. The statistics of the signal-to-interference-plus-noise ratio (SINR) are key to the performance analysis of wireless cellular networks. The signal strengths and interference levels depend strongly on the network geometry, i.e., the relative positions of the transmitters and the receivers. Accordingly, in wireless cellular networks, the spatial statistics of the traffic demand, i.e., the user equipment (UE) distribution, as well as that of the service points, i.e., the base station (BS) distribution, have a direct impact on the network performance. Therefore, planning, design, and deployment of cost-effective and high-capacity wireless networks requires accurate and realistic, yet relatively simple and manageable, traffic models in both the time and space domain.

Traffic demand modeling in the time domain has been well-investigated in the literature [1, 2]. Traditionally, in voice-only networks, homogeneous Poisson process models were accurate enough to model traffic in time. After the emergence of different applications, such as video and data with variable data rate demands, the Poisson model failed to capture the traffic statistics [1]; as a result, various heterogeneous (super-Poisson) traffic models based on the hidden Markov model (HMM), Markov modulated Poisson process (MMPP) [2], and other stochastic methods have been proposed in the literature and used for performance analysis.

Similarly, in the space domain, a popular approach in modeling and analysis of the supply and demand in heterogeneous wireless cellular networks has been the use of two independent Poisson point processes (PPPs) for the locations of BSs and UEs [3–6]. This popular approach has a major shortcoming: although the PPP model may be a fitting one for the BS locations, it is less adequate for the UE locations, mainly due to the fact that the model is not adjustable (tunable) to represent the amount of heterogeneity (non-uniformity) in the UE locations. There is still relatively little literature that takes into account the heterogeneous spatial distribution of the traffic demand in wireless cellular networks [7–14].

Wireless spectral efficiency can be significantly affected by the UEs’ spatial heterogeneity [7, 8], and thus relevant spatial traffic generators and models are important. Future (5G) wireless networks will likely be based on technologies where this heterogeneity is likely to significantly affect performance. Device-to-device (D2D) communications, where UEs can communicate in direct links, are sensitive to the distances between neighbouring UEs [15], and neighbouring links may cause or suffer severe interference because of the short distances involved [16]. Communications at millimeter wave (mmWave) frequencies, which are proposed for 5G networks [17–20], are expected to be very sensitive to the shapes and layouts of buildings. For example, because of the low expected wave penetration though building walls [20], it makes sense to analyze indoor and outdoor environments.
separately; furthermore, since indoor UEs’ traffic may be off-loaded to Wi-Fi and femto-cells, the study of the distribution of the outdoor UEs becomes very interesting.

The main contribution of this paper is the study of the heterogeneity of the spatial distribution of outdoor users based on building data taken from the OpenStreetMap (OSM) project [21], using the city center of Paris, France, as an example. The authors in [9] note that it is generally difficult to obtain real-world location data of wireless devices; the freely-available building data from OSM provides a large source of urban maps that can give an approximation of the real spatial user distributions: the buildings impose a ‘thinning’ of the PPP (which results in inhomogeneity[9]), while the large amount of available map data ensure statistically significant results. The resulting point process is investigated via a second-order statistic, the Coefficient of Variation (CoV), of two scalar traffic metrics in the space domain: that of the ‘Voronoi cell area’ and that of the ‘Delaunay cell edge length’. We also capture the cumulative distribution function (CDF) of each of these two traffic metrics, and fit it to known distribution functions. A good understanding of the distribution type of these spatial traffic metrics can be valuable for designing traffic models which are tunable and realistic.

The remainder of this paper is organized as follows: In Section II, the methodology of the extraction and processing of the maps is described. The two scalar traffic metrics that are used to capture spatial traffic characteristics are introduced in Section III. In Section IV, the statistics of the traffic distribution based on the open map data are investigated and the results are presented. Section V concludes the paper.

II. MAP EXTRACTION AND PROCESSING

Maps of the city center of Paris, France are obtained from the OSM project [21], which is a volunteer project whose purpose is to recreate vector maps of the whole earth for open access. These maps contain, among others, the ‘footprints’ of the various buildings, i.e., the 2D polygons that describe the shape of the building as it stands on the ground. OSM data has previously been used for studying the wireless channel in a European historical urban center, but only for one specific city block [22]. In this study, we perform a statistical study of an entire historical city center cut up into smaller square tiles.

Central Paris has several interesting characteristics that make it a good choice for study, among which:

- It is an important urban center, with a large resident, business, and tourist populations, and therefore deserves to be studied for wireless system planning.
- Both its historical and current importance make it a city of great interest to the volunteer community: thus we can expect the building data to both reliable and complete, at least enough for statistical purposes.
- It is mostly topographically flat. The building heights are also quite regular, most measuring around 20m (7 floors).

The 2D representation of the city is thus sufficient for many purposes.

The data are extracted as follows:

Fig. 1. An example of a city area as visualized on the OSM website.

Fig. 2. The city tile from Fig. 1 after processing, showing indoor (colored) and outdoor (white) locations.
1) A master file containing the whole city is downloaded.
2) City tiles of size 1km × 1km are extracted from the master file. We consider an area of 10km × 8km, with consecutive tiles shifted 500m both horizontally and vertically (thus the same area may be considered up to 4 times): this results in 19 × 15 total tiles.
3) For each tile, the building shapes and types are extracted. Some unnecessary building types (e.g., bridges) are removed. The building node coordinates are converted from spherical earth coordinates to local rectangular coordinates, flattened at the center of the 1km × 1km tile (this results in a horizontal flattening error of the order of centimeters in each tile corner).
4) The building polygons are then merged into ‘islands’, of which the interiors (‘courtyards’) are filled (they are considered as indoor).
5) We only keep tiles that have a high building coverage. In this study, a tile is kept if its total ‘island’ coverage area is above 50 percent for the whole 1km × km tile, as well as over 40 percent for each of the four 500m × 500m corner sub-tiles. The purpose of this filtering is to focus our study on high-building-density areas, which are of most interest, and avoid areas that contain many parks, rivers, canals, and other areas of low building and user density. This results in 83 out of 285 tiles being kept.

