

# Electrical Impedance Tomography for Deformable Media

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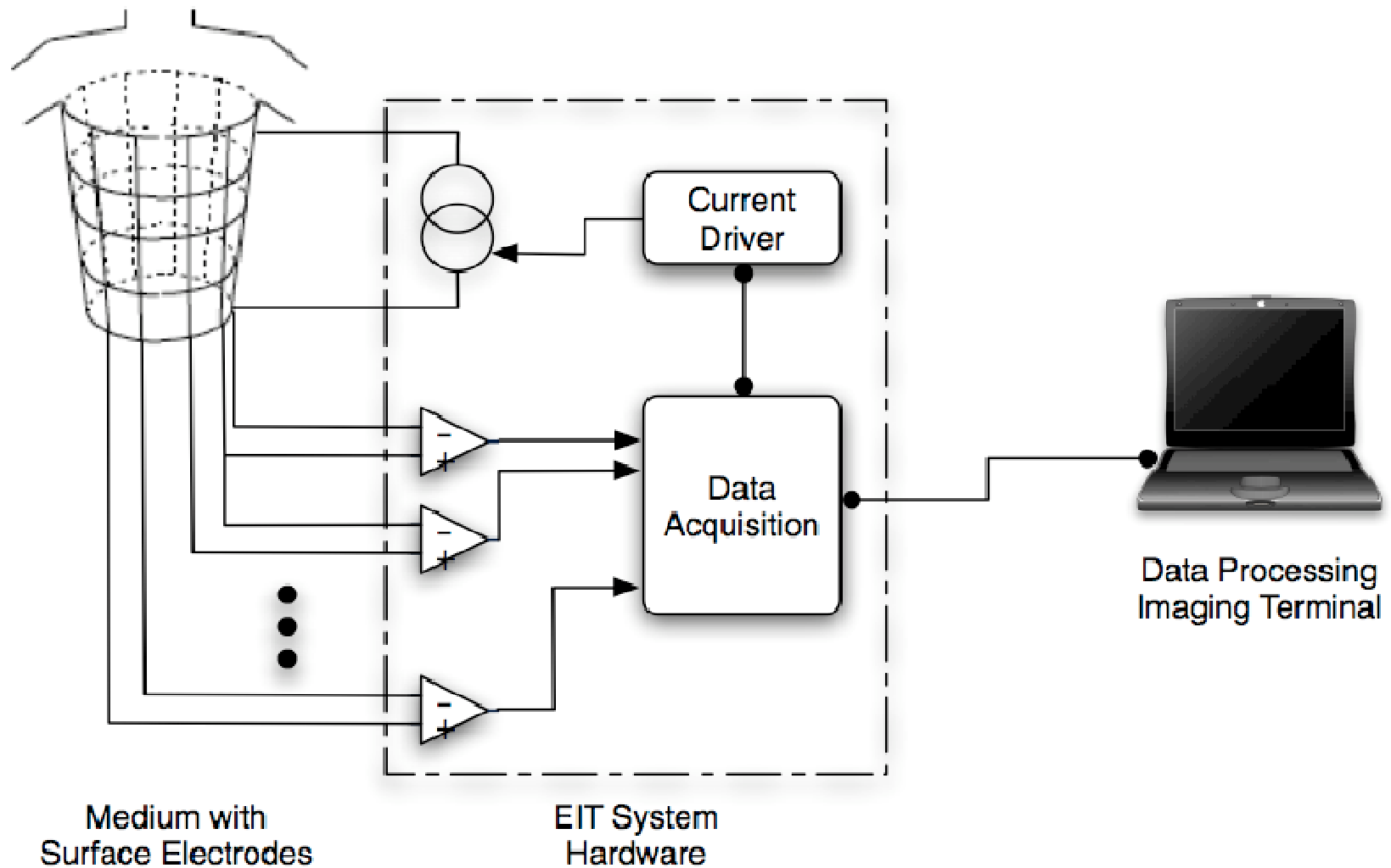
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November 9<sup>th</sup>, 2006

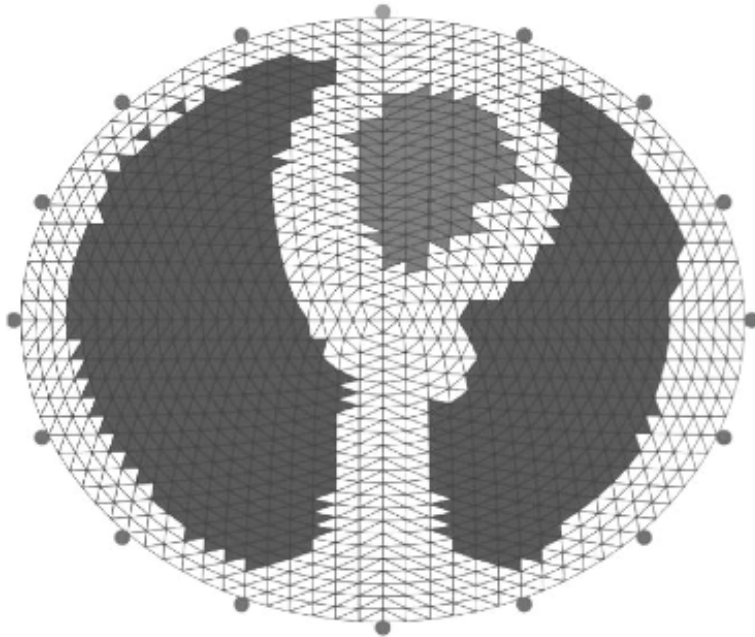
# Outline

- Electrical impedance tomography
- Image variability from boundary deformation
- Electrode displacement regularization
- Imaging of deformable media
- Conclusion

