

Reconsidering Performance of DEVS Modeling and Simulation Environments Using the DEVStone Benchmark

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Abstract

The Discrete Event System Specification formalism (DEVS), which supports hierarchical and modular model composition, has been widely used to understand, analyze and develop a variety of systems. DEVS has been implemented in various languages and platforms over the years. The DEVStone benchmark was conceived to generate a set of models with varied structure and behavior, and to automate the evaluation of the performance of DEVS-based simulators. However, DEVStone is still in a preliminar phase and more model analysis is required. In this paper, we revisit DEVStone introducing new equations to compute the number of events triggered. We also introduce a new benchmark, called HOMem, designed as an alternative version of HOmod, with similar CPU and memory requirements, but with an easier implementation and analytically more manageable. Finally, we compare both the performance and memory footprint of five different DEVS simulators in two different hardware platforms.

Keywords: DEVS, DEVStone, Synthetic Benchmarks, Performance, Memory Usage

1. Introduction

In the last four decades, various Modeling and Simulation (M&S) methodologies have provided excellent approaches to solve problems. Among them, one of the M&S techniques that has gained popularity is the Discrete Event System Specification (DEVS): a sound, formal definition, based on generic dynamic systems theoretical concepts, which supports efficient event based simulation, verification and validation [1] [2].

DEVS divides the system into basic models, called atomic models, and composite models called coupled models. Atomic models define the behavior of the system, whereas coupled models specify the structure. We can distinguish between classic DEVS and Parallel DEVS (PDEVS) [2]. In classic DEVS, when two or more models are scheduled for state transitions at the same time, one of the models is chosen according to

19 a *select* function provided in the coupled model specification. PDEVS is an extension of classic DEVS to
20 allow all imminent components to be activated and to send their output to other components. Removing the
21 *select* function and adding a new *confluent* transition function, PDEVS introduces the possibility to manage
22 simultaneous events in a natural manner.

23 DEVS has been successfully used for modeling a wide range of application domains. For example, it
24 has been used in urban traffic analysis [3], logistics and supply chain [4], computer architecture [5], [6],
25 embedded system designs [7], unmanned aerial vehicles [8], decision support systems [9], etc. Because of
26 the ease of model definition, model composition, reuse, and hierarchical coupling, DEVS has always been
27 successfully applied in such a variety of applications.

28 In contrast to time-stepped discrete time simulation, DEVS advances time through the concept of min-
29 imum time to next event, thereby advancing time asynchronously and achieving significant speedup over
30 the former method [2]. As a result, the DEVS formalism has been implemented in major object-oriented
31 programming languages, like Lisp, Scheme, C++, Java, Python, SmallTalk, leading to many DEVS sim-
32 ulation engines across the globe, like DEVSJAVA [10], DEVS-Suite [11], COSMOS [12], CD++ [13],
33 PyPDEVS [14], aDEVS [15], JAMES-II [16], DEVSim++ [17], xDEVS [18], to name but a few.

34 This variety of simulation engines has generated an extensive study in DEVS performance, commonly
35 focused on particular application domains. However, after several years of research, a final version of a
36 discrete event simulation benchmark was published, named DEVStone [19], [20], [21]. DEVStone can be
37 used to automatically generate a vast variety of models with different shapes and sizes. These models can
38 then be simulated to test different features with respect to the corresponding simulator.

39 These benchmarks incorporate several benefits but some of them suffer from shortcomings in their math-
40 ematical descriptions, like the formal computation of the total number of events triggered. In this paper, we
41 reconsider these benchmarks. Firstly, we include the computation of the total number of events triggered
42 inside each benchmark. Secondly, we fix some equations that in [21] did not give the exact number of
43 transitions, concretely equations (2), (3) and (4) in [21]. It is worthwhile to mention that these errors have
44 not affected the reliability of previous paper results, since these models have been always used to compare
45 wall-clock execution times. Finally, we define an additional benchmark, called HMem, that demands the
46 same computational effort than HMod, the more complex model in DEVStone, but is analytically more
47 manageable, as is demonstrated in the research work.

48 The remainder of this paper is organized as follows: we show a brief description of the DEVS formalism
49 and introduce several DEVS simulation engines in Section 2. The DEVStone benchmark is revisited in

50 Section 3, including all the contributions to the benchmark performed in this work. In Section 4 we describe
51 our experimental infrastructure and methodology. In Section 5 we present experimental results, including a
52 comparison of up to five simulators and more than 1400 DEVStone models. Finally, we present conclusions
53 in Section 6.

54 **2. DEVS: Formalism and Simulation Engines**

55 *2.1. The Discrete Event System Specification*

56 DEVS is a general formalism for discrete event system modeling based on set theory [2]. The DEVS
57 formalism provides the framework for information modeling which gives several advantages to analyze
58 and design complex systems: completeness, verifiability, extensibility, and maintainability. Once a system
59 is described in terms of the DEVS theory, it can be easily implemented using an existing computational
60 library. As stated in Section 1, the parallel DEVS (PDEVS) approach was introduced, after 15 years, as a
61 revision of Classic DEVS. Currently, PDEVS is the prevalent DEVS, implemented in many libraries. In the
62 following, unless it is explicitly noted, the use of DEVS implies PDEVS.

63 DEVS enables the representation of a system by three sets and five functions: input set (X), output set
64 (Y), state set (S), external transition function (δ_{ext}), internal transition function (δ_{int}), confluent function
65 (δ_{con}), output function (λ), and time advance function (ta).

66 DEVS models are of two types: atomic and coupled. Atomic models are directly expressed in the
67 DEVS formalism specified above. Atomic DEVS processes input events based on their model's current state
68 and condition, generates output events and transition to the next state. The coupled model is the aggrega-
69 tion/composition of two or more atomic and coupled models connected by explicit couplings. Particularly,
70 an atomic model is defined by the following equation:

$$A = \langle X, Y, S, \delta_{\text{ext}}, \delta_{\text{int}}, \delta_{\text{con}}, \lambda, ta \rangle \quad (1)$$

71 where:

- 72 • X is the set of inputs described in terms of pairs port-value: $\{p \in IPorts, v \in X_p\}$.
- 73 • Y is the set of outputs, also described in terms of pairs port-value: $\{p \in OPorts, v \in Y_p\}$.
- 74 • S is the set of sequential states.

- 75 • $\delta_{\text{ext}} : Q \times X^b \rightarrow S$ is the external transition function. It is automatically executed when an external
76 event arrives to one of the input ports, changing the current state if needed.
- 77 – $Q = (s, e) \mid s \in S, 0 \leq e \leq ta(s)$ is the total state set, where e is the time elapsed since the last
78 transition.
- 79 – X^b is the set of bags over elements in X .
- 80 • $\delta_{\text{int}} : S \rightarrow S$ is the internal transition function. It is executed right after the output (λ) function and is
81 used to change the state S .
- 82 • $\delta_{\text{con}} : Q \times X^b \rightarrow S$ is the confluent function, subject to $\delta_{\text{con}}(s, ta(s), \emptyset) = \delta_{\text{int}}(s)$. This transition
83 decides the next state in cases of collision between external and internal events, i.e., an external event
84 is received and elapsed time equals time-advance. Typically, $\delta_{\text{con}}(s, ta(s), x) = \delta_{\text{ext}}(\delta_{\text{int}}(s), 0, x)$.
- 85 • $\lambda : S \rightarrow Y^b$ is the output function. Y^b is the set of bags over elements in Y . When the time elapsed
86 since the last output function is equal to $ta(s)$, then λ is automatically executed.
- 87 • $ta(s) : S \rightarrow \mathfrak{R}_0^+ \cup \infty$ is the time advance function.

The formal definition of a coupled model is described as:

$$M = \langle X, Y, C, EIC, EOC, IC \rangle \quad (2)$$

88 where:

- 89 • X is the set of inputs described in terms of pairs port-value: $\{p \in IPorts, v \in X_p\}$.
- 90 • Y is the set of outputs, also described in terms of pairs port-value: $\{p \in OPorts, v \in Y_p\}$.
- 91 • C is a set of DEVS component models (atomic or coupled). Note that C makes this definition recursive.
- 92 • EIC is the external input coupling relation, from external inputs of M to component inputs of C .
- 93 • EOC is the external output coupling relation, from component outputs of C to external outputs of M .
- 94 • IC is the internal coupling relation, from component outputs of $c_i \in C$ to component outputs of $c_j \in C$,
95 provided that $i \neq j$.

96 Given the recursive definition of M , a coupled model can itself be a part of a component in a larger coupled
97 model system giving rise to a hierarchical DEVS model construction.

