

# CARLETON UNIVERSITY

Department of Systems and Computer Engineering

SYSC 4600 – Digital Communications – Quiz 2 Solutions – Fall 2015

Professor H. Yanikomeroglu

05 October 2015

100 pts, 20 mins

Name:

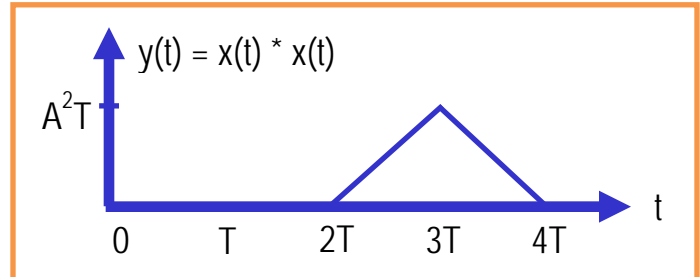
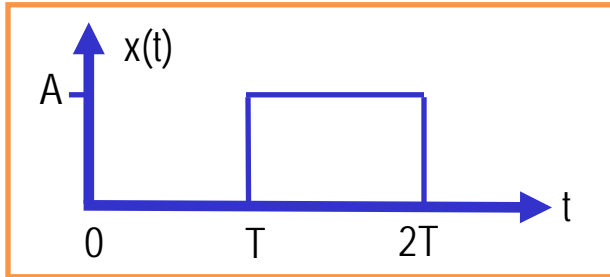
Student #:

E-mail:

Q1 [60 pts] – Convolution & FT:

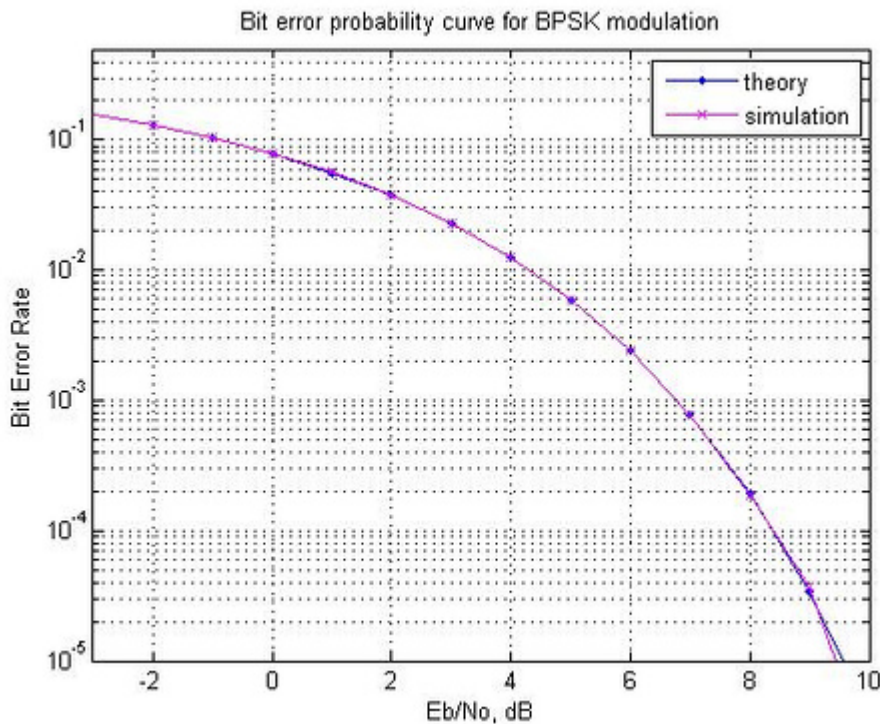
a)  $y(t) = x(t) * x(t)$ . Sketch  $y(t)$ .

b)  $|X(f)|$  is the magnitude of  $x(t)$ 's FT. Write the expression for  $|X(f)|$  and sketch it.



$$|X(f)| = AT |\text{sinc}(fT)|$$

Q2 [40 pts] – Power Calculations: In the 4G LTE wireless networks, the bandwidth is assigned to applications in terms of “resource blocks (RBs)”. The bandwidth of one RB is 200 KHz.



Consider an LTE application that uses BPSK modulation; the corresponding BER versus SNR ( $E_b/N_0$ ) relation is given in the above figure. This application requires a BER of  $10^{-4}$  and it is assigned one RB.

The AWGN power spectral density is  $N_0 = -174$  dBm/Hz, and the receiver noise figure is 8 dB. Find the necessary received signal power,  $P_s$ , in Watts.

$$P_N = N_0 + B + F = -174 \text{ dBm/Hz} + 53 \text{ dBHz} + 8 = -113 \text{ dBm}$$

$$\text{BER} = 10^{-4} \rightarrow \text{SNR} = 8.5 \text{ dB}$$

$$\text{SNR} = P_S - P_N$$

$$P_S = \text{SNR} + P_N = 8.5 \text{ dB} + -113 \text{ dBm} = -104.5 \text{ dBm} = -134.5 \text{ dBW} = 3.55 \times 10^{-14} \text{ W}$$