# Electrical impedance tomography

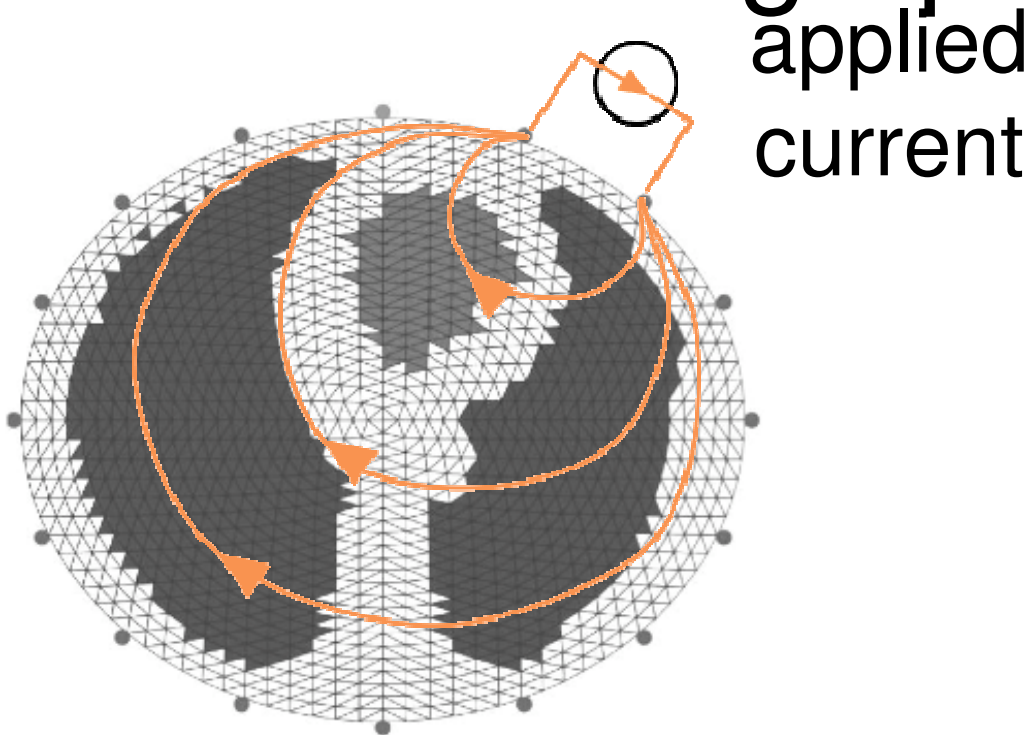


# Electrical impedance tomography



internal  
conductivity

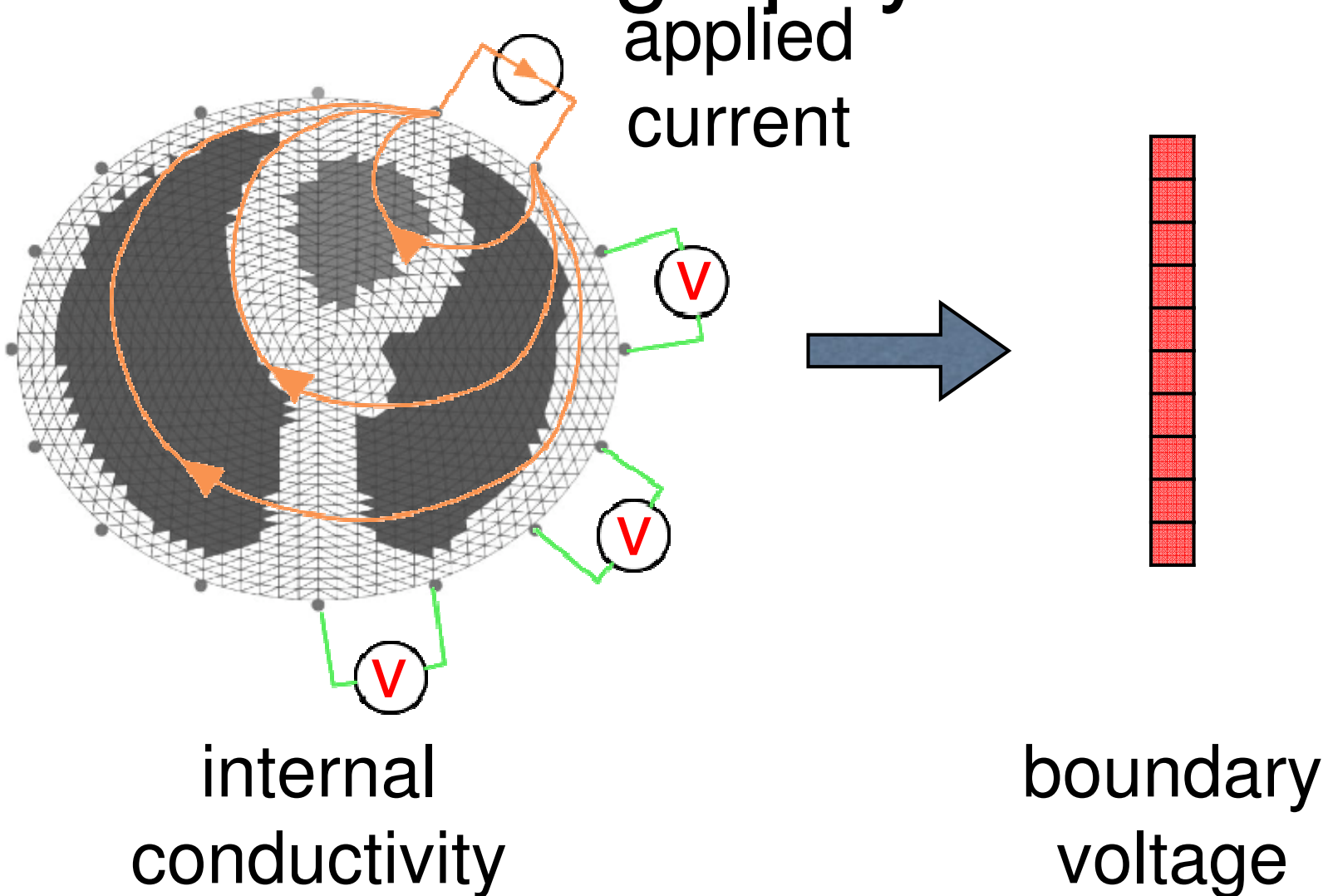
# Electrical impedance tomography



applied  
current

internal  
conductivity

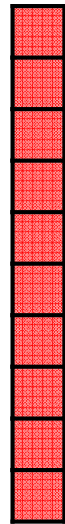
# Electrical impedance tomography



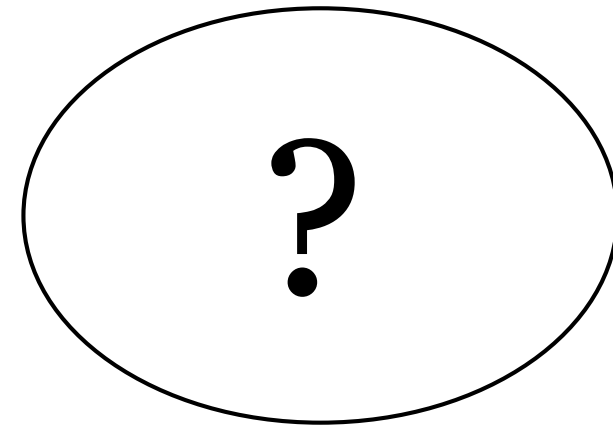
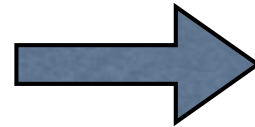
# Electrical impedance tomography