98 2.2. *DEVS Simulation Engines*

99 In the last decade, many DEVS M&S engines have come into existence. All of them offer a programmer-
100 friendly Application Programming Interface (API) to define new models using a high level language. How-
101 ever, only a few of them provide a user-friendly Graphical User Interface (GUI) for model specification. In
102 the following, we describe some of the most referenced DEVS M&S simulation frameworks:

103 2.2.1. *DEVSJAVA*

104 DEVSJAVA has been developed by Bernard P. Zeigler (University of Arizona, U.S.A.) and Hessem
105 Sarjoughian (Arizona State University, U.S.A.) [10]. It is written in Java and supports virtual time, real
106 time, and sequential and parallel execution. The definition of new models is performed through an API.
107 Several M&S tools have been defined around DEVSJAVA (GUIs for results visualization, GUIs for models
108 definition, etc.), as DEVSJAVA is one of the primary DEVS M&S reference simulators in the community.

109 2.2.2. *DEVS-Suite and COSMOS*

110 DEVS-Suite is a simulator built based on the Parallel DEVS formalism. This software provides a library
111 of examples proving some experimental concepts. It also incorporates simulation visualization techniques
112 consisting of displaying static structure of models, animation of models, and run-time viewing of time-based
113 trajectories [11]. CoSMoS (Component-Based System Modeling and Simulation) is a framework aimed at
114 integrated visual model development, model configuration and automatic data collection simulation [12].
115 The CoSMoS environment supports component-based modeling with direct support for DEVS formalism
116 and XML Schema. DEVS-Suite's core is largely DEVSJAVA. It is bundled within the CoSMoS distribution
117 and thus enables both modeling and simulation of Parallel DEVS models.

118 2.2.3. *CD++*

119 CD++ has been developed by Gabriel Wainer and his students (Carleton University, Canada; Universidad
120 de Buenos Aires, Argentina). Written in C++, it allows the definition of DEVS and Cell-DEVS models
121 graphically. These models are also defined using an API. CD++ supports virtual and real time, as well as
122 sequential, parallel and distributed simulations [13].

123 2.2.4. *PyPDEVS*

124 PythonPDEVS (a.k.a. PypDEVS) implements both Classic and Parallel DEVS in the Python language,
125 with a matching simulator [14]. Models are defined through the provided API, allowing the execution of

126 virtual time or real time simulations. The latest release of PyPDEVS is focused on improving the perfor-
127 mance, mainly because Python is an interpreted language. To this end, several schedulers have been defined,
128 obtaining good performance metrics.

129 2.2.5. *aDEVS*

130 ADEVS (A Discrete Event System simulator) is a C++ library for constructing discrete event simu-
131 lations based on the Parallel DEVS and Dynamic DEVS (dynDEVS) formalisms [15]. Developed by Jim
132 Nutaro, it allows the implementation of both sequential and parallel simulations using the provided C++
133 API. This tool has usually displayed the best performance.

134 2.2.6. *JAMES-II*

135 Developed at the University of Rostock, the Java-based Multipurpose Environment for Simulation II
136 (JAMES II) provides support for many different formalisms, including various variants of DEVS. Besides
137 an API to define models, this framework also provides a GUI to configure experiments and check simulation
138 results. This simulation engine supports sequential and parallel execution [16].

139 2.2.7. *DEVSsim++*

140 Developed by Tag Gon Kim and his group at Korea Advanced Institute of Technology (KAIST) [17],
141 this is a C++ based engine and used extensively for large simulations focusing on wargaming and simulation
142 interoperability.

143 2.2.8. *xDEVS*

144 xDEVS engine is Java-based and is released under the GNU Public License (GPL). This facilitates the
145 rapid development of new components and extensions, and wide adoption of the core engine. xDEVS
146 provides the user with a set of base classes that can be used to develop new DEVS models, or to develop
147 new DEVS simulation engines. It is based on the fundamental separation of model and the underlying
148 corresponding simulator [2] and rightly so, provides, the modeling Application Program Interface (API) and
149 the simulation API [18]. It is made available as a standalone executable jar and as an Eclipse plugin.

150 2.2.9. *Others*

151 In addition to the above DEVS implementations used widely, there are others with selective adoption
152 such as GALATEA [22] for Multi-Agent Systems (MAS), SimStudio [23], PowerDEVS [24] for hybrid
153 systems, MS4Me based on DEVSJAVA [25] and last but not the least, Virtual Laboratory Environment
154 (VLE) [26], that based on C++, is a multiparadigm environment based on several DEVS extensions.

155 We have selected five well-known DEVS simulation frameworks distributed among three implemen-
156 tation languages and compared their performance against a revisited DEVStone benchmark. The current
157 diversity on the programming languages used is concentrated on C++, JAVA and Python. As a conse-
158 quence, we have selected two JAVA-based simulators (DEVSJAVA and xDEVS), two C++-based simulators
159 (aDEVs and CD++) and PyPDEVs as the Python-based simulation engine. In the following, we describe
160 the revisited DEVStone benchmark.

161 3. DEVStone

162 DEVStone is a synthetic benchmark [21] that has been used in recent years to evaluate the performance
163 of different DEVS simulators [21] [27] [28]. DEVStone can be used to automatically generate a vast variety
164 of models with different shapes and sizes. These models can then be simulated to test different features with
165 respect to the corresponding simulator. A DEVStone benchmark is defined with five parameters:

166 **Type:** Different structure and interconnection schemes between the components in the model.

167 **Width** This parameter is based the number of components in each intermediate coupled model.

168 **Depth** The number of levels in the model hierarchy.

169 **Internal transition time:** The execution time spent by each internal transition function.

170 **External transition time:** The execution time spent by each external transition function.

171 According to the DEVStone specifications, both the internal and external transition function times are
172 spent executing Dhrystones [29] to keep the CPU busy.

173 In [21], four different DEVStone benchmarks were presented (named LI, HI, HO and HOMod), deriving
174 different equations to compute the number of external and internal transition functions.

175 In the following a formal definition of the DEVStone atomic model is introduced. Next, all the five
176 benchmarks considered in this work (LI, HI, HO, HOMod and the newly introduced HOMem) are presented.

177 To simplify the computation of the total number of events triggered, it is assumed that: (1) the execution time
178 spent by the external or internal transition function is equal to 0 seconds, i.e. the transition is instantaneous
179 in a computational sense, and (2) all the events injected to the DEVStone benchmarks are separated in time
180 by more than 0 seconds.

Algorithm 1 DEVStone atomic model

Require: NUM_DELT_INTS, NUM_DELT_EXTS and NUM_OF_EVENTS are global variables, and store the total number of internal transition functions, external transition functions and events triggered inside the whole model. Δ_{int} and Δ_{ext} are the delays introduced in the internal and external transition functions, respectively.

```
function [list,phase, $\sigma$ ] = init()
list = [] {list is part of the state, and stores all the events received by this atomic model}
 $\sigma = \infty$ 

function [list,phase, $\sigma$ ] =  $\delta_{\text{int}}$ (list,phase, $\sigma$ )
NUM_DELT_INTS = NUM_DELT_INTS + 1
Dhystone( $\Delta_{\text{int}}$ )
list = []
 $\sigma = \infty$ 

function [list,phase, $\sigma$ ] =  $\delta_{\text{ext}}$ (list,phase, $\sigma$ , $e$ , $X^b$ )
NUM_DELT_EXTS = NUM_DELT_EXTS + 1
Dhystone( $\Delta_{\text{ext}}$ )
values =  $X^b(\text{in})$  { $X^b(\text{in})$  is a list containing all the events waiting in the “in” input port}
NUM_OF_EVENTS = NUM_OF_EVENTS + values.size()
list = [list;values] {Concatenate both lists}
phase = “active”
 $\sigma = 0$ 

function [list,phase, $\sigma$ ] =  $\delta_{\text{con}}$ (list,phase, $\sigma$ , $ta(s)$ , $X^b$ )
 $\delta_{\text{ext}}(\delta_{\text{int}}(\text{list},\text{phase},\sigma),0,X^b)$ 

function  $\lambda()$ 
send(“out”, list) {sends the whole list by the “out” output port}

function  $\sigma = ta(\text{list},\text{phase},\sigma)$ 
 $\sigma = \sigma$ 
```

181 *3.1. DEVStone atomic model*

182 The atomic model of DEVStone can be defined as shown in Algorithm 1.

183 *3.2. LI (Low level of Interconnections) models*

184 Figure 1 shows the general structure of an LI model. With d layers (depth), the first $d - 1$ (with $d \geq 1$)
185 layers have the structure of Figure 1(a). All these layers have one coupled model and $w - 1$ (with $w \geq 2$)
186 atomic models (where w is the width). On the other hand, the d -th layer has the structure given in Figure
187 1(b), just with one atomic model. The arrows in the Figure represent the connection between the input and
188 output ports in the whole model.