An example city tile, visualized on the OSM website, and then processed by the algorithm above is shown in Figs 1 and 2, respectively.

III. SCALAR TRAFFIC METRICS AND STATISTICS

Given a set of points \( P = \{p_1, p_2, \ldots, p_n\} \) in two dimensional space \( \mathbb{R}^2 \), the Voronoi tessellation \( T = \{c_{p_1}, c_{p_2}, \ldots, c_{p_n}\} \) is the set of cells such that every location, \( y \in c_{p_i} \), is closer to \( p_i \) than any other point in \( P \). This can be expressed formally as

\[
c_{p_i} = \{y \in \mathbb{R}^2 : |y - p_i| \leq |y - p_j| \text{ for } i, j \in 1, \ldots, n\}.
\]

The Voronoi tessellation in \( \mathbb{R}^2 \) has the property that each of its vertices is given by the intersection of exactly three Voronoi cells. The corresponding three points define a Delaunay cell. So the two tessellations (Voronoi and Delaunay) are said to be dual. Figure 3 demonstrates a pattern of points with its Voronoi tessellation and Delaunay tessellations.

Various statistical quantities can now be considered for measuring a point pattern. The ‘Voronoi cell area’ \( (V) \) is the first natural choice. Various statistics of the Voronoi cells for a Poisson point process (Poisson-Voronoi Tessellation) are well investigated in the literature [23]. The second metric is the ‘Delaunay cell edge length’ \( (D) \), whose various statistics are investigated in [24].

In this paper, we use the CoV, which is the standard deviation normalized by the mean, of the traffic metrics \( V \) and \( D \) to capture the heterogeneity of spatial traffic. The advantage of CoV is that it is scalar showing the heterogeneity by only one scalar value. It is shown in [23] and [24] that the expected value of the CoV of \( V \) and \( D \) are, respectively, 0.530 and 0.492 for a homogeneous PPP. We therefore use the normalized metrics

\[
C_V = \frac{\sigma_V}{0.530 \mu_V}
\]

and

\[
C_D = \frac{\sigma_D}{0.492 \mu_D},
\]

such that \( \mathbb{E}(C_V) = \mathbb{E}(C_D) = 1 \) for a homogeneous PPP.

IV. TRAFFIC GENERATION AND SIMULATION RESULTS

On each of the 83 high building-density 1000m × 1000m maps obtained from the procedure described in Section II, we distribute points (network users) according to a homogeneous PPP with density \( \lambda \), and only keep the points which fall in outdoor locations. As a result, the density of points in all outdoor areas is constant across all the maps. Figure 4 illustrates users distributed in the outdoor areas of the map in Figure 2, and the resulting Voronoi tessellation. Figure 5 shows the CoV values of the Voronoi cell areas and the Delaunay cell edge lengths of the resulting spatial traffic patterns averaged over all 83 maps. We observe that low user densities have CoVs close to 1: the same as that of a homogeneous PPP, while high user densities result in increased CoVs, as the spatial heterogeneity becomes more pronounced.

For a more accurate view of the statistical distribution of points (network users), we investigate the fitness of the distributions of the measured traffic metrics with several known distribution functions, for \( \lambda = 1000 \) users per \( km^2 \) of outdoor area. Figures 6 and 7 show the CDFs and the fitness of different distributions for, respectively, the ‘Voronoi cell...
To evaluate the goodness-of-fit for the various distributions, we compare their log-likelihood (LL) measures [25] to the simulated data. Among all distribution functions, the Weibull distribution shows the highest fitness measure. Its CDF is given by:

$$1 - e^{-\frac{x}{\alpha}}$$

where, \( \alpha \) is the scale parameter, and \( k \) is the shape parameter.

The parameters of the Weibull distributions that best fit the simulated data, for both \( V \) and \( D \), are summarized in Table I. Traffic generation models can use this table to generate accurate traffic patterns which statistically follow the topology of the buildings in the city.

V. Conclusion

In this paper, we studied the spatial heterogeneity of network users as distributed on the outdoor areas of maps of dense
parts of central Paris, France; our approach can be reproduced on any major urban area for which building data is openly available. The availability of a large amount of maps ensures a large sample for statistical analysis.

We studied the CoV and the CDF of two spatial traffic metrics: the ‘Voronoi cell area’ and the ‘Delaunay cell edge length’, and showed a good fit. Fitted Weibull distribution parameters with relatively high shape values as well as the CoV values indicate that, even without considering population density information, the thinning induced by the layout of the buildings can lead to significant heterogeneity of the traffic in the space domain as the density of users increases.

This work can be extended in a number of directions. Adding information on population density and social attractors would increase the accuracy of the model, with an expected increase in the heterogeneity as well. Moreover, combining the spatial distribution with user rate demands in the time domain would also increase the overall heterogeneity, as well as the accuracy of the model.

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REFERENCES


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<th>Metric</th>
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<td>Voronoi cell area</td>
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<tr>
<td>Delaunay cell length</td>
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