inverse problem

- non-linear
- unstable
- not unique

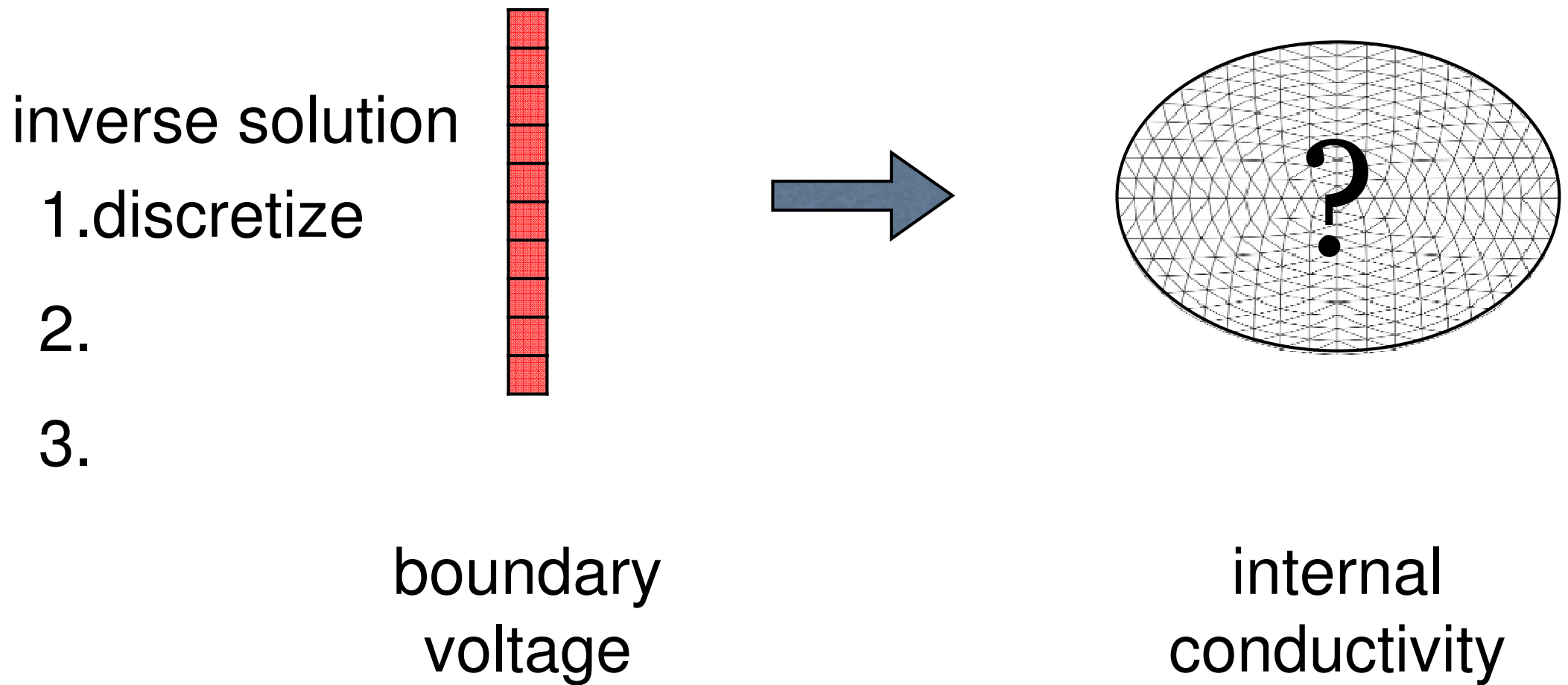


boundary  
voltage



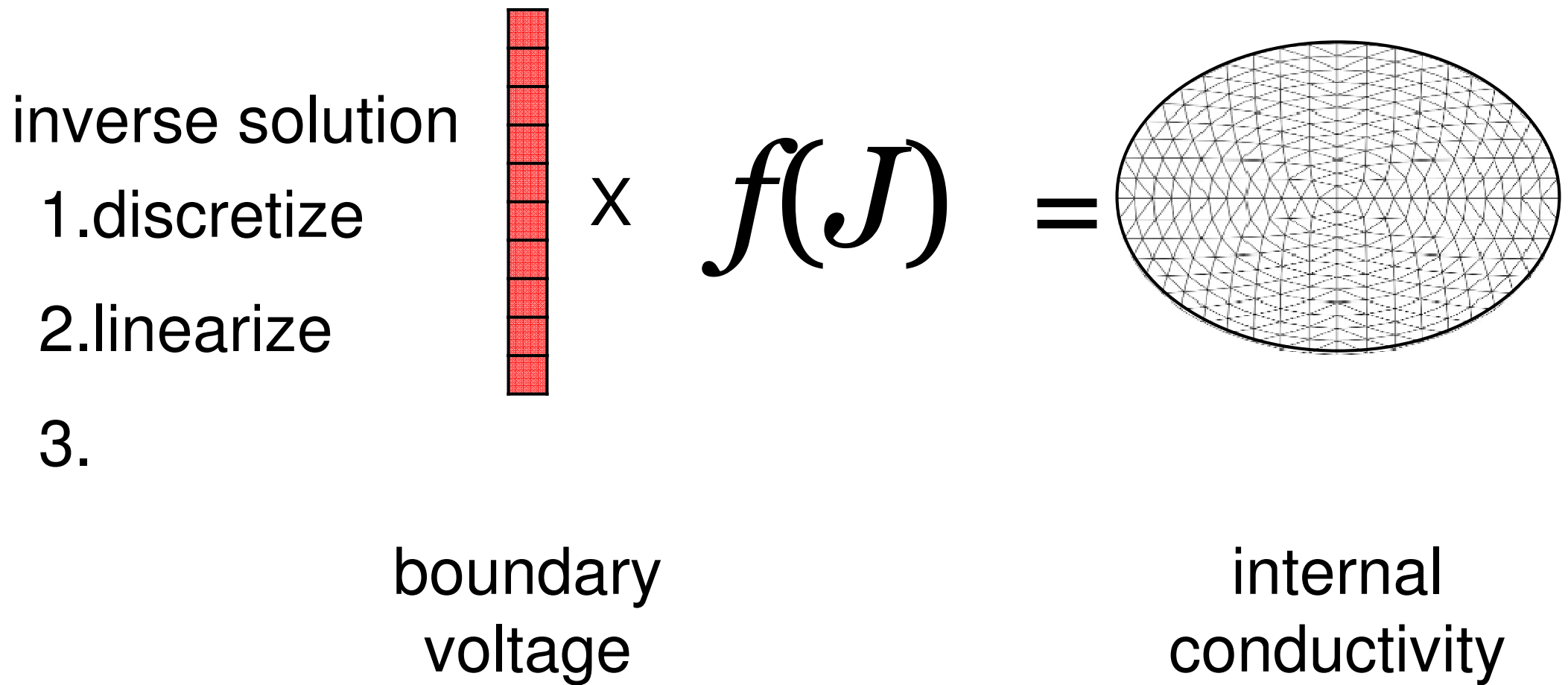
internal  
conductivity

# Electrical impedance tomography

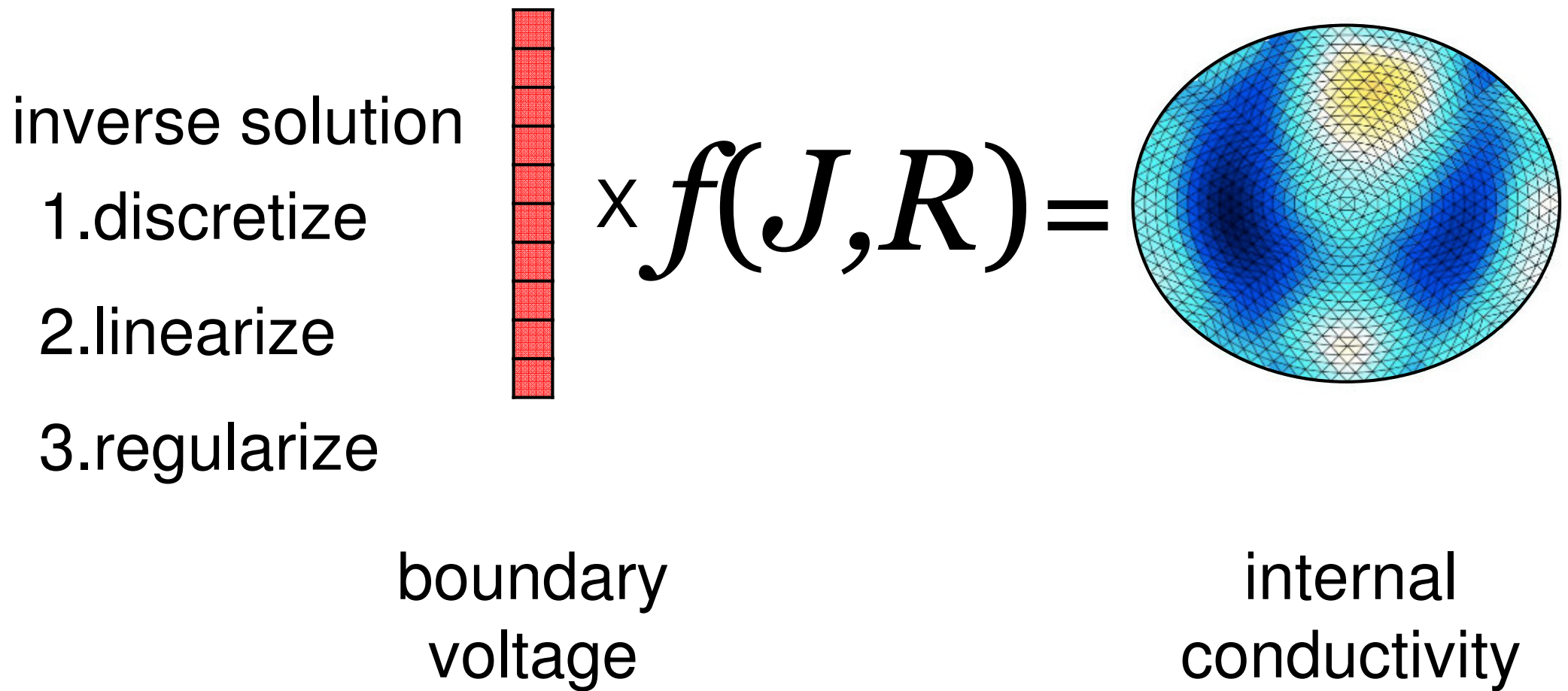




# Electrical impedance tomography



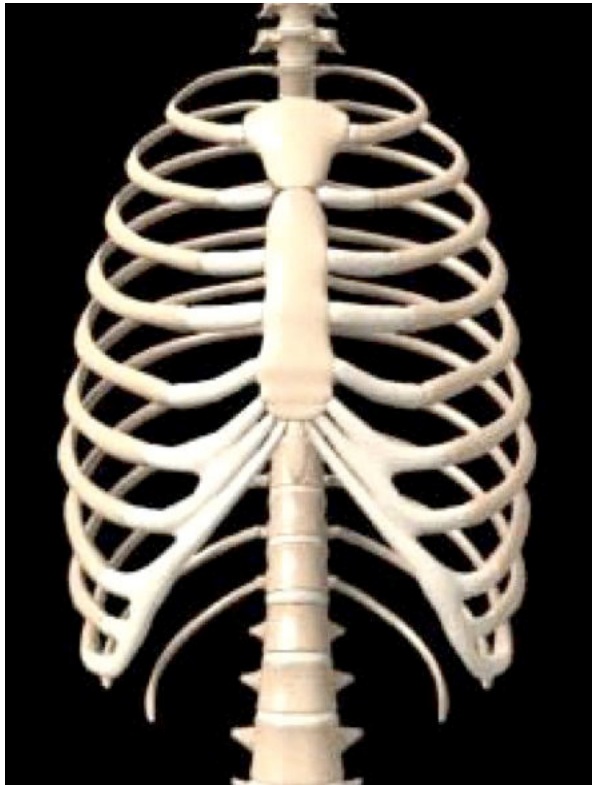
# Electrical impedance tomography



# Boundary deformation

- Thesis motivation
- the body is soft and is always in motion
  - body motion causes EIT errors because:
    - the boundary deforms
    - the electrodes move
  - monitoring may require movement e.g., breathing to monitor lung ventilation

# Boundary deformation

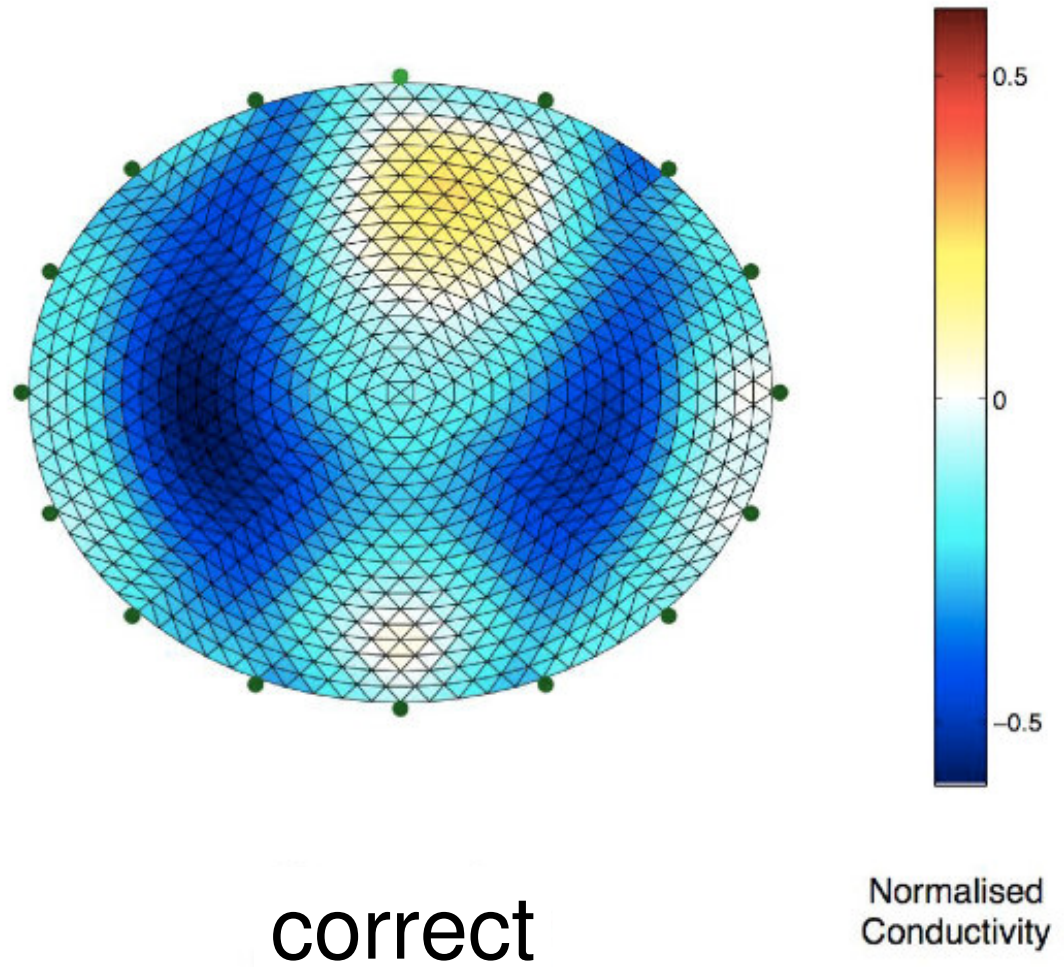
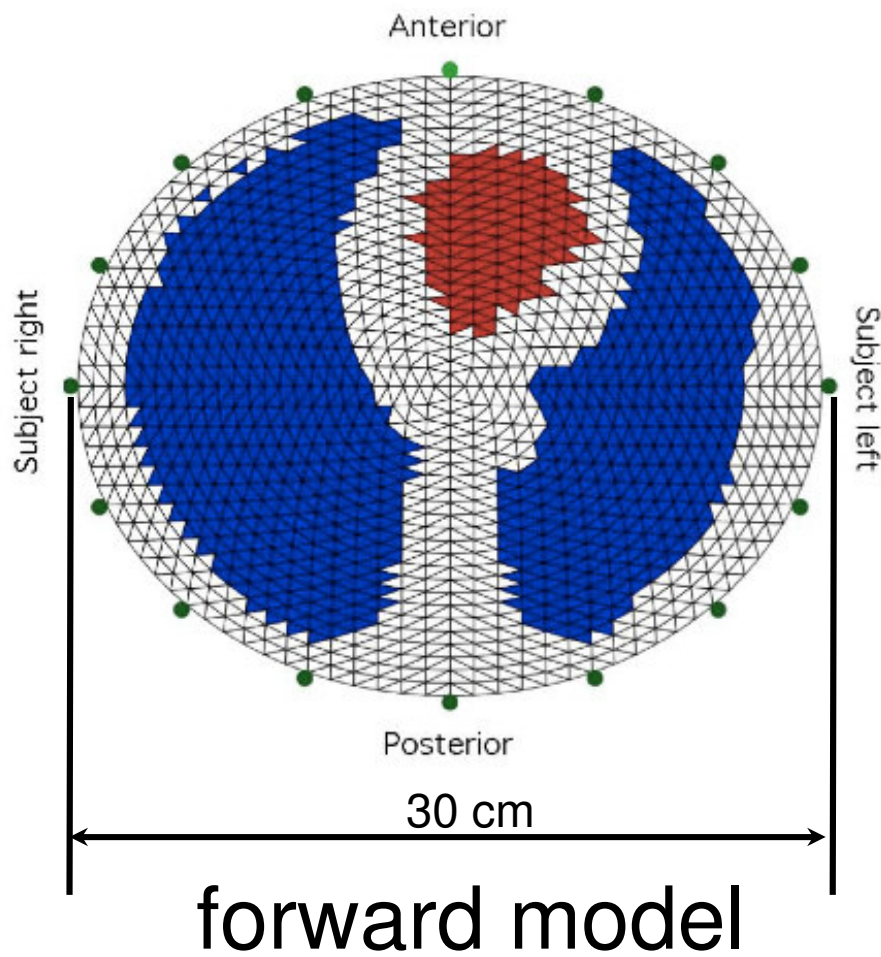


adapted from <http://www.brendoman.com/media/> (Oct. 12, 2006)

# Boundary deformation

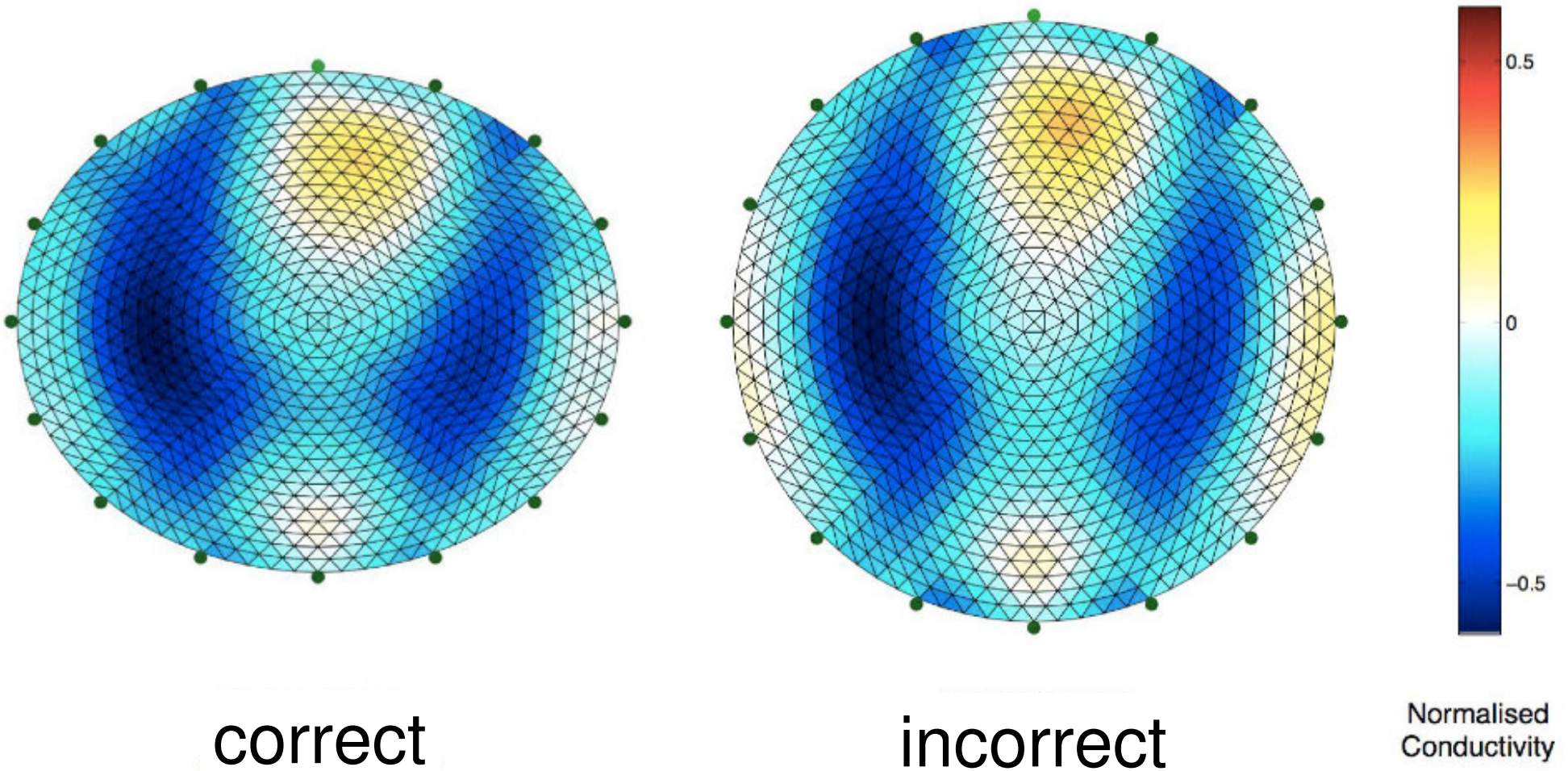
- study of deformation simulated EIT measurements to determine how much error is introduced from
  1. boundary deformation
  2. electrode displacement along boundary
- analysed results by
  1. inspection
  2. error measurement