189 As stated above, two metrics are measured: execution time and memory footprint (also known as mem-
190 ory high-water mark). Obviously, these two metrics depend on the number of atomic models, number of

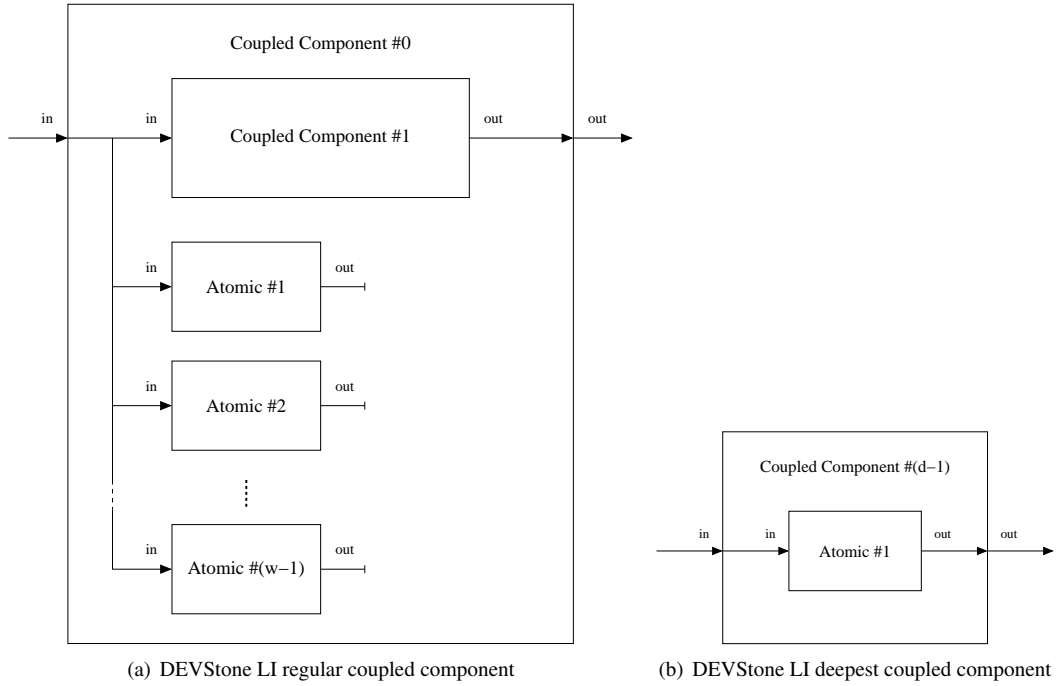


Figure 1: DEVStone LI components

191 internal transitions, number of external transitions, and the total number of events internally generated. Ad-
 192 ditionally, memory footprint depends on the concurrency of the model, that is, the number of pending events
 193 simultaneously waiting at the input ports.

194 Since the model structure is known, and the simplification $\Delta_{\text{int}} = \Delta_{\text{ext}} = 0$ is made, the theoretical
 195 execution time and the total number of events generated can be easily computed.

196 Firstly, considering the model's $d - 1$ levels with $w - 1$ atomic models and 1 level with 1 atomic model,
 197 the total number of atomic models is:

$$\# \text{Atomic} = (w - 1) \cdot (d - 1) + 1 \quad (3)$$

198 Secondly, LI models produce one external transition, output event and internal transition for each atomic
 199 model and external events injected. Thus, in LI models, the number of transitions and events generated is
 200 equal to the number of atomic models multiplied by the total number of external events injected N :

$$\#\delta_{\text{int}} = N \cdot ((w - 1) \cdot (d - 1) + 1) \quad (4)$$

$$\#\delta_{\text{ext}} = N \cdot ((w - 1) \cdot (d - 1) + 1) \quad (5)$$

$$\#\text{Events} = N \cdot ((w - 1) \cdot (d - 1) + 1) \quad (6)$$

201 In the following DEVStone benchmarks, we derive the equations for the number of transition functions
202 and events internally generated given a single external event injected, i.e., for this benchmark:

$$\#\delta_{\text{int}} = (w - 1) \cdot (d - 1) + 1 \quad (7)$$

$$\#\delta_{\text{ext}} = (w - 1) \cdot (d - 1) + 1 \quad (8)$$

$$\#\text{Events} = (w - 1) \cdot (d - 1) + 1 \quad (9)$$

203 3.3. HI (High Input couplings) models

204 Figure 2 shows the general structure of a HI model. It is equal to the LI model, but where the output
205 port of an atomic component i is connected to the input port of the next atomic component $i + 1$, as seen in
206 Figure 2(a).

207 Therefore, the number of atomic models is equal to the LI model. However, the number of transition
208 functions and events generated are quite different, because for each external input, the set of $w - 1$ atomic
209 models acts as a shift register, generating one additional event for each external event. As a result, the
210 number of atomic models, transition functions and events generated is computed as follows:

$$\#\text{Atomic} = (w - 1) \cdot (d - 1) + 1 \quad (10)$$

$$\#\delta_{\text{int}} = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 = \left(\frac{w^2 - w}{2} \right) \cdot (d - 1) + 1 \quad (11)$$

$$\#\delta_{\text{ext}} = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 = \left(\frac{w^2 - w}{2} \right) \cdot (d - 1) + 1 \quad (12)$$

$$\#\text{Events} = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 = \left(\frac{w^2 - w}{2} \right) \cdot (d - 1) + 1 \quad (13)$$

211 3.4. HO (Hi model with numerous Outputs) models

212 Figure 3 shows the general structure of a HO model. HO has a more complex interconnection map with
213 the same number of atomic and coupled components. For example, HO coupled components have two input

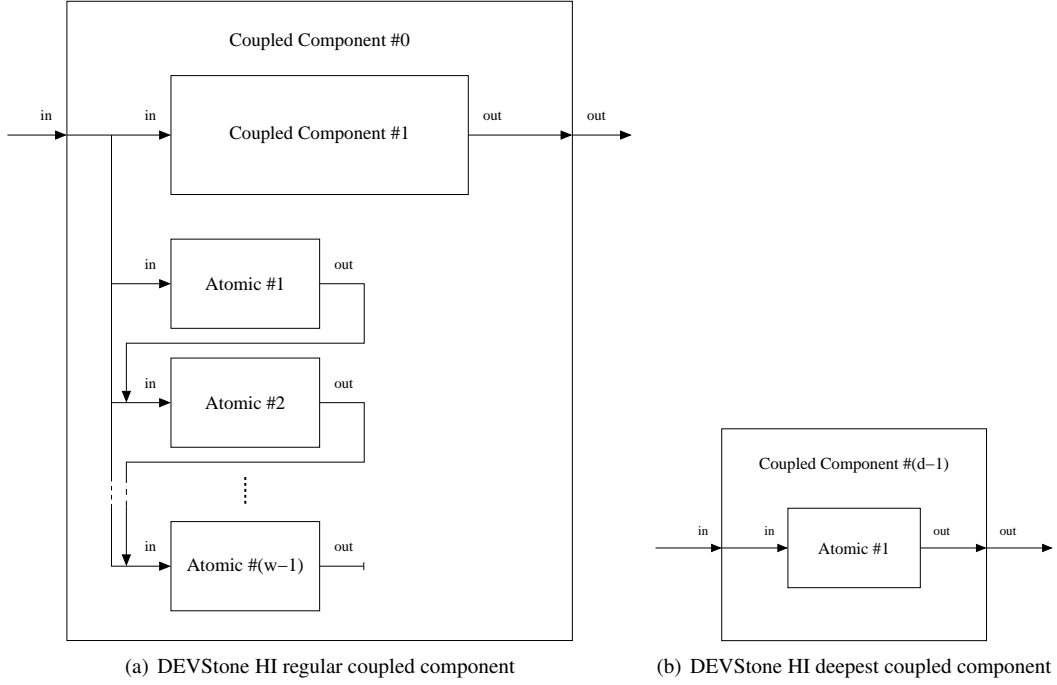


Figure 2: DEVStone HI components

214 and two output ports in each level. The main differences with HI are that the second input port of each
 215 coupled model is connected to the input of each atomic model. Additionally, the output of each atomic
 216 model is connected to the second output of its parent coupled model.

