The op-amp is ideal, with $V_{CC} = 10\,\text{V}$ and $V_{EE} = -10\,\text{V}$. The diode forward voltage, $V_D = 0.7\,\text{V}$.

- What is the frequency of oscillation.
- Sketch $V_o$ when the oscillation amplitude has stabilized.
- Indicate the approximate voltage of oscillation on the sketch.

This is a Wien bridge sine-wave oscillator. It oscillates because $G = 1 + \frac{91\,\text{k}\Omega}{20\,\text{k}\Omega} = 5.55 > 3$.

- What is the frequency of oscillation.
  \[ \omega = (RC)^{-1} = (35\,\text{k}\Omega \times 27\,\text{nF})^{-1} = 1058.2\,\text{rad/s} \]
  \[ f = \frac{1}{2\pi}\omega = 168.4\,\text{Hz} \]
- Sketch $V_o$ when the oscillation amplitude has stabilized.
  The oscillation will be roughly sine shaped at $f = 168.4\,\text{Hz}$
- Indicate the approximate voltage of oscillation on the sketch.
  amplitude stabilized at $\pm0.7\,\text{V}$.
The op-amp is ideal, with $V_{CC} = 2\, \text{V}$ and $V_{EE} = -2\, \text{V}$.

![Circuit Diagram]

Initial conditions are: $V_- = 0$ and $V_o = +V_{CC}$.

Sketch as a function of time: 1) $V_-$, 2) $V_+$, 3) $V_o$

- $V_o$ will switch between $\pm 2\, \text{V}$
- $V_+$ will switch between $\pm 2\, \text{V}$
  \[
  \frac{69\, \text{k}\Omega}{69\, \text{k}\Omega + 39\, \text{k}\Omega} = 1.28\, \text{V}
  \]
- $V_+$ will exponentially rise between $\pm 1.28\, \text{V}$.

Timing will be symmetric between +ve and -ve pulses.

\[
(V_f - V_\infty) = (V_i - V_\infty)e^{-t/\tau},
\]
were $\tau = RC = 27\, \text{k}\Omega \times 35\, \text{nF} = 0.945\, \text{ms}$

For the -ve transition, $V_i = 1.28\, \text{V}$, $V_f = -1.28\, \text{V}$, and $V_\infty = -2\, \text{V}$.

\[
t = \tau \ln \left( \frac{V_f - V_\infty}{V_i - V_\infty} \right) = (0.945\, \text{ms}) \ln \left( \frac{1.28 - (-2)}{-1.28 - (-2)} \right) = 1.43\, \text{ms}
\]
Initial conditions are that the charge on the capacitor is zero. $V_{CC} = 9\, \text{V}$.

- Sketch $V_o$, $V_A$ and $V_B$.

- What is the length of the $V_o = \text{high}$ and $V_o = \text{low}$ outputs?

This configuration is similar, but not the same as the configuration discussed in class. Normally $V_+$ of the upper comparator is connected to $V_B$. This means that the upper transitions will not happen at $V_B = \frac{2}{3}V_{CC}$, but instead when $V_A = \frac{2}{3}V_{CC}$. At this time, we calculate

$$i = \frac{V_{CC} - \frac{2}{3}V_{CC}}{52\, \text{k}\Omega} = \frac{9\, \text{V} - 6\, \text{V}}{52\, \text{k}\Omega} = 3\, \text{V}/52\, \text{k}\Omega = 57.69\, \mu\text{A}.$$  

Using $i$, we calculate $V_B = V_A - i(12\, \text{k}\Omega) = 5.31\, \text{V}$.

Another way to see this is to think about Capacitor $C$ charging until $V_A = 2/3V_{CC}$ (RESET) and discharging until $V_B = 1/3V_{CC}$ (SET). In the usual 555 astable configuration, the trigger and threshold pins (pins 2 and 6) are both connected to the top of $C$, so $V_A = V_B$, however in the above circuit $V_A$ and $V_B$ are related by

$$V_A = V_B + (V_{CC} - V_B)\frac{R_B}{R_A + R_B}$$  

(voltage divider). Setting $V_A = 2/3V_{CC}$ and rearranging, RESET occurs when $V_B$ reaches voltage $V_R$ given by

$$V_R = \left(\frac{2}{3} - \frac{R_B}{R_A + R_B}\right)\left(\frac{R_A + R_B}{R_A}\right)V_{CC}$$

$$V_R = \left(\frac{2}{3} - \frac{12\, \text{k}\Omega}{52\, \text{k}\Omega + 12\, \text{k}\Omega}\right)\left(\frac{52\, \text{k}\Omega + 12\, \text{k}\Omega}{52\, \text{k}\Omega}\right)9\, \text{V} = 5.31\, \text{V}$$

The durations of the charge and discharge half-cycles are then given by the usual formula

$$t = RC \ln \left(\frac{V_\infty - V_i}{V_\infty - V_f}\right) = (0.49)RC$$
with \( V_i = V_{CC}/3 \), \( V_f = V_R \), \( V_\infty = V_{CC} \) and \( R = R_A + R_B \) for the charge half-cycle and \( V_i = V_R \), \( V_f = V_{CC}/3 \), \( V_\infty = 0 \) and \( R = R_B \) for the discharge half-cycle. \( V_o = V_{CC} \) during the charge period and \( V_o = 0 \) V during the discharge period. Thus:

- \( t_{\text{high}} = 0.49 \times 56 \mu F \times (52 \text{k}\Omega + 12 \text{k}\Omega) = 1.76 \text{ms} \)
- \( t_{\text{low}} = 0.49 \times 56 \mu F \times (12 \text{k}\Omega) = 0.33 \text{ms} \)

The shape of \( V_B \) is essentially the same as that of the regular 555 astable configuration, rising and falling exponentially between the two limits - except that the upper limit is \( V_R \) instead of \( 2/3V_{CC} \). Meanwhile \( V_A \) rises exponentially from somewhat above \( 1/3V_{CC} \) to \( 2/3V_{CC} \), and then drops immediately to zero for the duration of the discharge half-cycle since it is connected directly to the discharge pin (pin 7).