# Boundary deformation



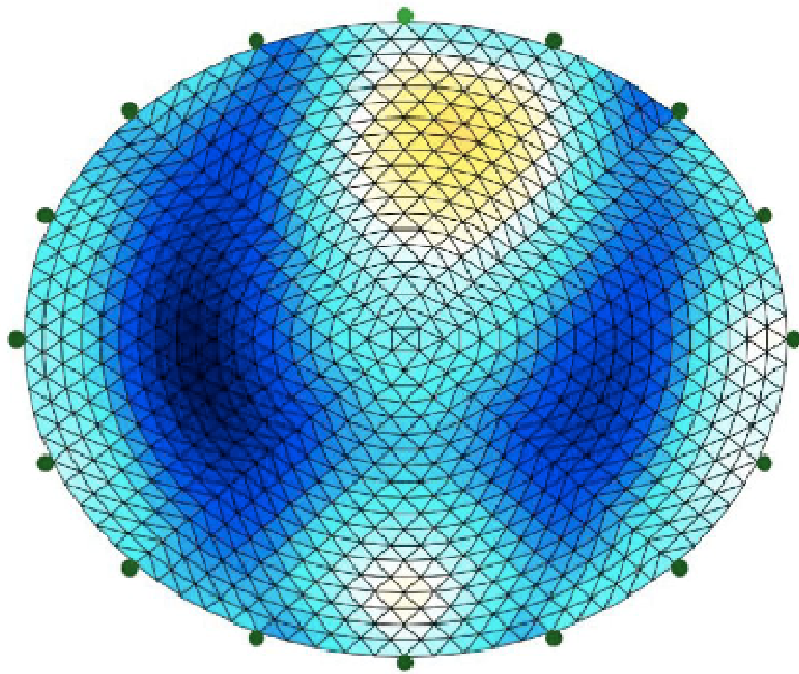


# Boundary deformation

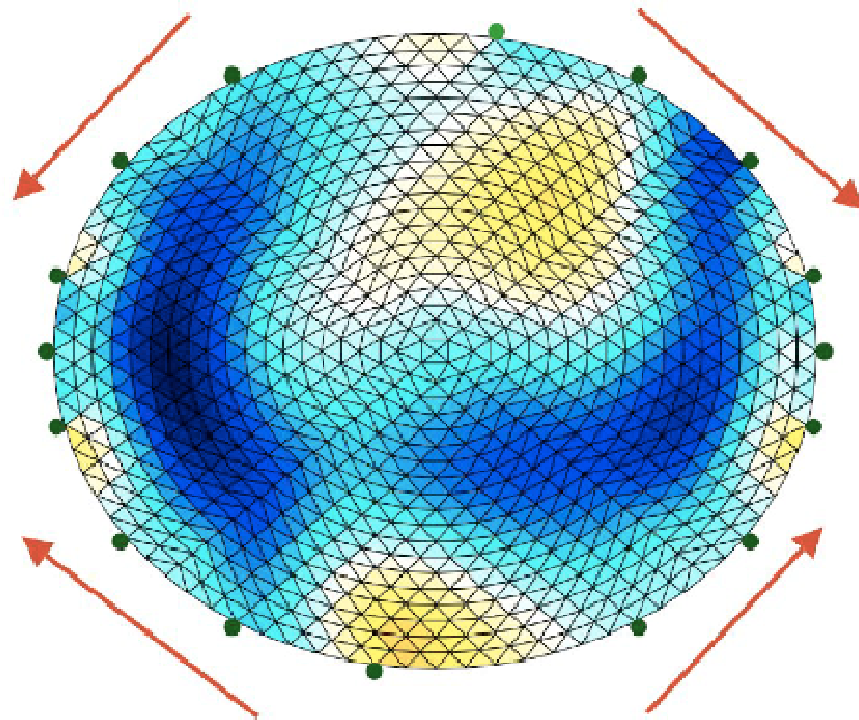


# Boundary deformation

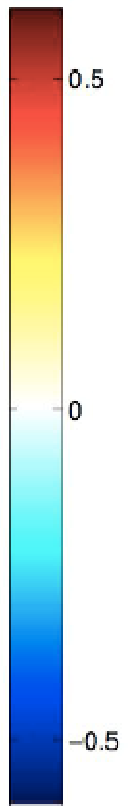
Electrodes moved by approx. 1.50 cm



correct



incorrect

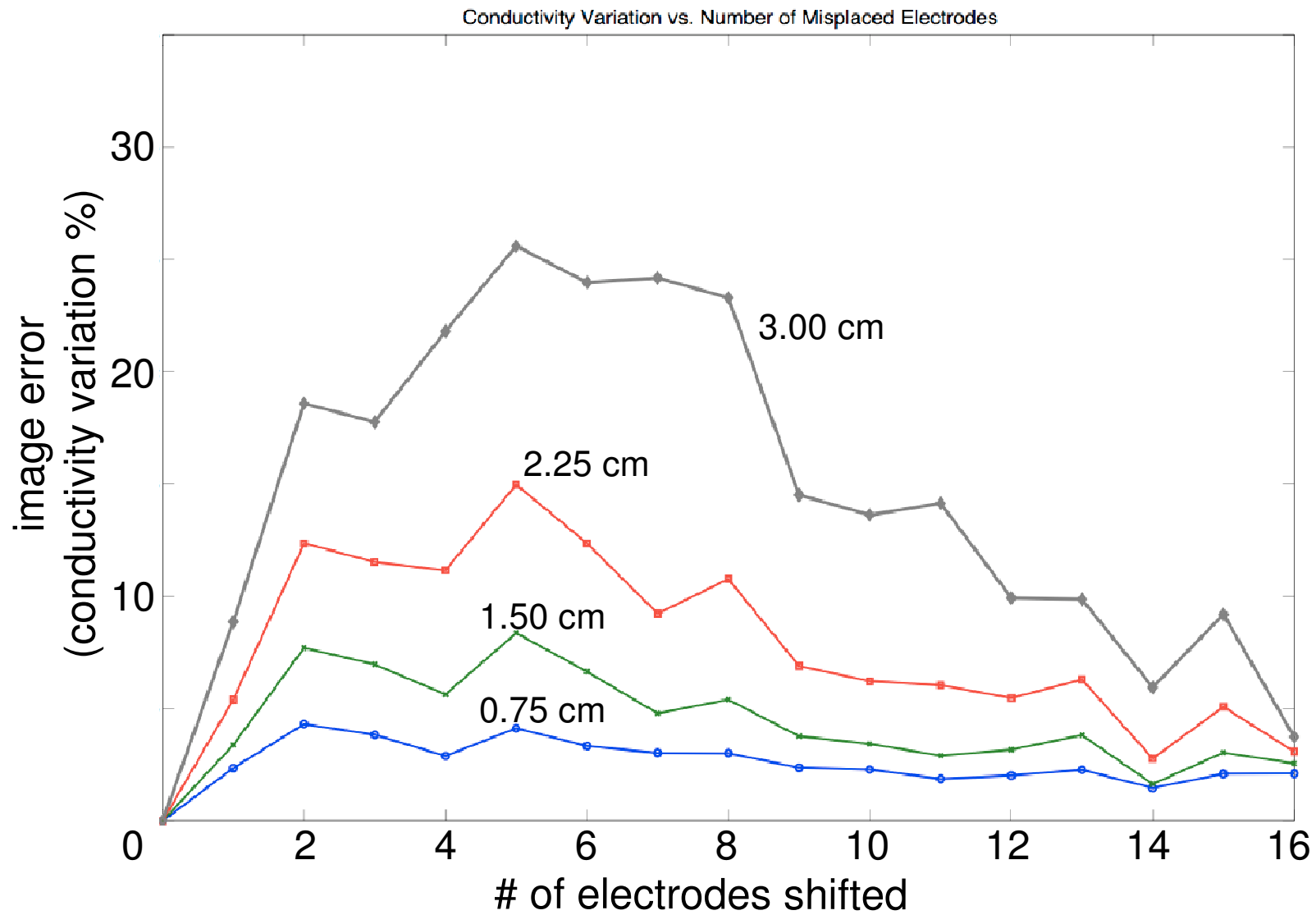


Normalised Conductivity



# Boundary

## deformation



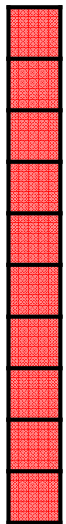
# Displacement regularization

The proposed solution includes an electrode displacement parameter into the inverse problem

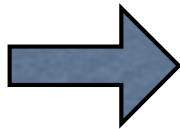
- define the system model
- define the augmented regularization matrix
- define the augmented Jacobian matrix