217 It is worthwhile to mention that the number of atomic models, transition functions and events generated
 218 in HO models are exactly the same as in the HI model. However, the main difference is in both the execution
 219 time and memory footprint, which are higher due to the additional external input connections. Thus,

$$\#Atomic = (w - 1) \cdot (d - 1) + 1 \quad (14)$$

$$\#\delta_{int} = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 \quad (15)$$

$$\#\delta_{ext} = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 \quad (16)$$

$$\#Events = \left((w - 1) + \sum_{i=1}^{w-2} i \right) \cdot (d - 1) + 1 \quad (17)$$

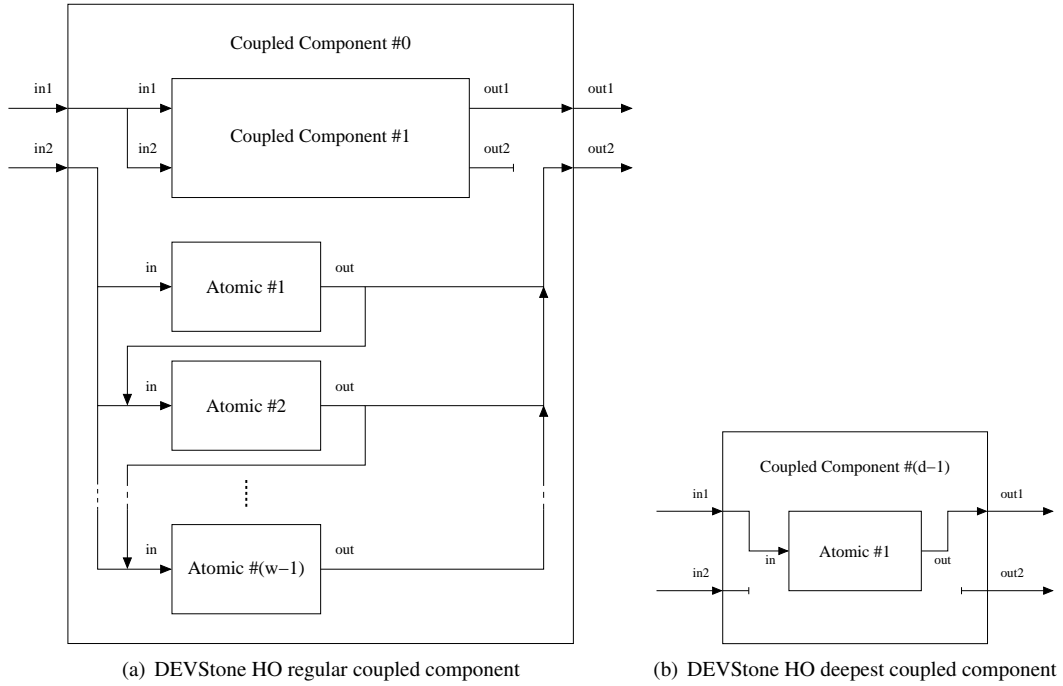


Figure 3: DEVStone HO components

220 3.5. *HOMod models*

221 Figure 4 depicts the structure of a *HOMod* DEVStone model. As usual, the deepest coupled model is
 222 formed by one single atomic model. The remaining coupled models are constituted by 1 coupled model,
 223 a chain of $w - 1$ atomic models, and a set of $k = 1 \dots w - 1$ chains formed by $\sum_{i=1}^k i$ atomic models. The
 224 second external input port is connected to the whole first row and only to the first atomic component in the
 225 remaining rows. Additionally, all the atomic models in the second row are connected to the first row, which
 226 in turn send the whole output directly to the coupled component. Finally, each remaining atomic component
 227 is connected to its upper component.

228 The computation of the number of atomic modes is quite straightforward.

$$\#Atomic = \left((w - 1) + \sum_{i=1}^{w-1} i \right) \cdot (d - 1) + 1 \quad (18)$$

229 However, the calculation of the number of transition functions is hard. After an exhaustive mathematical
 230 analysis we have determined that:

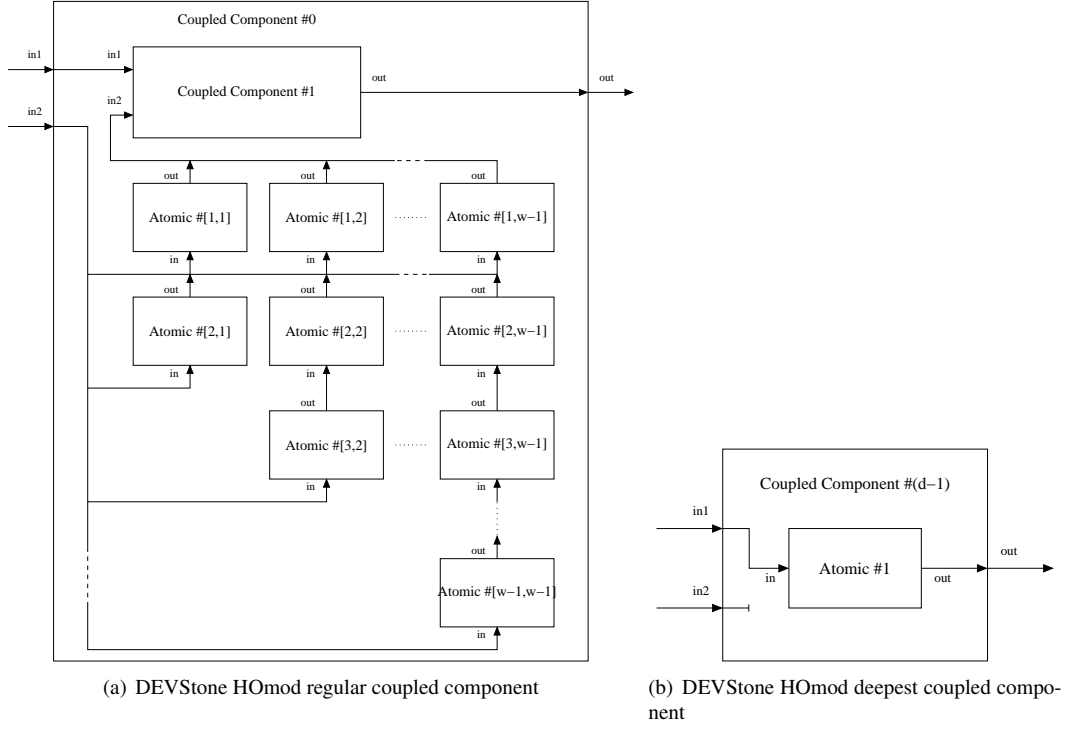


Figure 4: DEVStone HMod components

$$\#\text{Atomic} = \left((w-1) + \sum_{i=1}^{w-1} i \right) \cdot (d-1) + 1 \quad (19)$$

$$\#\delta_{\text{int}} = (d-1) \cdot (w-1)^2 + \left((d-1) + (w-1) \cdot \sum_{i=1}^{d-2} i \right) \times \left((w-1) + \sum_{i=1}^{w-1} i \right) + 1 \quad (20)$$

$$\#\delta_{\text{ext}} = (d-1) \cdot (w-1)^2 + \left((d-1) + (w-1) \cdot \sum_{i=1}^{d-2} i \right) \times \left((w-1) + \sum_{i=1}^{w-1} i \right) + 1 \quad (21)$$

231

Similarly, the computation of the number of events follows a recursive equation, defined below:

$$\#\text{Events} = \sum_{l=1}^{d-1} \left(\sum_{c=1}^{K_l+w-1} \left(W_1 \times \sum_{i=1}^w P_l^{c-i+1} + \sum_{i=1}^w (W_i \cdot P_l^{c-i+1}) \right) \right) + 1 \quad (22)$$

232

where:

$$W_i = \begin{cases} w-i & \text{if } w-i \geq 0 \\ 0 & \text{otherwise} \end{cases} \quad (23)$$

$$K_l = \begin{cases} 1 & \text{if } l = 1 \\ K_{l-1} + W_1 & \text{if } l > 1 \end{cases} \quad (24)$$

233 and

$$P_1^1 = 1 \quad (25)$$

$$P_l^j = 0 \text{ if } 1 > j > K_l \quad (26)$$

$$P_l^j = (w - 1) \times \sum_{i=1}^w P_{l-1}^{j-i+1} \quad (27)$$

234 As can be seen, the complexity of the equations describing the metrics of HOmod is high. The inclusion
 235 of these equations in a simulator is hard, and the theoretical analysis becomes prohibitive. For these reasons,
 236 we have defined a new DEVStone benchmark named HOMem that, providing the same computational effort
 237 than HOmod into the different simulation frameworks, shows a straightforward mathematical formulation.

238 3.6. HOMem models

239 As stated above, we propose the inclusion of a new model in the DEVStone benchmark called HOMem.
 240 HOMem is basically proposed as a mechanism to increment the traffic of events with respect to HO, equiva-
 241 lently to HOmod, but with a simpler structure and mathematical description.

242 Figure 5 shows the structure of the HOMem DEVStone benchmark. As can be seen, the deepest coupled
 243 model is identical to HOmod. As for the remaining coupled models, each one is formed by 1 coupled model
 244 and $2 \cdot (w - 1)$ atomic models. The second $w - 1$ chain receives the input through external input connections,
 245 and propagates these inputs to the first chain of $w - 1$ atomic models. These, in turn, send all the inputs
 246 received to the coupled model.