# Displacement regularization

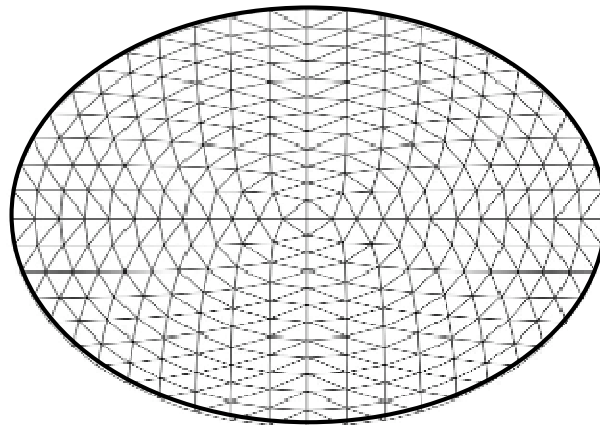
boundary  
voltage



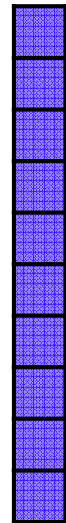
**v**



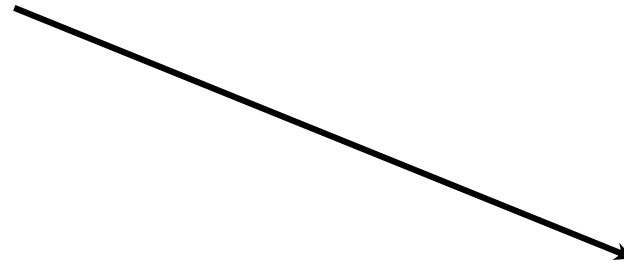
internal  
conductivity



image

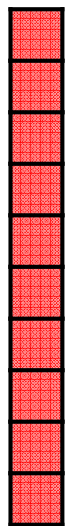


**x**

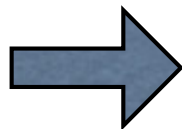


# Displacement regularization

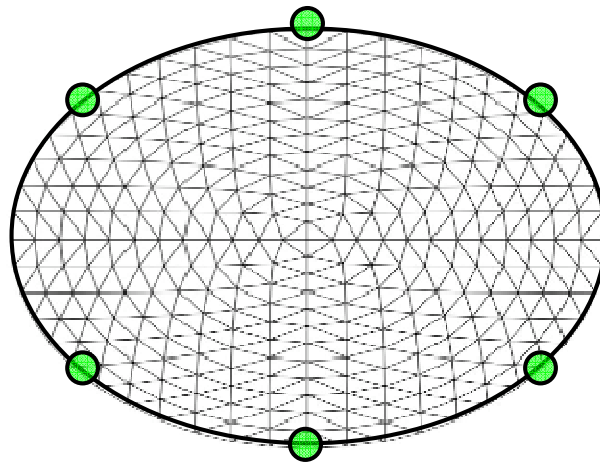
boundary voltage



$\mathbf{v}$

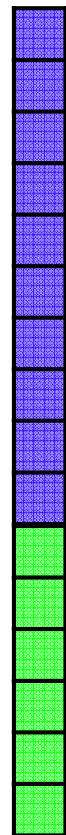


internal conductivity

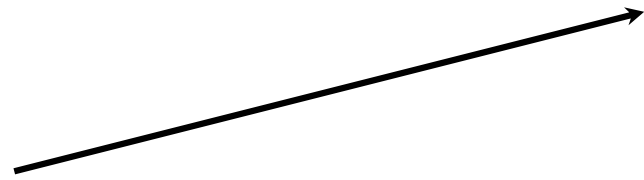
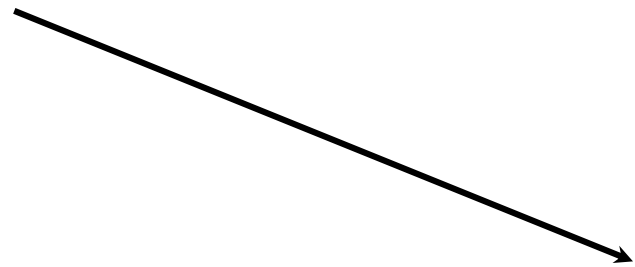


electrode displacement

image



$\mathbf{x}$



# Displacement regularization

$$\mathbf{x} = f(J, R) \mathbf{v}$$

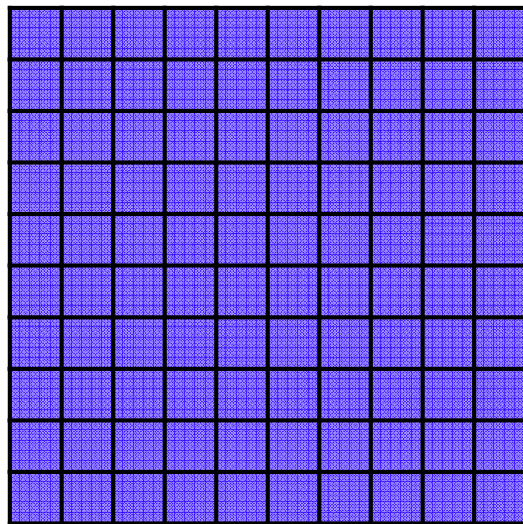
$$\mathbf{x} = (J^T J + \lambda^2 R)^{-1} J^T \mathbf{v}$$

# Displacement regularization

Building  $R$  -- *a priori* claims

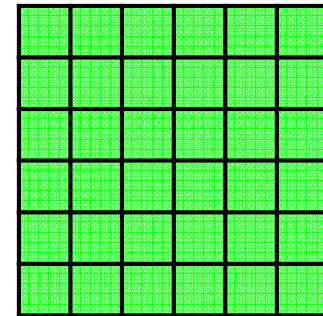
- conductivity distribution is smooth
- adjacent electrode displacements are correlated

# Displacement regularization



elements

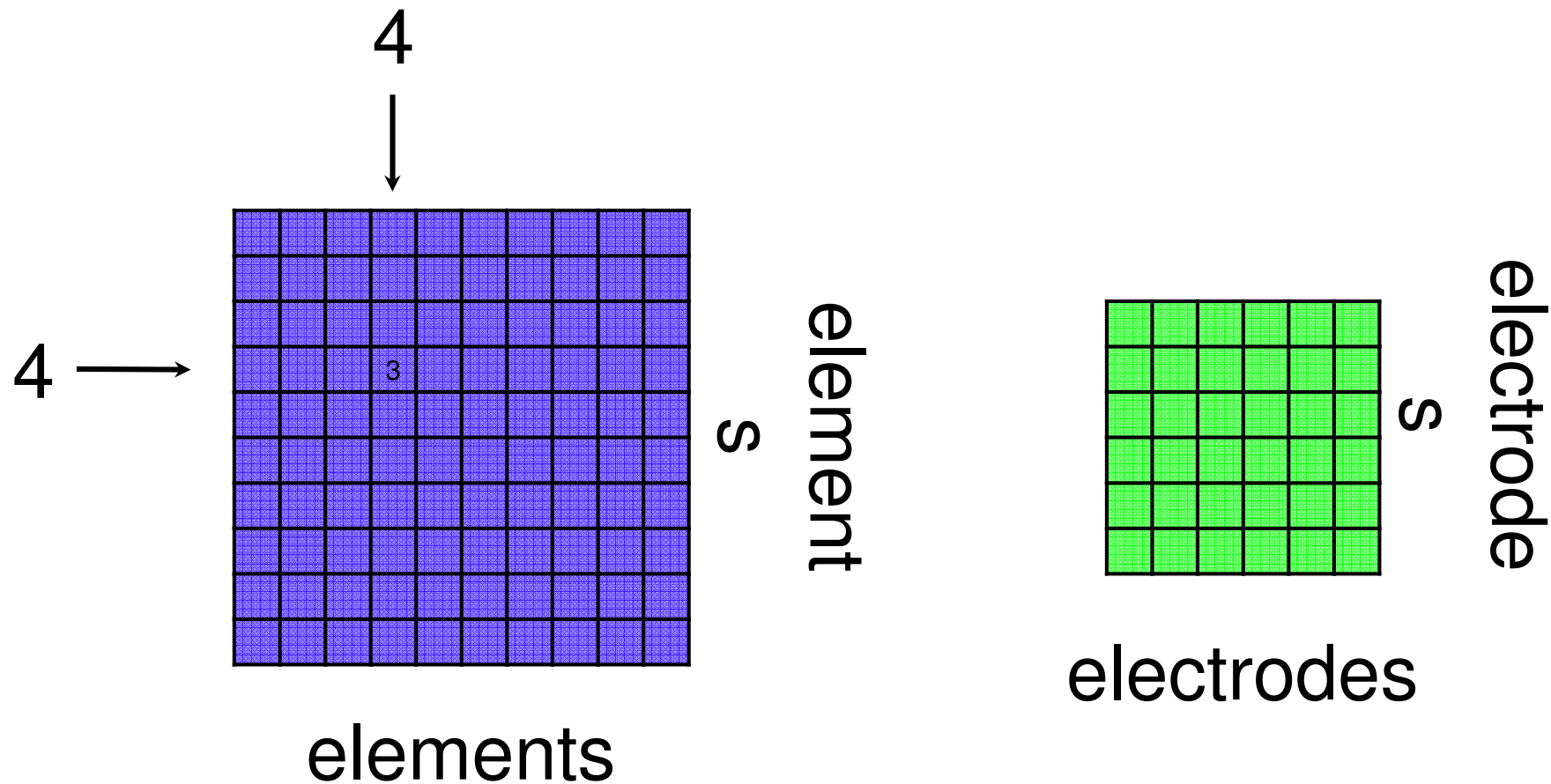
s  
element



electrodes

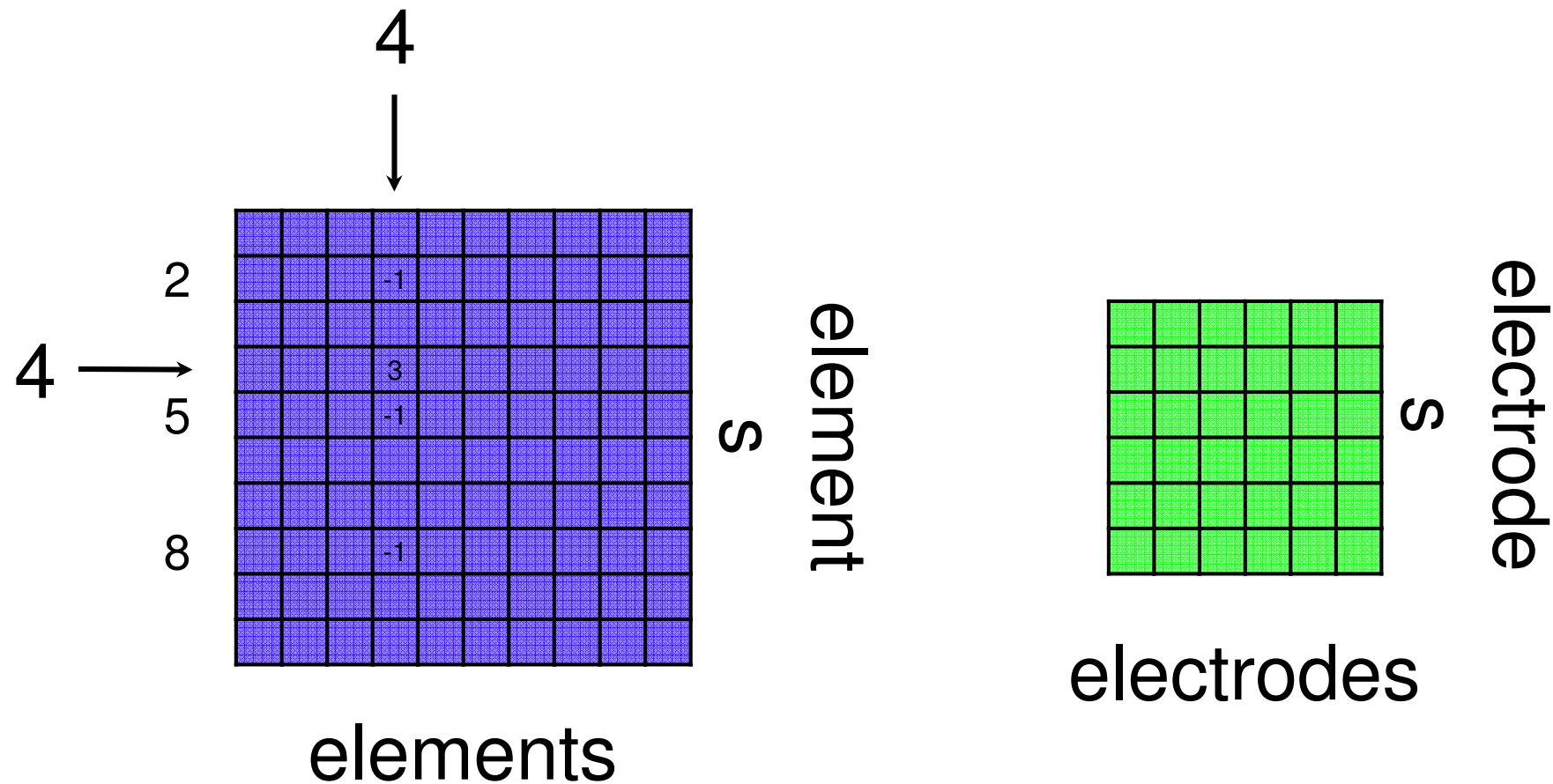
s  
electrode

# Displacement regularization

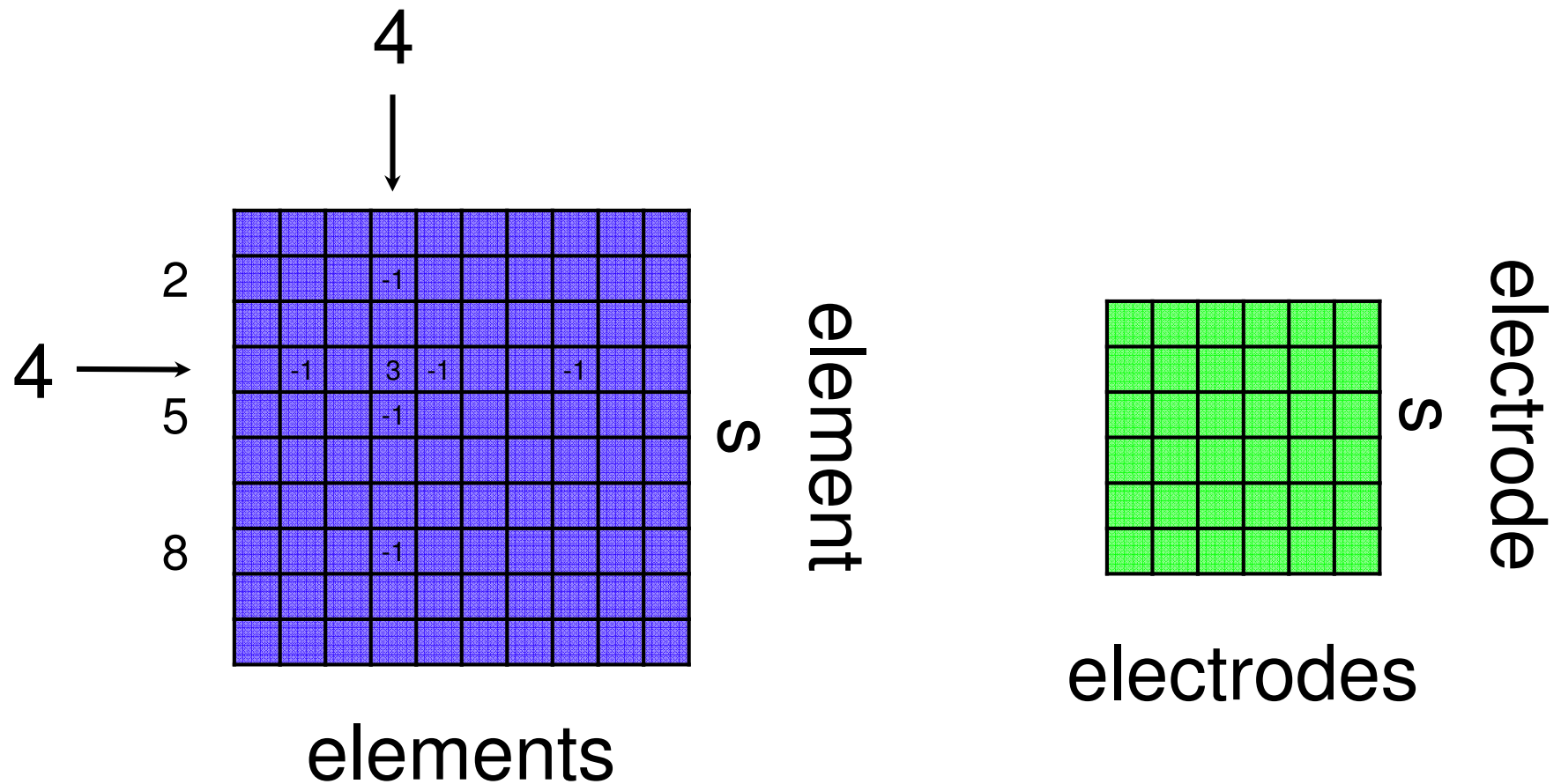




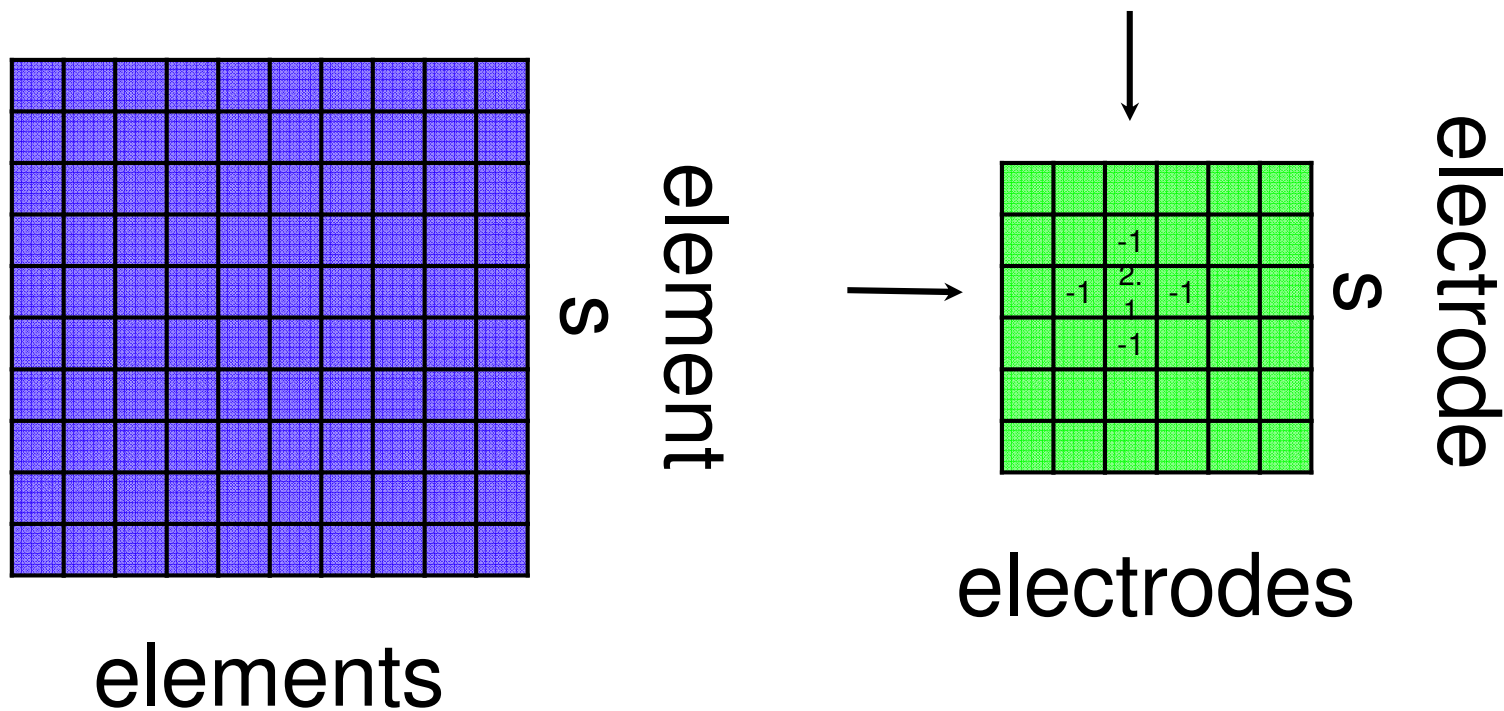
# Displacement regularization



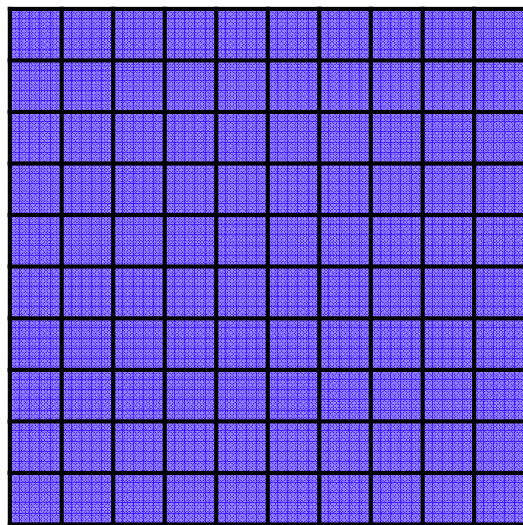
# Displacement regularization



# Displacement regularization



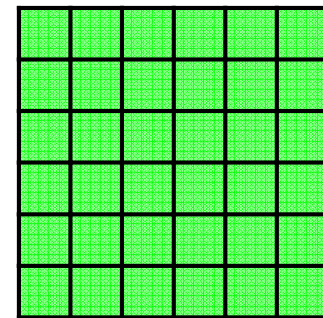
# Displacement regularization



elements

s  
element

$\mu^2$



electrodes

s  
electrode

# Displacement regularization

$$R = \begin{bmatrix} \text{blue grid} & 0 \\ 0 & \text{green grid} \end{bmatrix}$$