247 The number of transition functions are easy to compute, since it is equal to the number of atomic models.
 248 However, to calculate the number of events it must be taken into account that each single event is sent $w - 1$
 249 times to the whole second chain of atomic models. This grows exponentially with the depth of the model, in
 250 the following form:

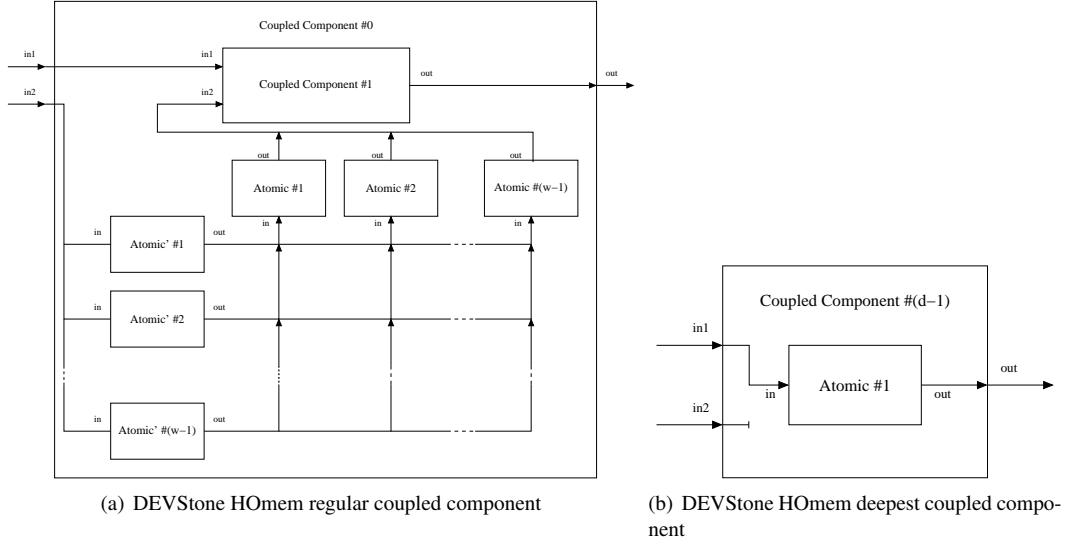


Figure 5: DEVStone HOMem components

$$\#\text{Atomic} = 2 \cdot (w - 1) \cdot (d - 1) + 1 \quad (28)$$

$$\#\delta_{\text{int}} = 2 \cdot (w - 1) \cdot (d - 1) + 1 \quad (29)$$

$$\#\delta_{\text{ext}} = 2 \cdot (w - 1) \cdot (d - 1) + 1 \quad (30)$$

$$\#\text{Events} = \sum_{l=1}^{d-1} \left((w - 1)^{2^l} + (w - 1)^{2^{l-1}} \right) + 1 \quad (31)$$

251 Experimental results show that this straightforward specification leads to similar execution time and
 252 memory footprint, when compared to HMod.

253 4. Experimental Methodology

254 Once the DEVStone equations have been analytically derived, we compare CPU execution time and
 255 memory footprint over a total of five well known simulation engines using all the benchmarks presented
 256 above. Our aim is to show an exhaustive comparison and a standard procedure to evaluate the performance
 257 of any new discrete event simulator.

258 We first provide a detailed description of the experimental set-up used in this research.

259 All the benchmarks presented above (LI, HI, HO, HMod and HOMem) were executed using five sim-
 260 ulation engines: aDEVS 2.8.1, CD++ 2.45 (a CD++ branch with support for PDEVS), DEVSJAVA 3.1,

261 xDEVS 1.20151013 and PyPDEVS 2.2.4. Table 1 shows the programming language and the main data
 262 structures used in each simulation engine. As stated above, CD++ and aDEVS are C++ implementations,
 263 DEVSJAVA and xDEVS have been implemented using Java, whereas PyPDEVS is a Python simulation
 264 engine. As Table 1 shows, aDEVS and xDEVS use generic classes, whereas PyPDEVS uses duck typing.
 265 To store events, aDEVS and CD++ use standard C++ arrays. On the contrary, DEVSJAVA, xDEVS and
 266 PyPDEVS use dynamic data structures, like linked lists or dictionaries. Finally, to store components and
 267 implement the simulation scheduler, all the frameworks use dynamic data structures such as sets or linked
 268 lists.

	aDEVS	CD++	DEVSJAVA	xDEVS	PyPDEVS
Programming Language	C++	C++	Java	Java	Python
Generics	Yes	No	No	Yes	Duck typing
Events container	array/port	array/port	Hashtable	LinkedList/port	dictionary
Components container	std::set	std::list	HashSet	LinkedList	list

Table 1: Main data structures used in the simulation engines

269 We tested all these simulation engines in two different machines: a 48 GB AMD Opteron 6272 @ 2.1
 270 GHz (abbreviated as AMD) and a 64 GB Intel Xeon 2670 @ 2.6GHz “Sandy Bridge” (abbreviated as Intel),
 271 in both cases under a GNU/Linux Debian 8 Operating System. aDEVS and CD++ were compiled using the
 272 `gcc -O3` optimization level.

273 In all the test cases, only one external event was injected, generating the total number of transition
 274 functions and the total number of events given in the previous equations. As demonstrated in [21] [27] [28],
 275 the previous metric just scaled linearly with the number of external events.

276 Each benchmark type was generated for different values of width and depth. These values were defined
 277 for running different trials with all the five simulators. We looked for a good trade-off between wall-clock
 278 simulation time and memory footprint, since these are the metrics measured in all the simulations. Table 2
 279 shows these intervals, where each row represent a DEVStone benchmark type, in relation with the width
 280 and depth, each described by the minimum value, the step size, and the maximum value used to generate a
 281 full range for these parameters. For example, the smallest LI model is a 2×1 model, where width = 2 and
 282 depth = 1. The biggest model, on the other hand, is a 1502×1501 model.

283 Finally, each simulation is repeated 10 times for each simulator, benchmark, size, and hardware plat-
 284 forms. Simulation wall-clock time and memory footprint are averaged over these 10 trials. Although no
 285 significant deviations were appreciated, we kept this number of trials to avoid spurious deviations. Table 2

286 shows in the last column the total number of simulations performed.

Benchmark	Width			Depth			# Simulations
	Min.	Step	Max.	Min.	Step	Max.	
LI	2	100	1502	1	100	1501	25600
HI	2	100	1102	1	100	1101	14400
HO	2	100	1102	1	100	1101	14400
HOMod	2	1	10	1	1	10	9000
HOMem	2	1	10	1	1	10	9000

Table 2: Parameters configuration

287 5. Results

288 5.1. CPU comparison

Simulator	LI		HI		HO	
	AMD	Intel	AMD	Intel	AMD	Intel
aDEVs	2.5×10^0 1.19	2.1×10^0 1.19	1.0×10^3 1.11	1.0×10^3 1.11	1.2×10^3 1.11	1.2×10^3 1.11
CD++	∞ ∞	∞ ∞	6.3×10^3 3.46	5.1×10^3 3.46	7.0×10^3 3.69	4.5×10^3 3.69
DEVsJAVA	∞ ∞	∞ ∞	6.6×10^4 4.23	4.0×10^4 4.21	∞ ∞	∞ ∞
xDEVs	3.8×10^0 1.95	2.6×10^0 2.07	9.3×10^2 1.88	4.6×10^2 1.84	1.0×10^3 1.94	5.0×10^2 1.84
PyPDEVs	∞ ∞	∞ ∞	∞ ∞	∞ ∞	∞ ∞	∞ ∞

Table 3: Execution time (seconds) and memory footprint (GiB) of the larger models executed by the five simulation engines and in both AMD and Intel servers

289 Table 3 shows a comparison in execution time (in seconds, measured inside the simulator to avoid the
 290 loading time of the model) and memory footprint (in GiB, measured using the general GNU `time` command)
 291 for the five simulation engines and the largest models of the DEVStone models tested in this work, i.e., LI
 292 1502×1501, HI 1102×1101, and HO 1102×1101. HOMod 10×10 and HOMem 10×10 are not included
 293 because no simulator was able to finish them, at least during the 48 hours we run these tests. The same
 294 happened in all those cases in Table 3 marked with ∞ . As can be seen, only aDEVs and xDEVs were
 295 able to finish all the models in Table 3, followed by CD++, which was not able to load the largest LI
 296 model. Regarding memory footprint, there is not much difference between both servers. However, in terms
 297 of execution time, the best server in almost all cases was the 64 GB Intel Xeon 2670 @ 2.6GHz “Sandy

298 Bridge”, since between both servers, this one has the fastest processor and memory. Thus, simulation results
299 are coherent with the server used, i.e., the faster the processor and the greater the memory size, the faster the
300 simulation. Memory footprint is independent of the server, since it only depends on the internal structure of
301 the DEVStone model.

302 As can be seen in Table 3, some simulators were not able to execute the model because the system was
303 unable to handle the memory requirements. To tackle these issues in the remaining analysis, the wall clock
304 execution time is limited to 1200 seconds and the memory footprint to 4 GiB, enough to perform our more
305 than 70000 simulations in a reasonable amount of time, also obtaining significant values to compare. Thus,
306 in the following, every experiment with time or memory greater than the aforementioned values is truncated
307 to 1200 seconds or 4 GiB, respectively.

308 5.2. Execution time

309 Figure 6 shows the contour maps of the different execution times needed by all the five simulators in
310 both LI and HI models. Blue regions mean low execution time, whereas red regions mean high execution
311 time.

312 CD++, DEVSJAVA and PyPDEVs saturated the execution time of 1200 seconds multiple times in both
313 models. aDEVs and xDEVs, on the contrary, reached the best results.

314 Regarding the LI model, the ordered list of simulators, from best to worst contour maps is: aDEVs,
315 xDEVs, CD++, DEVSJAVA and PyPDEVs.