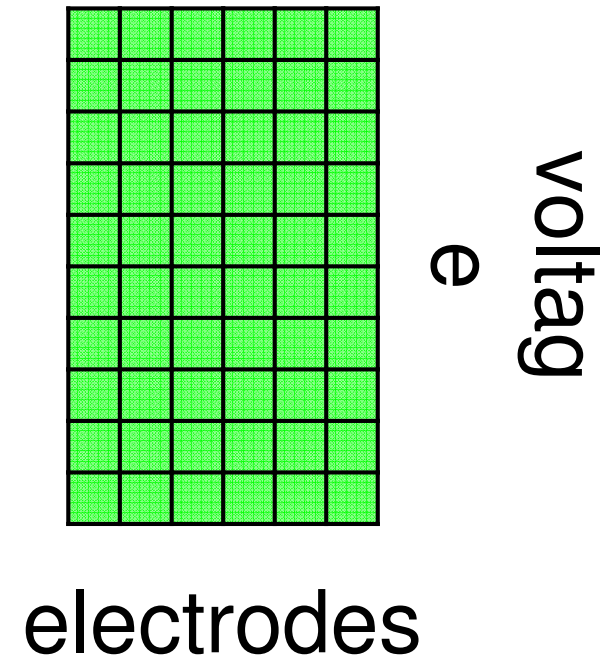
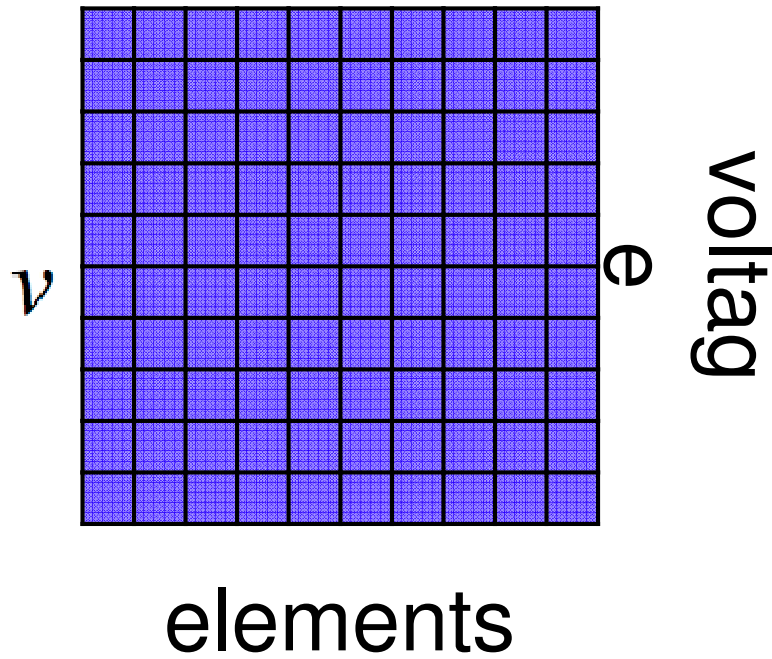
The matrix  $R$  is represented as a block matrix. The top-left block is a blue grid, the top-right block is 0, the bottom-left block is 0, and the bottom-right block is a green grid labeled  $\mu^2$ .

# Displacement regularization

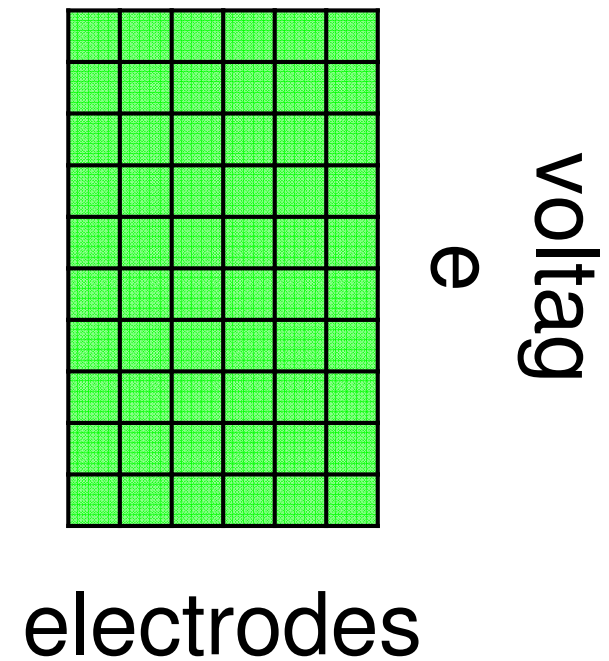
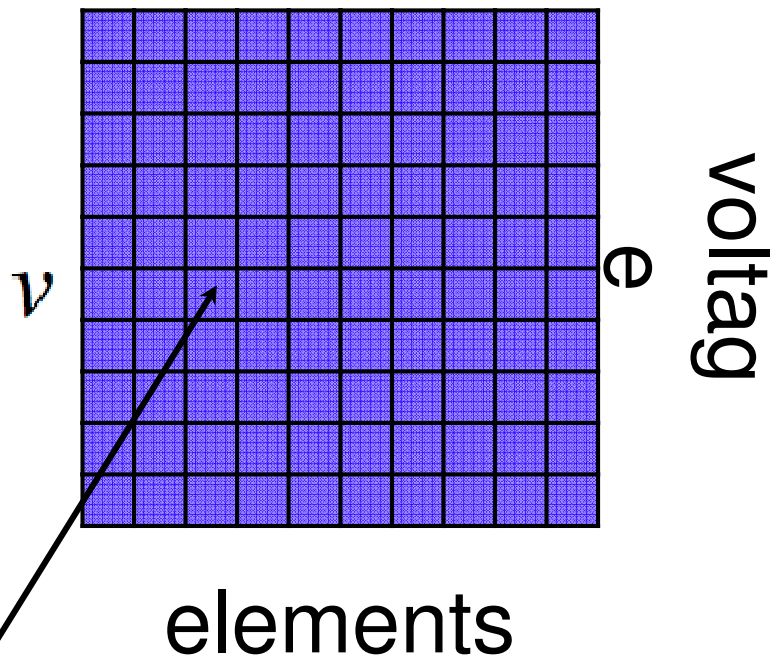
Building  $J$  -- sensitivity to input change

- conductivity change will affect boundary voltage
- displacements will affect boundary voltage

# Displacement $\sigma$ regularization



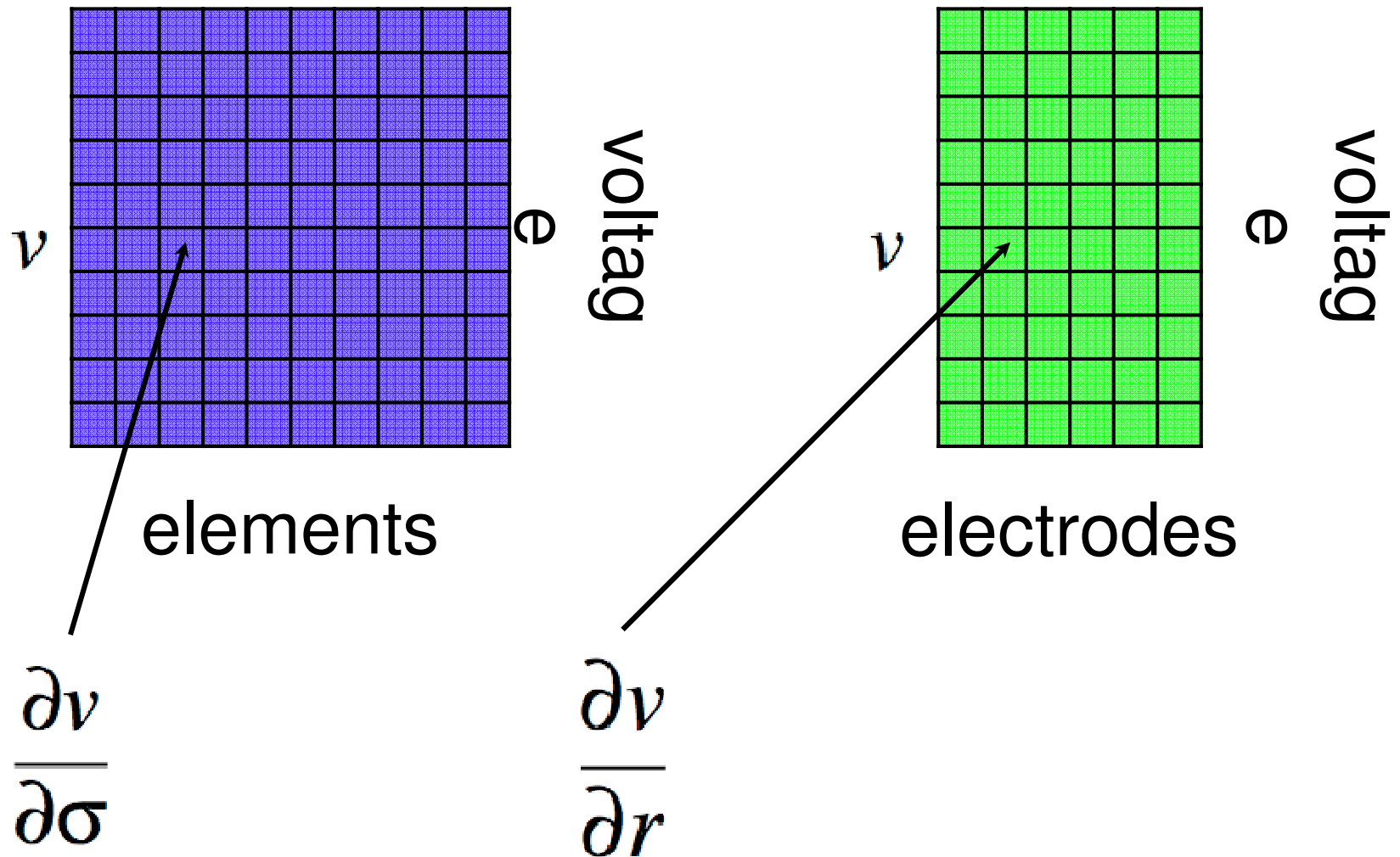
# Displacement $\sigma$ regularization



$$\frac{\partial v}{\partial \sigma} \approx \frac{v(\sigma + \Delta\sigma) - v(\sigma)}{\Delta\sigma}$$