316 With respect to the HI model, the list is: xDEVs, aDEVs, CD++, DEVSJAVA and PyPDEVs.

317 Continuing with this analysis, Figure 7 shows the same contour maps, this time in HO and HMem
318 models.

319 Regarding the HO model, xDEVs obtained best execution times, specially as width and depth were
320 increased. For low values of width and depth, aDEVs was better than xDEVs. Once again, CD++, DEVA-
321 JAVA and PyPDEVs saturated the execution time limit of 1200 seconds.

322 With respect to HMod and HMem, all the simulators reached the maximum execution time quite
323 soon, with relatively small models. Moreover, in the case of HMod, only two simulators, aDEVs and
324 xDEVs, were able to load all the models in memory, before the execution of the simulation. In fact, this
325 is due to the intrinsic complexity of the HMod benchmark, which includes many more atomic models
326 than HMem. HMem is simpler in structure than HMod, and all the simulation engines are able to load
327 it. Once the simulation starts, HMod and HMem offer similar execution time and memory footprint, as
328 shown in Section 5.4.

329 We do not show a comparison between all the simulators in HOmod because only aDEVS and xDEVS
330 were able to run a significant number of HOmod instances. These experiments are shown in the comparison
331 between aDEVS and xDEVS.

332 5.3. Memory footprint

333 As mentioned before, memory footprint is the memory high-water mark of a process. The comparison
334 of all the five simulators were performed constraining the execution time to 1200 seconds and the memory
335 footprint to 4 GiB. The set of five simulators compared in this paper have been developed using different
336 programming languages: aDEVS and CD++ in C++, DEVSJAVA and xDEVS in JAVA, and PyPDEVS in
337 Python. Since JAVA and Python use their own virtual machines, it is expected that these simulators have a
338 higher memory footprint. However, our experimental results showed some exceptions in this regard.

339 Figure 8 shows the memory footprint reached by the five simulators in LI and HI models. As can be seen,
340 DEVSJAVA and specially PyPDEVS reached the memory limit quite soon. aDEVS had by far the lowest
341 memory usage. However, between CD++ and xDEVS, the latter obtained less memory footprint even when
342 the Java Virtual Machine must be loaded into memory. This is because CD++ uses a complex structure to
343 store the model, as is evident when CD++ is completely saturated once width and depth is greater than 1200.

344 Now, Figure 9 shows the memory footprint reached by the five simulators in HO and HOMem models.

345 Regarding HO, the situation is almost identical to the HI model. aDEVS and xDEVS are still the two
346 best simulators.

347 With respect to HOMem, all the five simulators reached the memory limit quite soon. As in the exe-
348 cution time analysis, DEVSJAVA was the first to leave the model, for *width* greater than six. Surprisingly,
349 PyPDEVS offered comparable results to aDEVS, CD++ and xDEVS in HOMem and HOmod, the more
350 complex models.

351 As in the previous section, we do not show a comparison between all the simulators in HOmod because
352 only aDEVS and xDEVS were able to run a significant number of HOmod instances.

353 As a conclusion, we may say that, regarding memory footprint, aDEVS is by far the best DEVS simulator
354 between those analyzed in this paper. In the case of execution time, xDEVS is better as the complexity of
355 the model increases, until the cases of HOmod and HOMem, where the complexity of both models cannot
356 determine a classification with clarity. In the following, we investigate the performance of aDEVS and
357 xDEVS simulators in finer details, as well as the similarities between HOmod and HOMem.

358 *5.4. Comparison between aDEVs and xDEVs*

359 Firstly, we show the difference in execution time and memory footprint obtained by both simulators in
360 LI, HI, HO, HOmod and HOMem models.

361 Figure 10 depicts five contour maps. Each one represent the difference, in execution time, of xDEVs
362 minus aDEVs.

363 In the case of models with lower complexity, like the LI model in Figure 10(a), the difference is small
364 (2.5 seconds vs 2.1 seconds according to Table 3) and in favor of aDEVs. With respect to HOmod and
365 HOMem, the difference fundamentally varies from -10 seconds to 10 seconds, with more cases in favor of
366 aDEVs. However, these two models remain indecisive since they show sparse maps.

367 The analysis of Figures 10(b) and 10(c) is much clearer. As the model complexity is increased, the
368 difference is higher, in favor of xDEVs (up to 700 seconds faster in the case of HO).

369 We now compare both simulator in the HOmod and HOMem DEVStone model. aDEVs and xDEVs
370 were the only two simulators that were able to simulate a significant number of HOmod models.

371 Figure 11 depicts both the execution time and memory footprint reached by aDEVs and xDEVs in
372 HOmod and HOMem models. In both cases, contour maps are practically Yes/No maps, where, after a
373 given *width* and *depth* both simulators immediately reach the limit in execution time and memory footprint.
374 These “saturation” values in HOmod are reached “sooner” (in terms of w and d) than the corresponding
375 values in the HOMem model. We prove here that HOMem offers the same results than HOmod with a
376 more straightforward mathematical formulation, after a comparison of equations (28)-(31) against equations
377 (18)-(27).

378 **6. Conclusions**

379 The Discrete Event System Specification formalism (DEVs) has been widely used to conceive, design,
380 model and develop a great variety of systems. DEVs has been implemented in various languages and
381 platforms over the years. The DEVStone benchmark defines a set of models with varied structure and
382 behavior, and was designed to evaluate the performance of DEVs-based simulators.

383 The key contributions of this work are the following. We have added a new model to the benchmark,
384 called HOMem, which shows identical qualitative behavior than HOmod but with a more manageable math-
385 ematical formulation. As HOmod, HOMem is also intensive on both execution time and memory usage.
386 We have added the study of memory footprint in DEVStone, deriving the equations needed to compute the

387 number of events triggered inside the model and per each single injected external event. We have also re-
388 calculated the number of transition functions triggered in all the DEVStone benchmarks. Finally, we have
389 compared five simulation engines in two different hardware platforms, analyzing both the execution time and
390 memory footprint. To perform a fair comparison between simulation engines that allow and do not allow
391 model flattening, we did not flattened the benchmark in any case.

392 These five DEVStone models are executed against five different DEVS simulators, implemented in dif-
393 ferent programming languages such as C++, JAVA and Python.

394 Results show that all the simulators were able to run the HOMem model at least for a significant range
395 of *width* and *depth* values. Between all the five simulators, aDEVs, which is based on C++, had the lowest
396 memory footprint at least in LI, HI, and HO models. With respect to execution time, xDEVs was the fastest
397 one, specially in the set of HI and HO more complex models.

398 As future work, we propose the extension of this complete analysis to study the performance of DEVs-
399 tone parallel and distributed simulations.

400 **Acknowledgment**

401 The authors would like to thank Dr. Gabriel Wainer and Dr. Sixuan Wang for their assistance in the
402 compilation of CD++ under GNU/Linux.

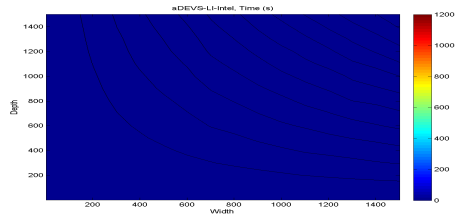
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404 TIN2014-54806-R and TIN2013-40968-P.

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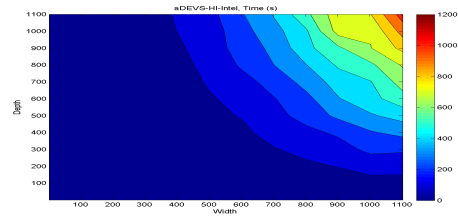
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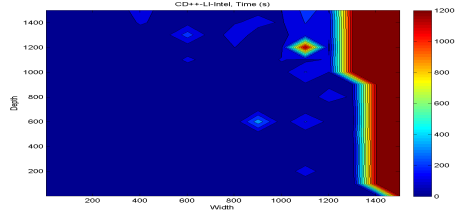
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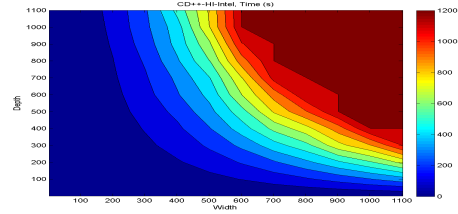
(a) aDEVS - LI



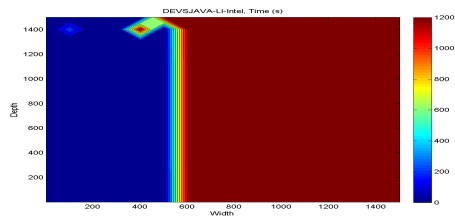
(b) aDEVS - HI



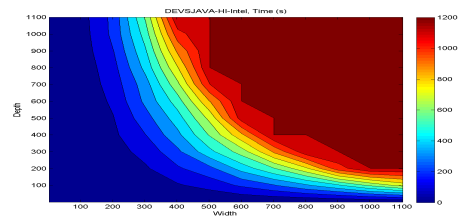
(c) CD++ - LI



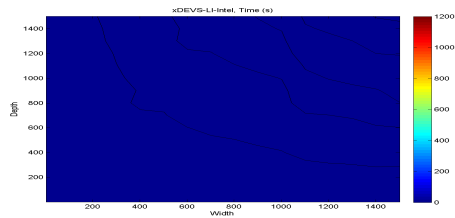
(d) CD++ - HI



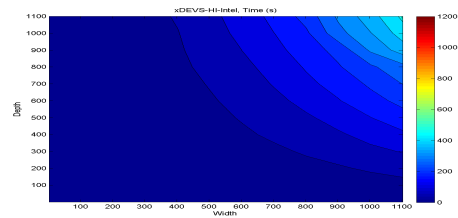
(e) DEVJSJAVA - LI



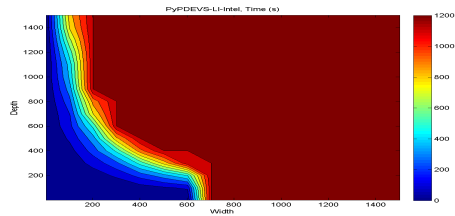
(f) DEVJSJAVA - HI



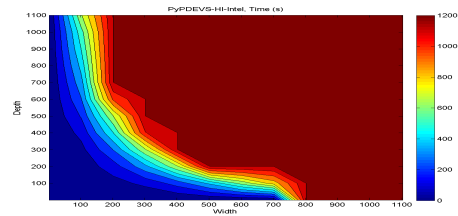
(g) xDEVS - LI



(h) xDEVS - HI

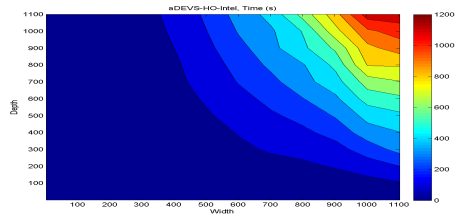


(i) PyPDEVS - LI

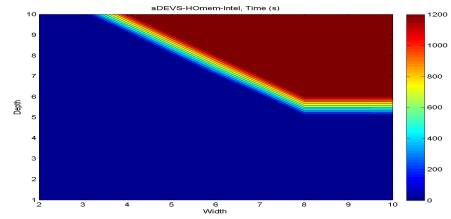


(j) PyPDEVS - HI

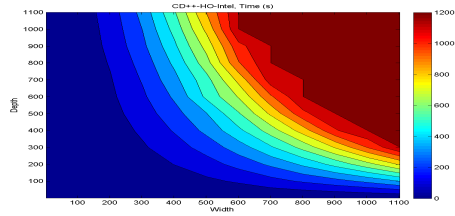
Figure 6: Execution time of LI and HI models



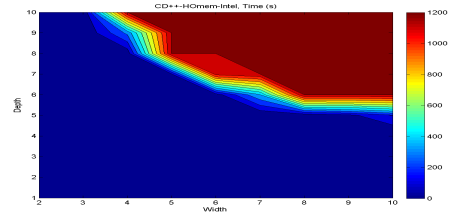
(a) aDEVS - HO



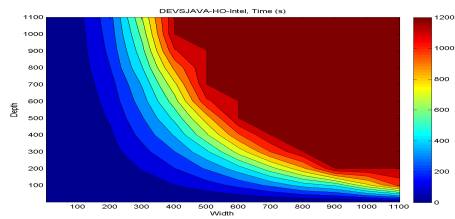
(b) aDEVS - HOMem



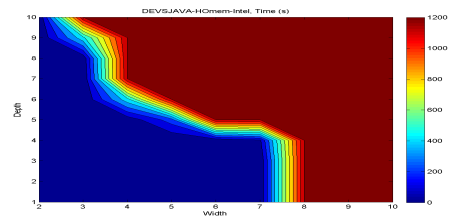
(c) CD++ - HO



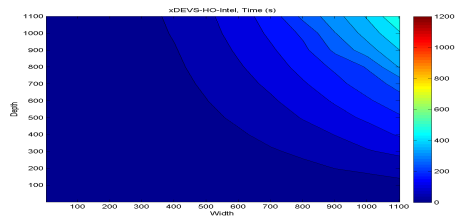
(d) CD++ - HOMem



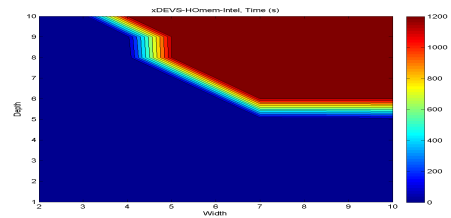
(e) DEVJSJAVA - HO



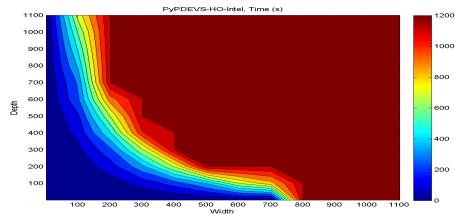
(f) DEVJSJAVA - HOMem



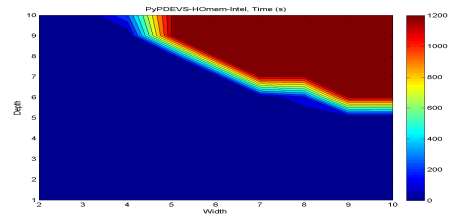
(g) xDEVS - HO



(h) xDEVS - HOMem

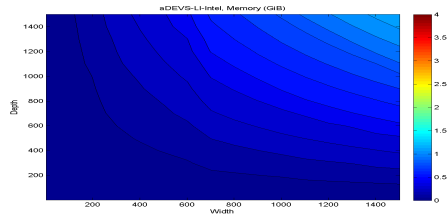


(i) PyPDEVS - HO

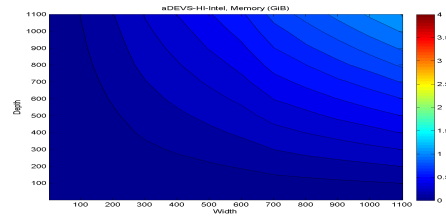


(j) PyPDEVS - HOMem

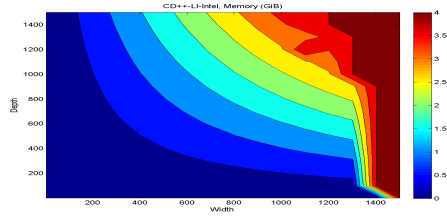
Figure 7: Execution time of HO and HOMem models



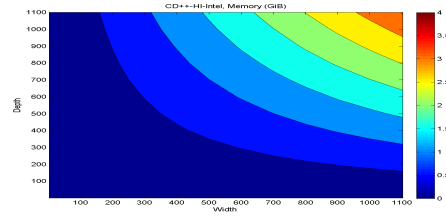
(a) aDEVs - LI



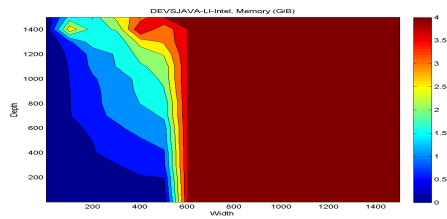
(b) aDEVs - HI



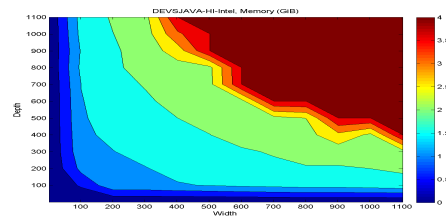
(c) CD++ - LI



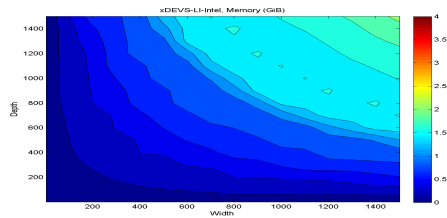
(d) CD++ - HI



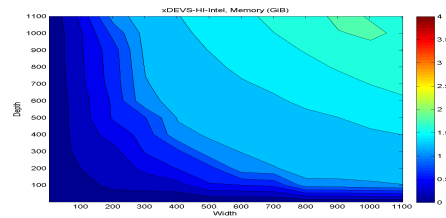
(e) DEVsJAVA - LI



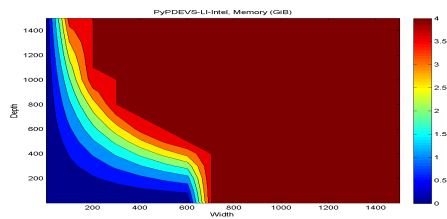
(f) DEVsJAVA - HI



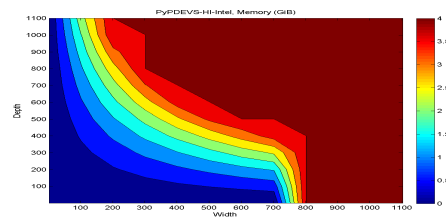
(g) xDEVs - LI



(h) xDEVs - HI

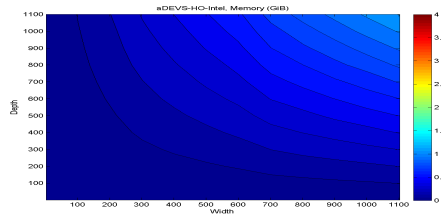


(i) PyPDEVs - LI

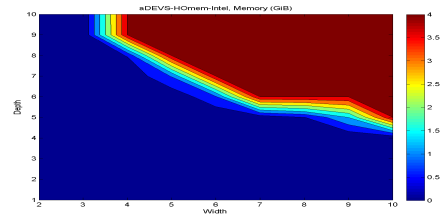


(j) PyPDEVs - HI

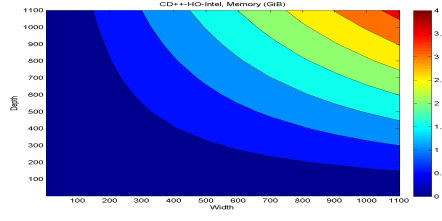
Figure 8: Memory footprint of LI and HI models