# Displacement $\sigma$ regularization $r$



# Displacement regularization

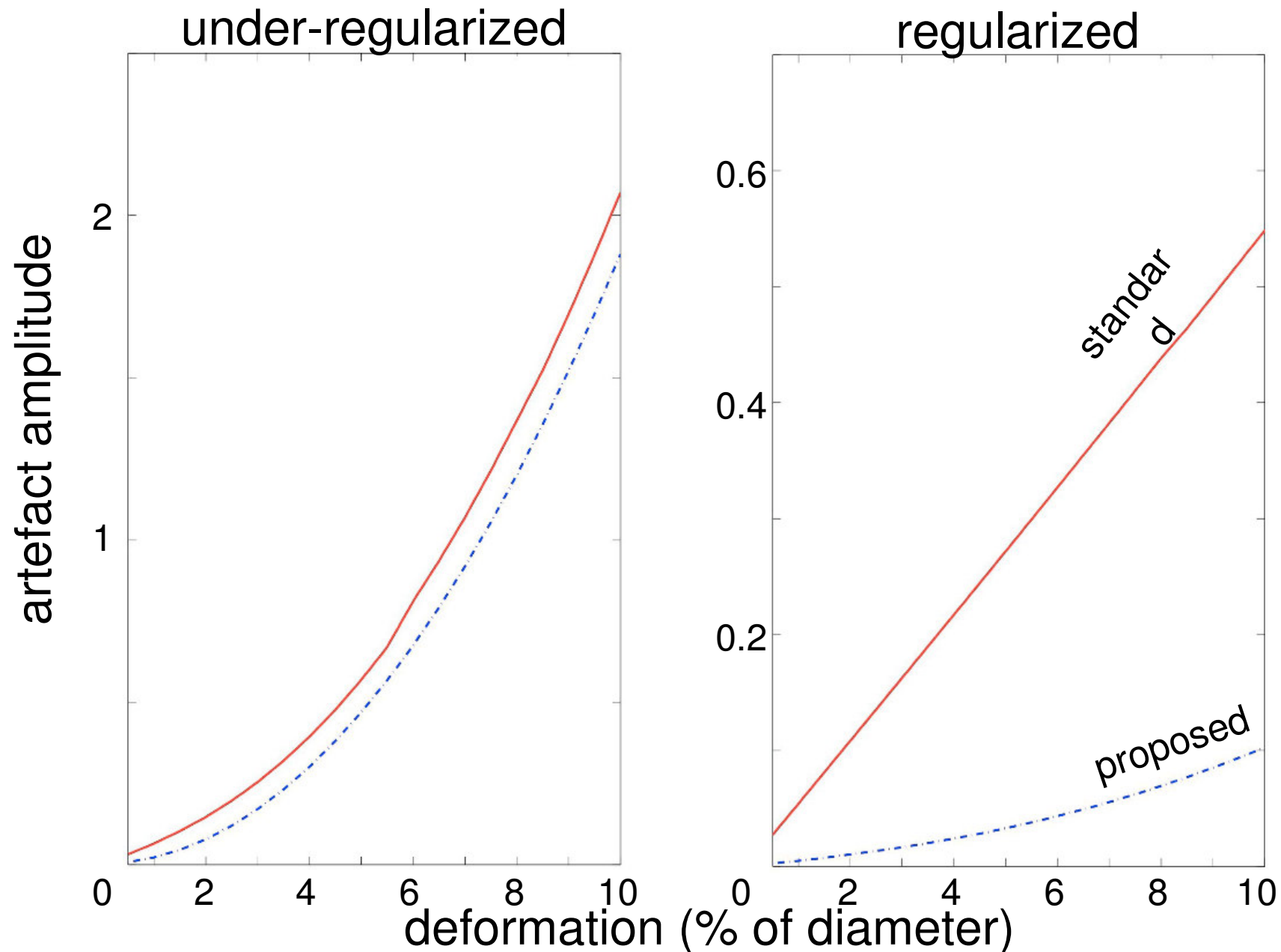
$$\mathbf{J} = \left[ \begin{array}{c|c} \text{Blue Grid} & \text{Green Grid} \end{array} \right]$$

# Algorithm performance

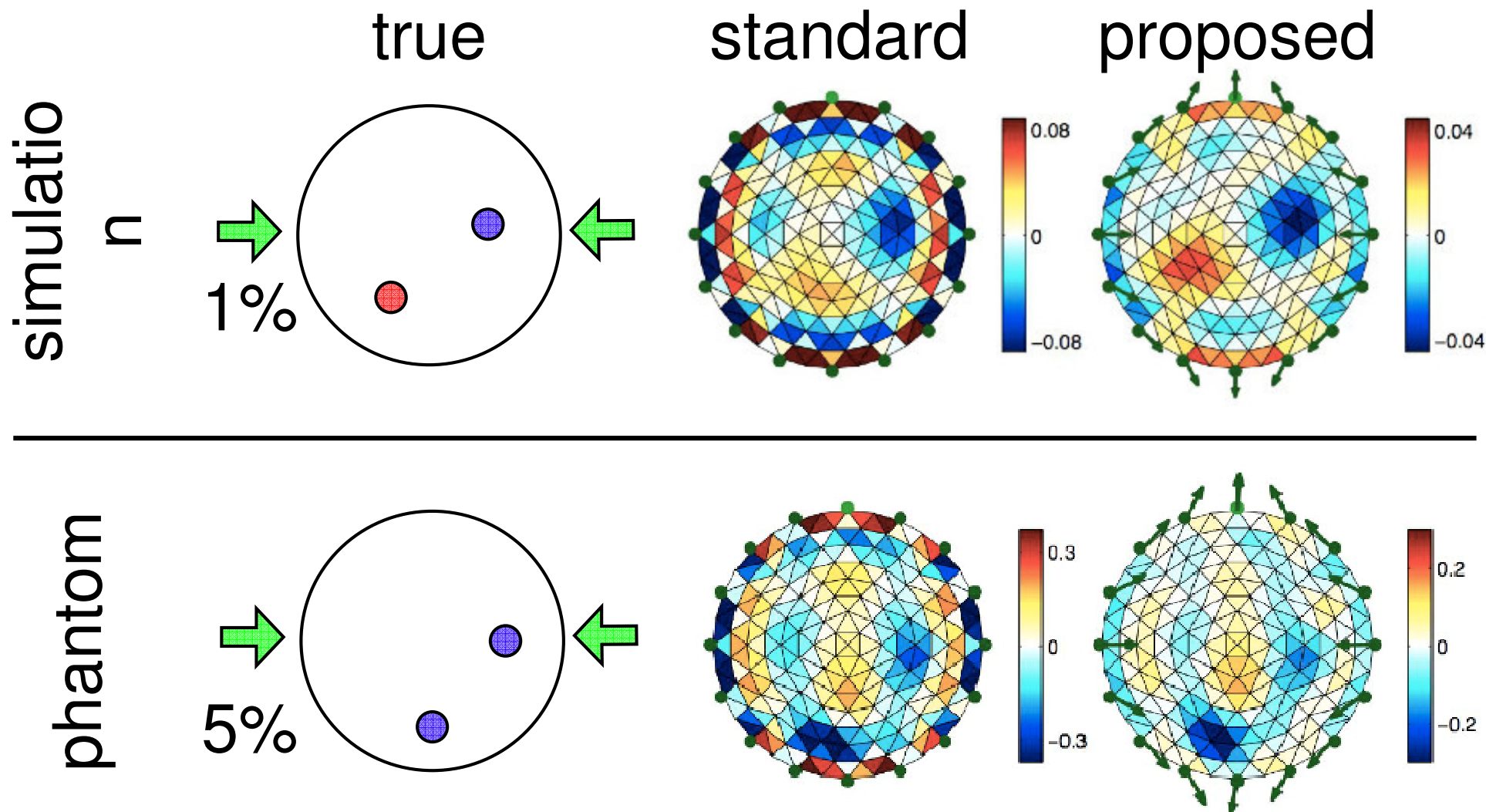
Results of a comparison to the standard algorithm

- no change in position accuracy
- marginal improvement in image resolution
- large improvement in artefact reduction
- calculates electrode displacements

# Algorithm performance



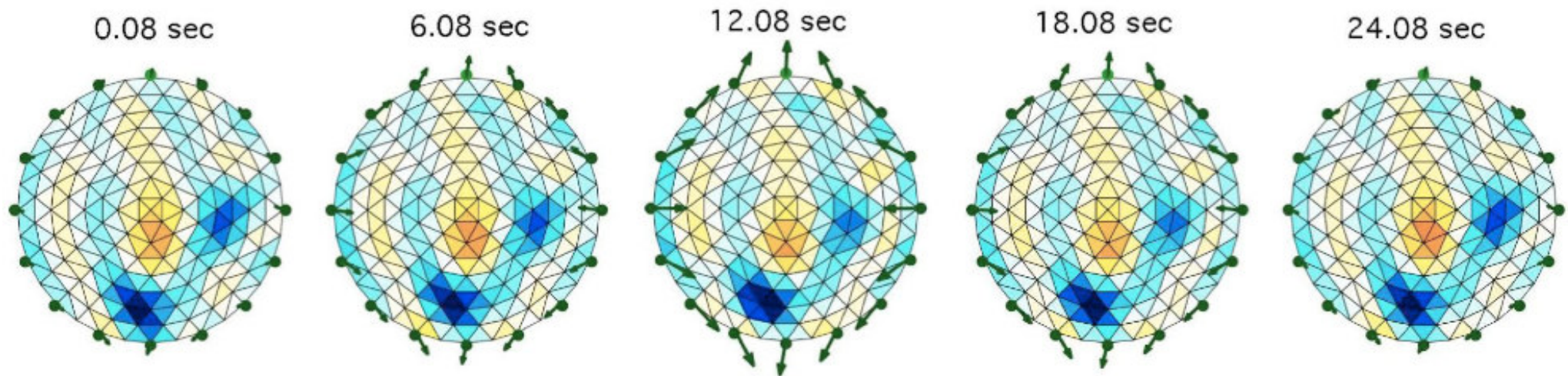
# Imaging deformable media



# Imaging deformable media

Phantom time series:

- 6 sec. increments
- periodic 5% deformation





# Imaging deformable media

Human TLC-RC breathing: 1.2 sec.

increments

10.8 sec

12 sec

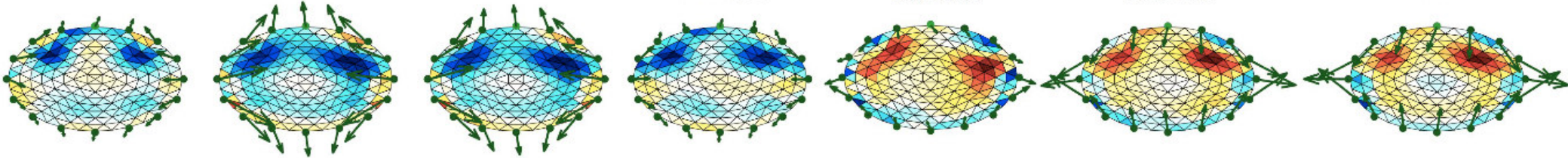
13.2 sec

14.4 sec

15.6 sec

16.8 sec

18 sec



Human “paradoxical” breathing: 1.2 sec.

increments

6 sec

7.2 sec

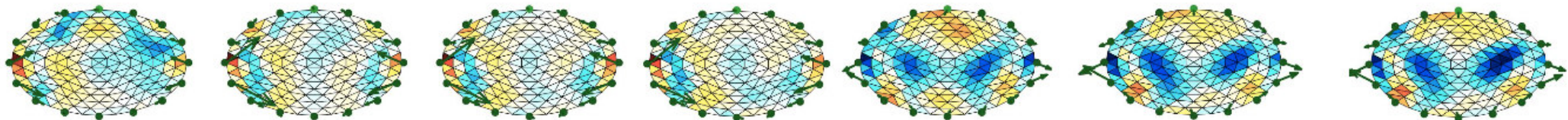
8.4 sec

9.6 sec

10.8 sec

12 sec

13.2 sec



# Conclusion

This thesis

- studied & quantified the effect of boundary deformation
- proposes an algorithm that compensates & calculates electrode displacement
- provides evidence supporting the use of EIT for deformable media



# Contributions

## journal

Soleimani, M., **Gomez-Laberge, C.**, and Adler, A. (2006) Imaging of conductivity changes and electrode movement in electrical impedance tomography. *Physiological Measurement*. 27:S103-S113

## conferences

**Gomez-Laberge, C.**, and Adler, A. (2006) Imaging of electrode movement and conductivity change simulations in electrical impedance tomography. In *Proceedings IEEE CCECE*. Ottawa, Canada.

McLeod, C., **Gomez-Laberge, C.**, and Adler, A. (2006) Reduction of electrode position errors in clinical imaging. In *Conference 7<sup>th</sup> Biomedical Applications of Electrical Impedance Tomography*. Seoul, South Korea.