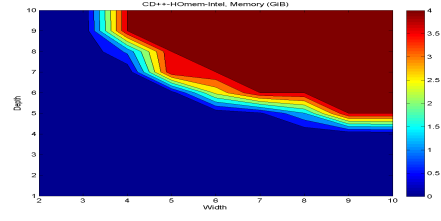
(a) aDEVS - HO



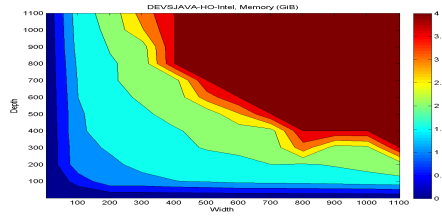
(b) aDEVS - HOMem



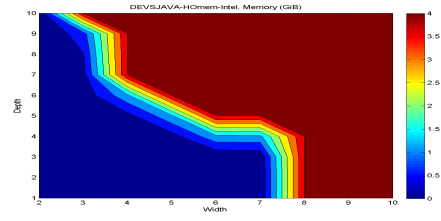
(c) CD++ - HO



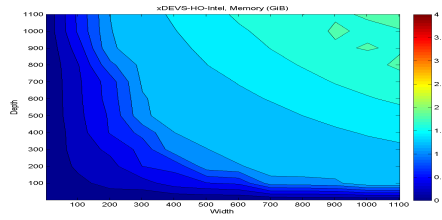
(d) CD++ - HOMem



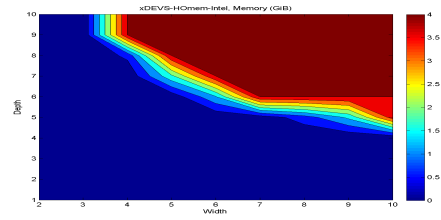
(e) DEVSJAVA - HO



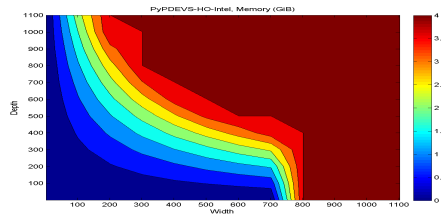
(f) DEVSJAVA - HOMem



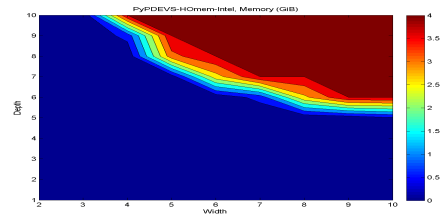
(g) xDEVS - HO



(h) xDEVS - HOMem

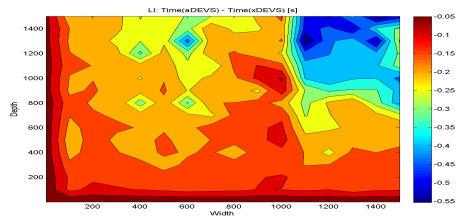


(i) PyPDEVS - HO

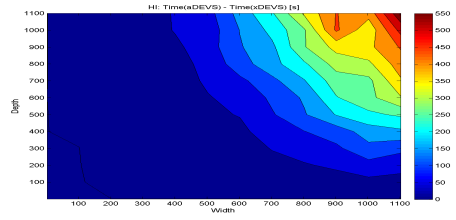


(j) PyPDEVS - HOMem

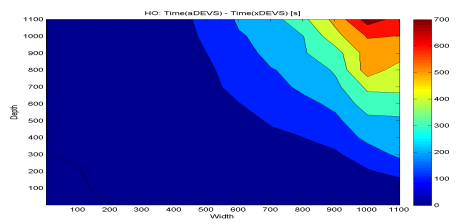
Figure 9: Memory footprint of HO and HOMem models



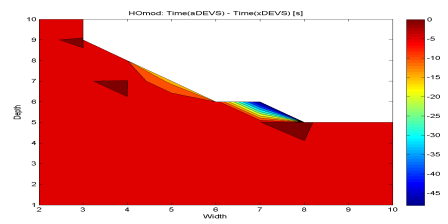
(a) LI: xDEVS - aDEVS



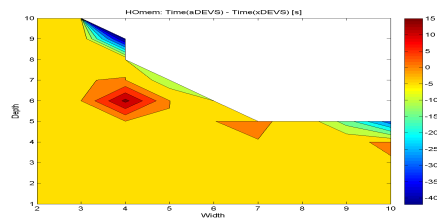
(b) HI: xDEVS - aDEVS



(c) HO: xDEVS - aDEVS

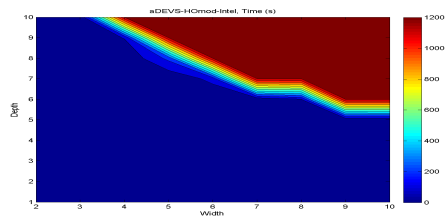


(d) HOmod: xDEVS - aDEVS

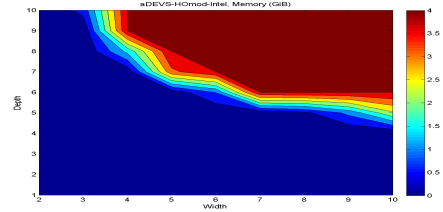


(e) HOMem: xDEVS - aDEVS

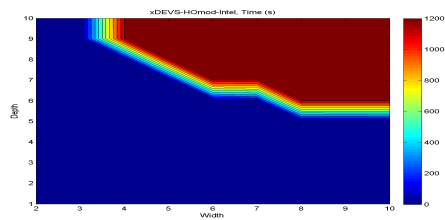
Figure 10: Execution time comparison of LI, HI, HO, HOmod and HOMem models computed as $\text{Time}(x\text{DEVS}) - \text{Time}(a\text{DEVS})$



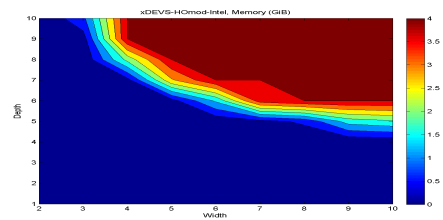
(a) aDEVS - HMod (Time)



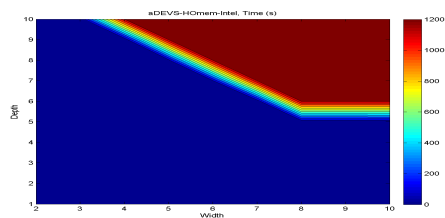
(b) aDEVS - HMod (Memory)



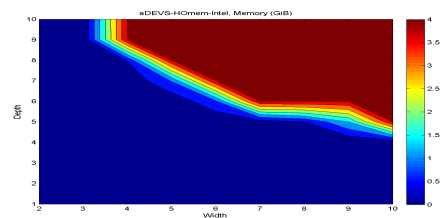
(c) xDEVS - HMod (Time)



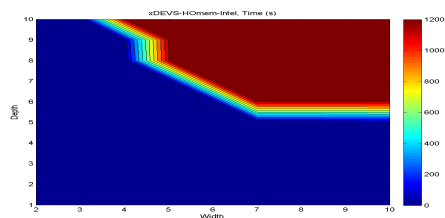
(d) xDEVS - HMod (Memory)



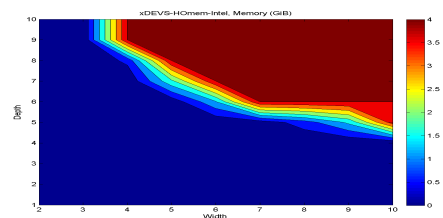
(e) aDEVS - HMem (Time)



(f) aDEVS - HMem (Memory)



(g) xDEVS - HMem (Time)



(h) xDEVS - HMem (Memory)

Figure 11: Execution time and memory footprint of HMod and HMem models given by aDEVS and xDEVS